# Lesson 9: Problem Solving When the Percent Changes

### **Student Outcomes**

- Students solve percent problems where quantities and percents change.
- Students use a variety of methods to solve problems where quantities and percents change, including double number lines, visual models, and equations.

### **Lesson Notes**

In this lesson, students solve multi-step word problems related to percents that change. They identify the quantities that represent the *part* and the *whole* and recognize when the whole changes based on the context of a word problem. They will build on their understanding of the relationship between the part, whole, and percent. All of the problems can be solved with a visual model. Students may solve some of the problems with an equation, but often the equation will require eighth grade methods for a variable on both sides of the equation. If students generalize and solve such equations, they should be given full credit.

### Classwork

### Example 1 (5 minutes)

MP.1 Begin class by displaying Example 1. Have the students work in groups or pairs to try to start the problem on their own.

- Based on the words in the example, which person's money should represent the whole?
  - The first whole is Sally's beginning money. The second whole is Sally's ending money.

#### Example 1 The amount of money Tom has is 75% of Sally's amount of money. After Sally spent \$120 and Tom saved all his money, Tom's amount of money is 50% more than Sally's. How much money did each have at the beginning? Use a visual model and a percent line to solve the problem. 0% **50**% 75% 100% 25% Before: Tom's Money Sally's Money 100% 150% 0% **50**% After: Tom's Money Sally's Money Each bar is \$60. Tom started with \$180, and Sally started with \$240.



- Students that had difficulty solving equations in earlier modules may need additional practice working with these onestep equations. Students should continue to use calculators where appropriate throughout the lesson.
- Where appropriate, provide visual models with equations to show an alternative problemsolving strategy for visual learners.



Lesson 9: Date: Problem Solving When the Percent Changes 11/19/14



131





### Example 2 (10 minutes)

Following the discussion of Example 1, have students try to start Example 2 without modeling. Students will solve the example using a visual model and an equation to show the change in percent. Pose possible discussion questions to the class as you solve the problem.

- Which person's candy represents the whole?
  - Erin's candy represents the whole.

xample 2	2					
rin and S asha had	asha went to a candy shop. $120\%$ more. How many ca	Sasha bough ndies did Erin	t 50% more and Sasha ha	candies than ve at first?	Erin. After E	rin bought 8 more candies,
a.	Model the situation using	g a visual mod	el.			
	0% Before: Erin's Candies Sasha's Candies		50%		100%	150%
	0% After:	20%	<b>40</b> %	<b>60</b> %	80%	<b>100</b> % <b>120</b> %
	0% After: Erin's Candies	20%	40%	60%	80%	100% 120%
	0% After: Erin's Candies Sasha's Candies	20%	40%	60%	80%	100% 120%

### Example 3 (7 minutes)

MP.4

The previous example presented a visual model approach. In this example, allow students to choose their preferred method to solve the problem. It is important for students to first write an algebraic expression that represents each person's money before they can form an equation.

Point out that since Kimberly and Mike have an equal amount of money in the beginning, the same variable can be used to represent the amount.

### Scaffolding:

- Consider having some groups solve the problem using a visual model and other groups using an equation.
- Have students explain their models to other groups and look for comparisons for problem solving.
- For the exercises, the teacher could select specific individuals to solve problems using an assigned method to allow students to get comfortable with choosing and utilizing problem-solving methods of choice and efficiency.



Lesson 9: Date: Problem Solving When the Percent Changes 11/19/14







### Example 3

Kimberly and Mike have an equal amount of money. After Kimberly spent \$50 and Mike spent \$25, Mike's money is50% more than Kimberly's. How much did Kimberly and Mike have at first?a.Use an equation to solve the problem.Equation Method:Let x be the amount of Kimberly's money, in dollars, after she spent \$50. After Mike spent \$25, his money is<br/>50% more than Kimberly's. Mike's money is also \$25 more than Kimberly's.0.5x = 25<br/>x = 50Kimberly started with \$100 because \$100 - \$50 = \$50. Mike has \$75 because (1.5)50 = 75.<br/>They each started with \$100.

Lead the class through constructing a visual model for part (b). Since we are subtracting money, first create the *after* picture, then, add the money to get the *before* picture.





Problem Solving When the Percent Changes 11/19/14



133





### **Exercise (13 minutes)**

This exercise allows students to choose any method they would like to solve the problem. Then, they must justify their answers by using a different method. After about 10 minutes, ask students to present their solutions to the class. Compare and contrast different methods, and emphasize how the algebraic, numeric, and visual models are related.



### **Closing (3 minutes)**

- What formula can we use to relate the part, whole, and percent?
  - Quantity = Percent × Whole
- Describe at least two strategies for solving a changing percent problem using an equation.
  - <sup>a</sup> You must identify the first whole and then identify what would represent the second whole.
  - You must use algebraic properties such as the distributive property to solve the problem.

Lesson Su	ummary
•	To solve a changing percent problem, identify the first whole and then the second whole. To relate the part, whole, and percent, use the formula
	$Quantity = Percent \times Whole.$
	Models, such as double number lines, can help visually show the change in quantities and percents.

### Exit Ticket (7 minutes)



Problem Solving When the Percent Changes 11/19/14





Name

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## Lesson 9: Problem Solving When the Percent Changes

### **Exit Ticket**

Terrence and Lee were selling magazines for a charity. In the first week, Terrance sold 30% more than Lee. In the second week, Terrance sold 8 magazines, but Lee did not sell any. If Terrance sold 50% more than Lee by the end of the second week, how many magazines did Lee sell?

Choose any model to solve the problem. Show your work to justify your answer.





135





### **Exit Ticket Sample Solutions**

Terrence and Lee were selling magazines for a charity. In the first week, Terrence sold 30% more than Lee. In the second week, Terrence sold 8 magazines, but Lee did not sell any. If Terrence sold 50% more than Lee by the end of the second week, how many magazines did Lee sell? Choose any model to solve the problem. Show your work to justify your answer. Answers may vary. **Equation Model:** Let m be the number of magazines Lee sold. 150% - 130% = 20%, so 0.2m = 8 and m = 40Visual Model: 0% 100% 130% First Week: Lee Terrence 0% 100% 130% 150% Second Week: Lee 8 Terrence By subtracting 150% and 130%, I determined that 8 magazines represents 20% of the magazines Lee sold in the first week. Then, I multiplied both the percent and the number of magazines by 5 to find that 40 magazines represents 100%of the magazines Lee sold.

### **Problem Set Sample Solutions**

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1. Solve each problem using an equation.

a. What is 150% of 625?

n = 1.5(625)

n = 937.5

b. 90 is 40% of what number?

90 = 0.4(n)

n = 225

c. What percent of 520 is 40? Round to the nearest hundredth of a percent.

40 = p(520)

p \approx 0.0769 = 7.69\%
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Problem Solving When the Percent Changes 11/19/14









Lesson 9: Date: Problem Solving When the Percent Changes 11/19/14

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137



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