

Lesson 12: Unique Triangles—Two Sides and a Non-**Included Angle**

Student Outcomes

- Students understand that two sides of a triangle and an acute angle, not included between the two sides, may not determine a unique triangle.
- Students understand that two sides of a triangle and a angle (or obtuse angle), not included between the two sides, determine a unique triangle.

Lesson Notes

A triangle drawn under the condition of two sides and a non-included angle is often thought of as a condition that does not determine a unique triangle. Lesson 12 breaks this idea down by sub-condition. Students see that the subcondition, two sides and a non-included angle, provided the non-included angle is an acute angle, is the only subcondition that does not determine a unique triangle. Furthermore, there is a maximum of two possible non-identical triangles that can be drawn under this sub-condition.

Classwork

MP.

Exploratory Challenge (30 minutes)



Ask students to predict, record, and justify whether they think the provided criteria will determine a unique triangle for each set of criteria.



Lesson 12:

Unique Triangles—Two Sides and a Non-Included Angle 4/9/14





MP



As students arrive at part (e), recommend that they label the two points of intersection as and

	e.	Complete the drawing of .			
2.	f. Now a.	Did the results of your drawing differ from your prediction? Answers will vary. Attempt to draw this triangle: draw , provided cm, cm, and . How are these conditions different from those in Exercise 1, and do you think the criteria will determine a unique triangle? The provided angle was an acute angle in Exercise 1; now the provided angle is a right angle. Possible prediction: since the same general criteria (two sides and a non-included angle) determined more than one triangle in Exercise 1 the same can hannen in this situation.			
			E	Scaffolding	
				Eor Eversise 2 pr	ort (a) romind
			3 cm	students to draw parts first (i.e.,	the adjacent and .
			$ \overrightarrow{F}$		

COMMON CORE Date:

Lesson 12:

Unique Triangles—Two Sides and a Non-Included Angle 4/9/14





This work is licensed under a <u>Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.</u>





Lesson 12:

Unique Triangles—Two Sides and a Non-Included Angle 4/9/14



121



This work is licensed under a Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.



Discussion (8 minutes)

Review the results from each case of the two sides and non-included angle condition.

- Which of the three cases, or sub-conditions of two sides and a non-included angle, determines a unique triangle?
 - ^a Unique triangles are determined when the non-included angle in this condition is or greater.
- How should we describe the case of two sides and a non-included angle that does not determine a unique triangle?
 - The only case of the two sides and a non-included angle condition that does not determine a unique triangle is when the non-included angle is an acute angle.
- Highlight how the radius in the figure in Exercise 1, part (e) can be pictured to be "swinging" between and
 Remind students that the location of is initially unknown and that ray is extended to emphasize this.



Lesson 12: Date:

Unique Triangles—Two Sides and a Non-Included Angle 4/9/14



Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.



This work is licensed under a

Closing (2 minutes)

- A triangle drawn under the condition of two sides and a non-included angle, where the angle is acute, does not determine a unique triangle. This condition determines two non-identical triangles.
- Consider a triangle correspondence that corresponds to two pairs of equal sides and one pair of equal, non-included angles. If the triangles are not identical, then can be made to be identical to by swinging the appropriate side along the path of a circle with a radius length of that side.
- A triangle drawn under the condition of two sides and a non-included angle, where the angle is or greater, does determine a unique triangle.

Exit Ticket (5 minutes)



Unique Triangles—Two Sides and a Non-Included Angle 4/9/14





Name

Date _____

Lesson 12: Unique Triangles—Two Sides and a Non-Included Angle

Exit Ticket

So far, we have learned about four conditions that determine unique triangles: three sides, two sides and an included angle, two angles and an included side, and two angles and the side opposite a given angle.

a. In this lesson, we studied the criterion two sides and a non-included angle. Which case of this criterion determines a unique triangle?

b. Provided has length cm, has length cm, and the measurement of is , draw , and describe why these conditions do not determine a unique triangle.









Exit Ticket Sample Solutions



Problem Set Sample Solutions





Lesson 12:

Unique Triangles—Two Sides and a Non-Included Angle 4/9/14







	Condition	Determines a Unique Triangle?	
1	Two sides and a non-included angle.	yes	
2	Two sides and an acute, non-included angle.	maybe	
3	Two sides and a non-included angle.	yes	
4	Two sides and a non-included angle, where the side adjacent to the angle is shorter than the side opposite the angle.	yes	
5	Two sides and a non-included angle.	maybe	
6	Two sides and a non-included angle, where the side adjacent to the angle is longer than the side opposite the angle.	no	



Lesson 12: Date: Unique Triangles—Two Sides and a Non-Included Angle 4/9/14







4. Choose one condition from the chart in Problem 3 that does not determine a unique triangle, and explain why.

Possible response: Condition 6 does not determine a unique triangle because the condition of two sides and an acute non-included angle determines two possible triangles.

5. Choose one condition from the chart in Problem 3 that does determine a unique triangle, and explain why.

Possible response: Condition 1 determines a unique triangle because the condition of two sides and a non-included angle with a measurement of or more determines a unique triangle.



Unique Triangles—Two Sides and a Non-Included Angle 4/9/14



