

C Lesson 5: Identical Triangles

Student Outcomes

- Students use a triangle correspondence to recognize when two triangles match identically.
- Students use notation to denote a triangle correspondence and use the triangle correspondence to talk about corresponding angles and sides.
- Students are able to label equal angles and sides of triangles with multiple arcs or tic marks.

Lesson Notes

This lesson provides a basis for identifying two triangles as *identical*. To clearly define triangles as identical, students must understand what a triangle correspondence is and be able to manipulate the relevant notation and terminology. Once this is addressed, students have the means, specifically the language, to discuss what makes a triangle unique in Lesson 7 and forward. Exercise 5 in the Problem Set is designed as an exploratory challenge; it is not expected that students develop an exact answer at this level.

Classwork

Opening (2 minutes)

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When studying triangles, it is essential to be able to communicate about the parts of a triangle without any confusion. The following terms are used to identify particular angles or sides:		
•	between	
•	adjacent to	
•	opposite to	
•	the included [side/angle]	

Opening Exercises 1–7 (15 minutes)







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Students have already been exposed to a correspondence without knowing the formal use of the word. The correspondence between numerical coordinates and geometric points allows methods from algebra to be applied to geometry. The correspondence between a figure in a scale drawing and the corresponding figure in a scale drawing allows students to compute actual lengths and areas from the scale drawing. In Grade 8, students will learn that figures are congruent when there is a transformation that makes a correspondence between the two figures. The idea of a correspondence lays the foundation for the understanding of functions that will be discussed in Grade 9.

Discussion (5 minutes)

Review the remaining two correspondences that students filled out in both tables.

- Why do we bother setting up a correspondence?
 - A correspondence provides a systematic way to compare parts of two triangles. Without a correspondence, it would be difficult to discuss the parts of a triangle because we would have no way of referring to particular sides, angles, or vertices.



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- Assume the correspondence
 What can be concluded about the vertices?
 - Vertex corresponds to , corresponds to , and corresponds to .
- How is it possible for any two triangles to have a total of six correspondences?
 - The first vertex can be matched with any of three vertices. Then, the second vertex can be matched with any of the remaining two vertices.

 With a correspondence in place, comparisons can be made about corresponding sides and corresponding angles. The following are corresponding vertices, angles, and sides for the triangle correspondence . Complete the missing correspondences:

 Vertices:

 Angles:

 Sides:

Example 1 (5 minutes)

Example 1

Given the following triangle correspondences, use double arrows to show the correspondence between vertices, angles, and sides.

Triangle Correspondence	
Correspondence of Vertices	$\uparrow \uparrow \downarrow \uparrow$
Correspondence of Angles	$\begin{array}{c} \uparrow \\ \downarrow \\ \downarrow \\ \downarrow \end{array}$
Correspondence of Sides	$\uparrow \uparrow \uparrow$



Two triangles are identical if there is a triangle correspondence so that corresponding sides and angles of each triangle is equal in measurement. In Figure 2, there is a correspondence that will match up equal sides and equal angles, ; we can conclude that is identical to

. This is not to say that we cannot find a correspondence in Figure 2 so that unequal sides and unequal angles are matched up, but there certainly is one correspondence that will match up angles with equal measurements and sides of equal lengths, making the triangles identical.





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Discussion (5 minutes)

In Figure 2, is identical to

- Which side is equal in measurement to ? Justify your response.
 - because it is known that the triangle correspondence equal angles.
- Which angle is equal in measurement to ? Justify your response.
 - because it is known that the triangle correspondence equal angles.

matches equal sides and

matches equal sides and

In discussing identical triangles, it is useful to have a way to indicate those sides and angles that are equal. We mark sides with tick marks and angles with arcs if we want to draw attention to them. If two angles or two sides have the same number of marks, it means they are equal.



Example 2 (3 minutes)



Exercise 8 (3 minutes)

Exercise 8 8. Sketch two triangles that have a correspondence. Describe the correspondence in symbols or words. Have a partner check your work. Answers will vary. Encourage students to check for correct use of notation and correctly made correspondences.



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Vocabulary

Correspondence: A *correspondence* between two triangles is a pairing of each vertex of one triangle with one (and only one) vertex of the other triangle.

lf	,	Y, and	is a correspondence between two triangles (written) <i>,</i> then	matches
	, side	matches side	, and so on.		

Closing (2 minutes)

- Two triangles and their respective parts can be compared once a correspondence has been assigned to the two triangles. Once a correspondence is selected, corresponding sides and corresponding angles can also be determined.
- Corresponding vertices are notated by double arrows; triangle correspondences can also be notated with double arrows.
- Triangles are identical if there is a correspondence so that corresponding sides and angles are equal.
- An equal number of tick marks on two different sides indicates the sides are equal in measurement. An equal number of arcs on two different angles indicates the angles are equal in measurement.

Exit Ticket (5 minutes)



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Exit Ticket

- 1. The following triangles are identical and have the correspondence each of the following sides and angles.
- . Find the measurements for



2. Explain why correspondences are useful.



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Exit Ticket Sample Solutions



Problem Set Sample Solutions

Given the following triangle correspondences, use double arrows to show the correspondence between vertices, angles, and sides.

1.

Triangle Correspondence		
Correspondence of Vertices	$\begin{array}{c} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	
Correspondence of Angles	$\underset{\longleftrightarrow}{\underset{\longleftrightarrow}{\underset{\longleftrightarrow}{\underset{\longleftrightarrow}{\underset{\longleftrightarrow}{\underset{\longleftrightarrow}{\underset{\longleftrightarrow}{\underset{\longleftrightarrow}$	
Correspondence of Sides	$\begin{array}{c} \uparrow \\ \downarrow \\ \downarrow \\ \downarrow \end{array}$	









3.

Triangle Correspondence	
Correspondence of Vertices	$\begin{array}{c} \longleftrightarrow \\ \longleftrightarrow \\ \longleftrightarrow \\ \end{array}$
Correspondence of Angles	$\begin{array}{c} \longleftrightarrow \\ \longleftrightarrow \\ \leftrightarrow \end{array}$
Correspondence of Sides	$\begin{array}{c} \longleftrightarrow \\ \longleftrightarrow \\ \longleftrightarrow \end{array}$

Name the angle pairs and side pairs to find a triangle correspondence that matches sides of equal length and angles of equal angles measurements.

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Example 2 Scaffolding Supplement





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