Lesson 3: Solving for Unknown Angles Using Equations

Student Outcomes

Students solve for unknown angles in word problems and in diagrams involving all learned angle facts.

Classwork

Opening Exercise (5 minutes)



In the following examples and exercises, students set up and solve an equation for the unknown angle based on the relevant angle relationships in the diagram. Encourage students to note the appropriate angle fact abbreviation for any step that depends on an angle relationship.





Five rays meet at a common vertex. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of $\$.

.

The sum of angles at a point is

at a point



Example 2 (4 minutes)

Example 2					
Four rays meet at a common vertex. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of . Find the measurements of angles and .					
The sum of the degree measurements of , , , and the arc that measures is $B \setminus x^{\circ}$					
at a point D 204°					
The measurement of The measurement of					

Exercise 2 (4 minutes)

Exercise 2				
Four rays meet at a common vertex. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of . Find the measurement of .				
, ,	, and are ang	gles at a point and sum to	12x°	
		at a point	B A	
			60°	
_	—		2.0	
			C/ JX	
The measurement of			Ц	

Example 3 (4 minutes)





ny





Exercise 3 (4 minutes)

Exercise 3				
Two lines meet at the common vertex of two rays. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of . Find the measurements of angles and .				
which The measurement of formed by adjacent angles and is equal to the sum of the measurements of the adjacent angles. This is also true for measurement of , which is formed by adjacent angles and . is vertically opposite from and equal to . , add , add Vert A A A A A A A A A A A A A A A A A A A	<u> </u>			
The measurement of C				
The measurement of				

The following examples are designed to highlight Mathematical Practice 7 by helping students to see the connection between an angle diagram and the equation used to model it. Solving equations with variables on both sides is a topic Grade 8 teachers may choose to show that solution method if they so choose.

Example 4 (6 minutes)





Lesson 3:





Students use information in the figure and a protractor to solve for .

- i) Students will measure a angle as shown; the remaining portion of the angle must be (add).
- ii) Students can use their protractor to find the measurement of and use this measurement to partition the other angle in the vertical pair.

As a check, students should substitute the measured value into each expression and evaluate; each angle of the vertical pair should equal the other. Students can also use their protractor to measure each angle of the vertical angle pair.



With a modified figure, students can write an algebraic equation that they have the skills to solve:

vert

Measurement of each angle in the vertical pair:

MP.

Extension: The algebra steps above are particularly helpful as a stepping-stone in demonstrating how to solve the equation that takes care of the problem in one shot:

vert

Measurement of each angle in the vertical pair:

Students understand the first line of this solution because of their knowledge of vertical angles. In fact, the only line they are not familiar with is the second line of the solution, which is a skill that they learn in Grade 8. Showing students this solution is simply a preview.









Exercise 4 (4 minutes)

Exercise 4	
Set up and solve an equation to find the value of . Find the measurement of one of the vertical angles.	x+54° 4x°

Students use information in the figure and a protractor to solve for .

- i) Students will measure a angle as shown; the remaining portion of the angle must be (add).
- ii) Students can use their protractor to find the measurement of and use this measurement to partition the other angle in the vertical pair.

Students should perform a check as in Example 4 before solving an equation that matches the modified figure.



Exit Ticket (5 minutes)







Name _____

Date _____

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Exit Ticket

1. Two rays have a common vertex on a line. Set up and solve an equation to find the value of . Find the measurements of angles and .



2. Two lines meet at the common vertex of two rays. Set up and solve an equation to find the value of . Find the measurements of angles and





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Exit Ticket Sample Solutions





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Problem Set Sample Solutions

Set up and solve an equation for the unknown angle based on the relevant angle relationships in the diagram. Add labels to diagrams as needed to facilitate their solutions. List the appropriate angle fact abbreviation for any step that depends on an angle relationship.

1.	Two	lines meet at a point. Set up and solve an equation to find the value of .	1
		vert	
		72°	(x+15)°
2.	Thre how	e lines meet at a point. Set up and solve an equation to find the value of $\$. Is your answe you know.	er reasonable? Explain
	Let		
		vert	
		on a line	78°
	Since	· , ·	52°
	The angle	answers seem reasonable since they are similar in magnitude to the e.	a°
			1
3.	Two value	lines meet at the common vertex of two rays. Set up and solve an equation to find the es of and .	Scaffolding:
		on a line	Students struggling to organize
			their solution may benefit from
		on a line	prompts such as the following:
		32°	 Write an equation to
		a°	model this situation.
			describes the situation
		b	Solve and interpret the
			solution. Is it reasonable?
		N N	
	Scaff	folded solutions:	
	a.	Use equation above.	
	b.	The angle marked , the angle with measurement , and the right angle are angles measurements sum to .	on a line. Their
	с.	The answers seem reasonable because once the values of and are substituted, it ap angles (and) form a right angle. We know those two angles should form a right a angle adjacent to it is a right angle.	pears that the two ngle because the



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7.	Three secor	e angles are at a point. The second angle is more than the first, and the third angle is nd angle.	more than the	
	a.	Find the measurement of all three angles.		
		at a point		
		Angle 1:		
		Angle 2:		
		Angle 3:		
	b.	Compare the expressions you used for the three angles and their combined expression. I equal and how they reveal different information about this situation.	Explain how they are	
		By the commutative and associative laws, is equal to		
		, which is equal to . The first expression,	, shows the sum of	
		three unknown numbers, where the second is more than the first, and the third is in the second is the second	more than the	
		second. The expression shows the sum of three times an unknown number with	1.	
8.	Four	adjacent angles are on a line. The measurements of the four angles are four consecutive e	ven numbers.	
	Dete	mine the measurements of all four angles.	C (());	
		on a line	Scaffolding:	
	The f	our anale measures are: and	Teachers may ne	ed to review
	ine j	our angle measures are. , , , , and .	the term "consec	utive" for
			students to succe	essfully
9.	Three	angles are at a point. The ratio of the measurement of the second angle to the	complete Probler	n Set 7.
	meas	urement of the first angle is . The ratio of the measurement of the third angle to		
	the n	leasurement of the second angle is .		
	Let t of th	he smallest measure of the three angles be . Then the measure of the second angle is e third angle is .	, and the measure	
		at a point		
	Angl	e 1		
	Angl	e 2		
	Angl	e 3		
				•



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