

## **Student Outcomes**

- Students understand the terms original price, selling price, markup, markdown, markup rate, and markdown rate.
- Students identify the original price as the whole and use their knowledge of percent and proportional relationships to solve multi-step markup and markdown problems.
- Students understand equations for markup and markdown problems and use them to solve for unknown quantities in such scenarios.

## **Lesson Notes**

In this lesson, students use algebraic equations to solve multi-step word problems involving markups and markdowns. This lesson extends the mathematical practices and terminology students saw in Module 1, Lesson 14.

New finance terms such as retail price, consumer, cost price, and wholesale price are introduced. Although students are not required to memorize these terms, they do provide a solid foundational knowledge for financial literacy. To make the lesson more meaningful to students, use examples from an actual newspaper circular.

Students have had significant exposure to creating tables and graphs to determine proportional relationships in Module 3. Before the lesson, the teacher may need to review past student performance data to target students who might potentially struggle with discovering proportional relationships using percent problems in Exercise 4.

Definitions:

**MARKUP:** A *markup* is the amount of increase in a price.

MARKDOWN: A markdown is the amount of decrease in a price.

ORIGINAL PRICE: The original price is the starting price. It is sometimes called the cost or wholesale price.

SELLING PRICE: The selling price is the original price plus the markup or minus the markdown.

**MARKUP/MARKDOWN RATE:** The *markup rate* is the percent increase in the price, and the *markdown rate* (discount rate) is the percent decrease in the price.

- Most markup problems can be solved by the equation: Selling Price = (1 + m)(Whole), where *m* is the markup rate, and the whole is the original price.
- Most markdown problems can be solved by the equation: Selling Price = (1 m)(Whole), where *m* is the markdown rate, and the whole is the original price.



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## Classwork

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## **Opening (3 minutes)**

Pose the question to the class. Students, who have been placed in groups, discuss possible answers. Teacher asks a few students to share out.

- A brand of sneakers costs \$29.00 to manufacture in Omaha, Nebraska. The shoes are then shipped to shoe stores across the country. When you see them on the shelves, the price is \$69.99. How do you think the price you pay for the sneakers is determined? Use percent to describe the markup. Explain your reasoning.
  - The store makes up a new price so they can make money.
  - <sup>a</sup> The store has to buy the sneakers and pay for any transportation costs to get the sneakers to the store.
  - <sup>a</sup> The store marks up the price to earn a profit because they had to buy the shoes from the company.
  - Markup is the amount of increase in a price from the original price.

Close the discussion by explaining how the price of an item sold in a store is determined. For example, in order for the manufacturer to make a profit, the store has to pay for the cost to make the item. Then, a store purchases the item at a *cost price* from the manufacturer. The store then increases the price of the item by a percent called the *markup rate* before it is sold to the store's customers. Stores do this to earn a *profit*.

## Example 1 (5 minutes): A Video Game Markup

Students construct an algebraic equation based on a word problem. They express the markup rate of 40% on a video game that costs \$30.00 as 1.40(30) to show that a markup means a percent increase. Students identify the quantity that corresponds with 100% (the whole).

#### Example 1: A Video Game Markup

Games Galore Super Store buys the latest video game at a wholesale price of 330.00. The markup rate at Game's Galore Super Store is 40%. You use your allowance to purchase the game at the store. How much will you pay, not including tax?

a. Write an equation to find the price of the game at Games Galore Super Store. Explain your equation.

Let P represent the price of the video game.

 $\textbf{Quantity} = \textbf{Percent} \times \textbf{Whole}$ 

P = (100% + 40%)(30)

The equation shows that the price of the game at the store is equal to the wholesale cost, which is 100% and the 40% increase. This makes the new price 140% of the wholesale price.

b. Solve the equation from part (a).

P = (100% + 40%)(30)

P = (1.40)(30)

*P* = 42

I would pay  $\$42.00\ \text{if I}$  bought it from Games Galore Super Store.



- Use sentence strips to create a word wall for student reference throughout the lesson to avoid confusion over financial terms.
- Some words can be written on the same sentence strip to show they are synonyms, such as discount price and sales price and cost price and wholesale price.



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c.

What was the total markup of the video game? Explain.

The markup was \$12.00 because \$42 - \$30 = \$12.

d. You and a friend are discussing markup rate. He says that an easier way to find the total markup is by multiplying the wholesale price of 30.00 by 40%. Do you agree with him? Why or why not?

Yes, I agree with him because (0.40)(30) = 12. The markup rate is a percent of the wholesale price. Therefore, it makes sense to multiply them together because Quantity = Percent × Whole.

- Which quantity is the *whole* quantity in this problem?
  - The wholesale price is the whole quantity.
- How do 140% and 1.4 correspond in this situation?
  - The markup price of the video game is 140% times the wholesale price. 140% and 1.4 are equivalent forms of the same number. In order to find the markup price, convert the percent to a decimal or fraction, and multiply it by the whole.
- What does a *markup* mean?
  - A markup is the amount of increase in a price.

## Example 2 (7 minutes): Black Friday

Students discuss the busiest American shopping day of the year, Black Friday—the day after Thanksgiving. The teacher could share the history of Black Friday to engage students in the lesson by reading the article at

<u>http://www.marketplace.org/topics/life/commentary/history-black-friday</u>. Students make the connection that markdown is a percent decrease.

Students realize that the distributive property allows them to arrive at an answer in one step. They learn that in order to apply an additional discount, a new whole must be found first and, therefore, requires multiple steps to solve.

Does it matter in what order we take the discount? Why or why not?

Allow students time to conjecture in small groups or with elbow partners before problem solving. Monitor student conversations, providing clarification as needed.

- I think the order does matter because applying the first discount will lower the price. Then, you would multiply the second discount to the new lower price.
- <sup>a</sup> I do not think order matters because both discounts will be multiplied to the original price anyway, and multiplication is commutative. For example,  $2 \times 3 \times 4$  is the same as  $3 \times 4 \times 2$ .

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Scaffolding:

Lesson 7

- Provide newspaper circulars from Black Friday sales, or print one from the Internet to access prior knowledge of discounts for all learners.
- Choose an item from the circular in lieu of the one provided in Example 1.

Example 2: Black Friday A \$300 mountain bike is discounted by 30% and then discounted an additional 10% for shoppers who arrive before 5:00 a.m. a. Find the sales price of the bicycle. Find the price with the 30% discount: Let D represent the discount price of the bicycle with the 30% discount rate. Quantity = Percent × Whole D = (100% - 30%)(300) D = (0.70)(300) D = 210\$210 is the discount price of the bicycle with the 30% discount rate.

- Which quantity is the new whole?
  - The discounted price of 30% off, which is \$210.

Find the price with the additional 10% discount: Let A represent the discount price of the bicycle with the additional 10% discount. A = (100% - 10%)(210)= (1 - 0.10)(210)= (0.90)(210)= 189\$189 is the discount price of the bicycle with the additional 10% discount. b. In all, by how much has the bicycle been discounted in dollars? Explain. 300 - 189 = 111. The bicycle has been discounted 111 because the original price was 300. With both discounts applied, the new price is \$189. After both discounts were taken, what was the total percent discount? c. A final discount of 40% means that you would add 30%+10% and apply it to the same whole. This is not the case because the additional 10% discount is taken after the 30% discount has been applied, so you are only receiving that 10% discount on 70% of the original price. A 40% discount would make the final price 180 because 180 = (0.60)(300).However, the actual final discount as a percent is 37%. Let P be the percent the sales price is of the original price. Let F represent the actual final discount as a percent. **Part = Percent × Whole**  $189 = P \times 300$  $\left(\frac{1}{300}\right)189 = P \times 300 \left(\frac{1}{300}\right)$ 0.63 = 63% = PF = 100% - 63% = 37%

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Teacher could also show students that a 30% discount means to multiply by 0.70, and an extra 10% means to multiply by 0.90. (0.70)(0.90) = 0.63, so it is the same as 100% - 63% = 37% discount. This can help students perform the mathematics more efficiently.

> d. Instead of purchasing the bike for \$300, how much would you save if you bought it before 5:00 a.m.? You would save \$111 if you bought the bike before 5:00 a.m. because \$300 - \$189 is \$111.

## Exercises 1–3 (6 minutes)

Students complete the following exercises independently or in groups of two using Quantity = Percent  $\times$  Whole. Review the correct answers before moving to Example 3. The use of a calculator is recommended for these exercises.

Exercises 1–3			
1.	Sasha went shopping and decided to purchase a set of bracelets for 25% off of the regular price. If Sasha buys the bracelets today, she will save an additional 5%. Find the sales price of the set of bracelets with both discounts. How much money will Sasha save if she buys the bracelets today? Let B be the sales price with both discounts in dollars. B = (0.95)(0.75)(44) = 31.35. The sales price of the set of bracelets with both discounts is \$31.35. State will save \$12.65		
2.	<ol> <li>A golf store purchases a set of clubs at a wholesale price of \$250. Mr. Edmond learned that the clubs were marked up 200%. Is it possible to have a percent increase greater than 100%? What is the retail price of the clubs?</li> <li>Yes, it is possible. Let C represent the retail price of the clubs, in dollars.</li> </ol>		
	C = (100% + 200%)(250)		
	=(1+2)(250)		
	=(3)(250)		
	= /50		
	The retail price of the clubs is \$750.		
3.	. Is a percent increase of a set of golf clubs from \$250 to \$750 the same as a markup rate of 200%? Explain.		
	Yes, it is the same. In both cases, the percent increase and markup rate show by how much (in terms of percent) the $750$ $3$		
	new price is over the original price. The whole is \$250 and corresponds to $100\%$ . $\frac{700}{250} = \frac{5}{1} \times 100\% = 300\%$ .		
	\$750 is $300\%$ of \$250. $300\% - 100\% = 200\%$ . From Exercise 2, the markup is $200\%$ . So, percent increase is the same as markup.		

## Example 3 (5 minutes): Working Backward

Refer to an item in the newspaper circular displayed to the class. Students find the markdown rate (discount rate) given an original price (regular price) and a sales price (discount price). Students find the total or final price, including sales tax.



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#### Example 3: Working Backward

A car that normally sells for \$20,000 is on sale for \$16,000. The sales tax is 7.5%.

- What is the whole quantity in this problem?
  - The whole quantity is the original price of the car, \$20,000.

a. What percent of the original price of the car is the final price?

Quantity = Percent × Whole 16,000 = P(20,000) 16,000  $\left(\frac{1}{20,000}\right) = P(20,000) \left(\frac{1}{20,000}\right)$ 0.8 = P 0.8 =  $\frac{80}{100} = 80\%$ 

The final price is 80% of the original price.

b. Find the discount rate.

The discount rate is 20% because 100%-80%=20%.

c. By law, sales tax has to be applied to the discount price. However, would it be better for the consumer if the 7.5% sales tax was calculated before the 20% discount was applied? Why or why not?

	Apply Sales Tax First	Apply the Discount First			
	Apply the sales tax to the whole.	(100% + 7.5%)(16,000)			
	(100% + 7.5%)(20,000)	(1+0.075)(16,000)			
	(1+0.075)(20,000)	(1.075)(16,000)			
	(1.075)(20,000)	\$17,200 is the final price, including the discount			
	\$21,500 is the price of the car, including tax, before the discount.	and tax.			
	Apply the discount to the new whole.				
	(100%-20%)(21,500)				
	(1 - 0.2)(21,500) = 17,200				
	\$17,200 is the final price, including the discount and tax.				
	Because both final prices are the same, it does not matter which is applied first. This is because multiplication is commutative. The discount rate and sales tax rate are both being applied to the whole, \$20,000.				
d.	Write an equation applying the commutative property to support your answer to part (c).				
	20,000(1.075)(0.8) = 20,000(0.8)(1.075)				



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## Exercises 4–5 (9 minutes)

Students write a markup or markdown equation based on the context of the problem. They use algebraic equations in the form: Quantity =  $(1 + m) \cdot$  Whole for markups, or Quantity = (1 - m) · Whole for markdowns. Students will use their equations to make a table and graph in order to interpret the unit rate (7.RP.A.2). Students may use a calculator for calculations, but their equations and steps should be shown for these exercises.

#### Exercise 4

a. Write an equation to determine the selling price in dollars, p, on an item that is originally priced s dollars after a markup of 25%.

p = 1.25s or p = (0.25 + 1)s

b. Create and label a table showing five possible pairs of solutions to the equation.

Price of Item Before Markup, s (in dollars)	Price of Item After Markup, p (in dollars)
10	12.50
20	25.00
30	37.50
40	50.00
50	62.50

### Scaffolding:

- Have visual learners refer to an anchor poster of proportional relationships to access prior knowledge. The poster should include items such as the following:
  - Word sentence
  - Equation
  - Graph of equation
  - Table of possible pairs of solutions
  - Meaning of (1, r) and (0,0) in context

#### Create and label a graph of the equation. C.



Interpret the points (0, 0) and (1, r). d.

> The point (0,0) means that a \$0 (free) item will cost \$0 because the 25% markup is also \$0. The point (1,r)is (1, 1, 25). It means that a \$1.00 item will cost \$1.25 after it is marked up by 25%; r is the unit rate.

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#### Exercise 5

Use the following table to calculate the markup or markdown rate. Show your work. Is the relationship between the original price and selling price proportional or not? Explain.

Original Price, m	Selling Price, p
(in dollars)	(in dollars)
\$1,750	\$1,400
\$1, 500	\$1,200
\$1,250	\$1,000
\$1,000	\$800
\$750	\$600

Because the selling price is less than the original price, use the equation: Selling Price =  $(1 - m) \times$  Whole.

1,400 = (1 - m)(1,750) $\frac{1,400}{1,750} = (1-m)\frac{1,750}{1,750}$ 0.80 = 1 - m0.20 = m

The markdown rate is 20%. The relationship between the original price and selling price is proportional because the table shows the ratio  $\frac{p}{m} = \frac{0.80}{1}$  for all possible pairs of solutions.

## Closing (3 minutes)

- How do you find the markup and markdown of an item?
  - To find the markup of an item, you multiply the whole by (1 + m), where m is the markup rate.
  - To find the markdown of an item, you multiply the whole by (1 - m), where m is the markdown rate.
- Discuss two ways to apply two discount rates to the price of an item when one discount follows the other.
  - In order to apply two discounts, you must first multiply the original price (whole) by 1 minus the first discount rate to get the discount price (new whole). Then, you must multiply by 1 minus the second discount rate to the new whole to get the final price. For example, to find the final price of an item discounted by 25% and then discounted by another 10%, you would first have to multiply by 75% to get a new whole. Then, you multiply the new whole by 90% to find the final price.
  - Another way to apply two discounts would be to subtract each discount from 1 and then find the product of these numbers and the original price. If we look at the same example as above, we would multiply (0.75)(0.9)(Whole).

Lesson	Summary
•	To find the markup or markdown of an item, multiply the whole by $(1\pm m)$ , where $m$ is the markup/markdown rate.
•	To apply multiple discount rates to the price of an item, you must find the first discount price and then use this answer to get the second discount price.

## Exit Ticket (7 minutes)



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# Lesson 7: Markup and Markdown Problems

## **Exit Ticket**

A store that sells skis buys them from a manufacturer at a wholesale price of 57. The store's markup rate is 50%.

a. What price does the store charge its customers for the skis?

b. What percent of the original price is the final price? Show your work.

c. What is the percent increase from the original price to the final price?







## **Exit Ticket Sample Solutions**

A store that sells skis buys them from a manufacturer at a wholesale price of \$57. The store's markup rate is 50%. a. What price does the store charge its customers for the skis?  $57 \times (1 + 0.50) = 85.50$ . The store charges \$85.50 for the skis. b. What percent of the original price is the final price? Show your work. Quantity = Percent × Whole Let P represent the unknown percent. 85.50 = P(57)  $85.50 \left(\frac{1}{57}\right) = P(57) \left(\frac{1}{57}\right)$  1.50 = P  $1.50 = \frac{150}{100} = 150\%$ . The final price is 150% of the original price. c. What is the percent increase from the original price to the final price? The percent increase is 50% because 150% - 100% = 50%.

## **Problem Set Sample Solutions**

In the following problems, students solve markup problems by multiplying the whole by (1 + m), where m is the markup rate, and work backward to find the whole by dividing the markup price by (1 + m). They also solve markdown problems by multiplying the whole by (1 - m), where m is the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdown rate, and work backward to find the whole by dividing the markdow





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3. The cost of a New York Yankee baseball cap is \$24.00. The local sporting goods store sells it for \$30.00. Find the markup rate.

Let P represent the unknown percent.

$$30 = P(24)$$
  
 $P = \frac{30}{24} = 1.25 = (100\% + 25\%)$ . The markup rate is 25%.

4. Write an equation to determine the selling price in dollars, p, on an item that is originally priced s dollars after a markdown of 15%.

p = 0.85s or p = (1 - 0.15)s

a. Create and label a table showing five possible pairs of solutions to the equation.

Price of Item Before Markdown, s (in dollars)	Price of Item After Markdown, p (in dollars)
10	8.50
20	17.00
30	25.50
40	34.00
50	42.50

b. Create and label a graph of the equation.



c. Interpret the points (0, 0) and (1, r).

The point (0,0) means that a \$0 (free) item will cost \$0 because the 15% markdown is also \$0. The point (1,r) is (1,0.85), which represents the unit rate. It means that a \$1.00 item will cost \$0.85 after it is marked down by 15%.

5. At the amusement park, Laura paid \$6.00 for a small cotton candy. Her older brother works at the park, and he told her they mark up the cotton candy by 300%. Laura does not think that is mathematically possible. Is it possible, and if so, what is the price of the cotton candy before the markup?

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Yes, it is possible. \frac{6.00}{1+3} = \frac{6}{4} = 1.50. The price of the cotton candy before the markup is $1.50.
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