# Lesson 15: Using Unique Triangles to Solve Real-World and Mathematical Problems

#### **Student Outcomes**

 Students use conditions that determine a unique triangle to construct viable arguments that angle measures and lengths are equal between triangles.

#### **Lesson Notes**

In Lesson 15, students continue to apply their understanding of the conditions that determine a unique triangle. In Lesson 14, they were introduced to diagrams of triangles that had pre-existing relationships, as opposed to the diagrams in Lesson 13 that showed distinct triangles with three matching, marked parts. This added a new challenge to the task of determining whether triangles were identical because some information had to be assessed from the diagram in order to establish a condition that would determine triangles as identical. In Lesson 15, students are exposed to yet another challenge where they are asked to determine whether triangles are identical and to show how this information can lead to further conclusions about the diagram (i.e., showing why a given point must be the midpoint of a segment). Problems in this lesson are both real-world and mathematical. All problems require an explanation that logically links given knowledge, a correspondence, and a condition that determines triangles to be identical; some problems require these links to yield one more conclusion. This lesson is an opportunity to highlight Mathematical Practice 1, giving students an opportunity to build perseverance in solving problems.

#### Classwork

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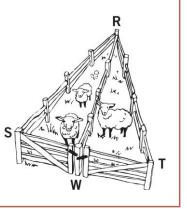
#### Example 1 (5 minutes)

#### Example 1

A triangular fence with two equal angles, , is used to enclose some sheep. A fence is constructed inside the triangle that exactly cuts the other angle into two equal angles: . Show that the gates, represented by and , are the same width.

There is a correspondencethat matches two pairs of angles ofequal measurement,and, and one pair of sides ofequal lengths shared side. The triangles satisfy the two angles and sideopposite a given angle condition.From the correspondence, we can concludethat, or that the gates are of equal width.

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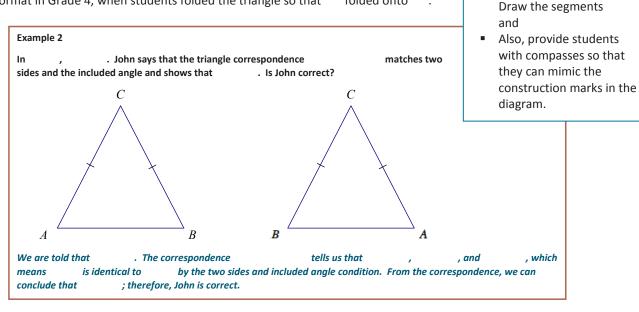
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If needed, provide a hint:

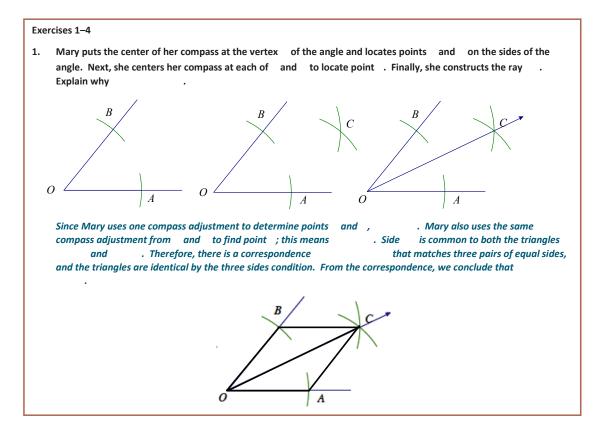
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## Example 2 (5 minutes)

As students work through Example 2, remind them that this question is addressed in an easier format in Grade 4, when students folded the triangle so that folded onto



#### Exercises 1–4 (20 minutes)





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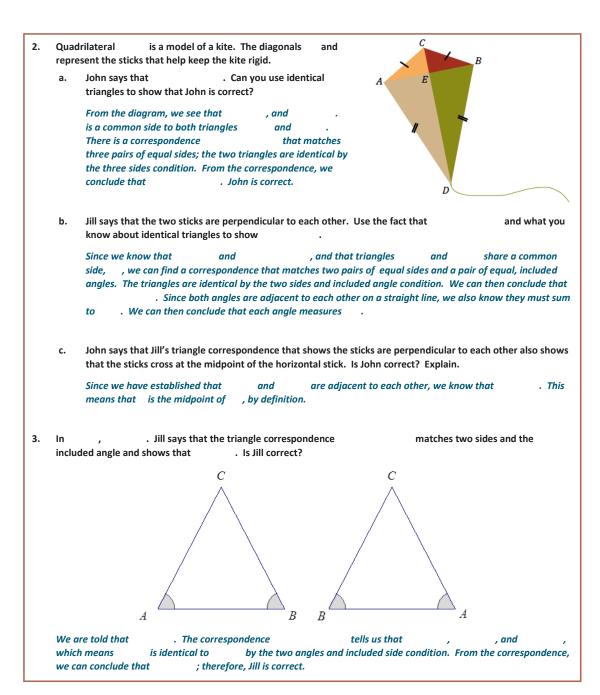
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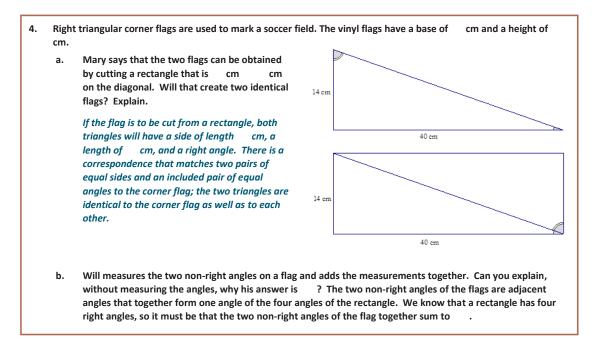
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### **Discussion (8 minutes)**

Consider a gallery walk as a means of reviewing responses to each exercise.

- Hold students accountable for providing evidence in their responses that logically progresses to a conclusion.
- Offer opportunities for students to share and compare their solution methods.

### Closing (2 minutes)

- In deciding whether two triangles are identical, examine the structure of the diagram of the two triangles to look for a relationship that might reveal information about corresponding parts of the triangles. This information may determine whether the parts of the triangle satisfy a particular condition, which might determine whether the triangles are identical.
- Be sure to identify and label all known measurements and then determine if any other measurements can be established based on knowledge of geometric relationships.

# Exit Ticket (5 minutes)



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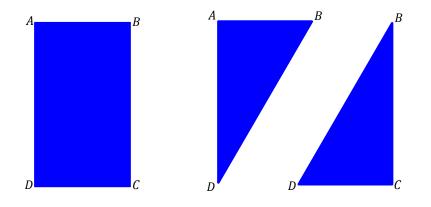
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#### **Exit Ticket**

Alice is cutting wrapping paper to size to fit a package. How should she cut the rectangular paper into two triangles to ensure that each piece of wrapping paper is the same? Use your knowledge of conditions that determine unique triangles to justify that the resulting pieces from the cut are the same.





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#### **Exit Ticket Sample Solutions**

Alice should cut along the diagonal of rectangle . Since is a rectangle, the opposite sides will be equal in length, or, and . A rectangle also has four right angles, which means a cut along the diagonal will result in each triangle with one angle. The correspondence matches two equal pairs of sides and an equal, included pair of angles; the triangles are identical by the two sides and included angle condition.

#### **Problem Set Sample Solutions**

1. Jack is asked to cut a cake into equal pieces. He first cuts it into equal fourths in the shape of rectangles, and then he cuts each rectangle along a diagonal. Did he cut the cake into equal pieces? Explain.

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 Image: Comparison of the cut the cake into equal pieces of the cut the cake into equal pieces.

 Yes, Jack cut the cake into equal pieces.
 Since the first series of cuts divided the cake into equal fourths in the shape of rectangles, we know that the opposite sides of the rectangles are equal in length; that means all triangles have two sides that are equal in length to each other. Each of the triangular pieces also has one right angle because we know that rectangles have four right angles.



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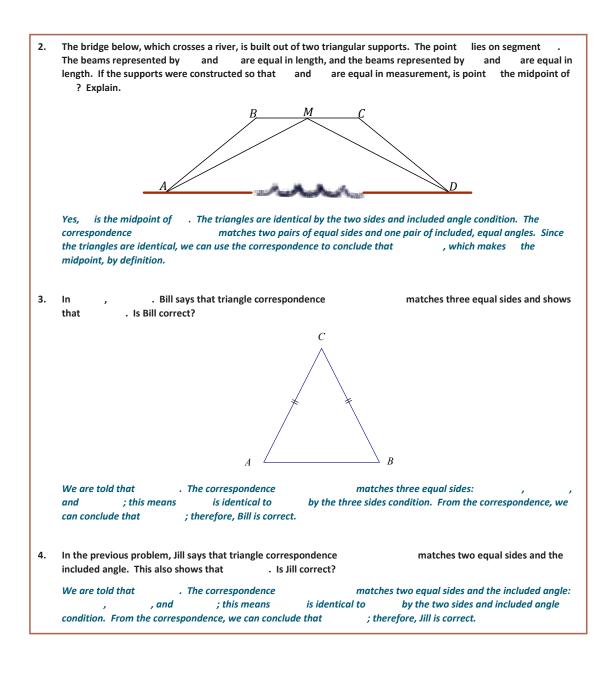
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