

## Lesson 3: Writing Products as Sums and Sums as Products

### Classwork

#### Opening Exercise

Solve the problem using a tape diagram. A sum of money was shared between George and Brian in a ratio of 3: 4. If the sum of money was \$56.00, how much did George get?

#### Example 1

Represent  $3 + 2$  using a tape diagram.

Represent  $x + 2$  using a tape diagram.

Draw a rectangular array for  $3(3 + 2)$ .

Draw an array for  $3(x + 2)$ .

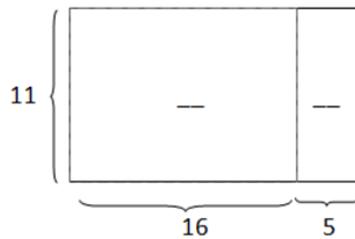
### Key Terms

**Distributive Property:** The distributive property can be written as the identity

$$a(b + c) = ab + ac \text{ for all numbers } a, b, \text{ and } c.$$

### Exercise 1

Determine the area of each region using the distributive property.



**Example 2**

Draw a tape diagram to represent each expression.

a.  $(x + y) + (x + y) + (x + y)$

b.  $(x + x + x) + (y + y + y)$

c.  $3x + 3y$

d.  $3(x + y)$

**Example 3**

Find an equivalent expression by modeling with a rectangular array and applying the distributive property to the expression  $5(8x + 3)$ .

**Exercise 2**

For parts (a) and (b), draw an array for each expression and apply the distributive property to expand each expression. Substitute the given numerical values to demonstrate equivalency.

a.  $2(x + 1)$ ,  $x = 5$

b.  $10(2c + 5)$ ,  $c = 1$

For parts (c) and (d), apply the distributive property. Substitute the given numerical values to demonstrate equivalency.

c.  $3(4f - 1), f = 2$

d.  $9(-3r - 11), r = 10$

#### Example 4

Rewrite the expression  $(6x + 15) \div 3$  in standard form using the distributive property.

#### Exercise 3

Rewrite the expressions as a sum.

a.  $(2b + 12) \div 2$

b.  $(20r - 8) \div 4$

c.  $(49g - 7) \div 7$

**Example 5**

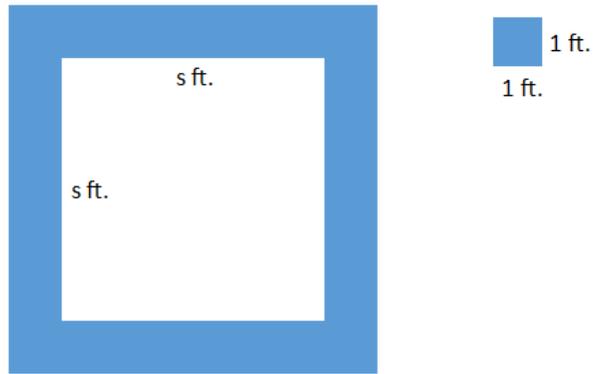
Expand the expression  $4(x + y + z)$ .

**Exercise 4**

Expand the expression from a product to a sum by removing grouping symbols using an area model and the repeated use of distributive property:  $3(x + 2y + 5z)$ .

**Example 6**

A square fountain area with side length  $s$  ft. is bordered by a single row of square tiles as shown. Express the total number of tiles needed in terms of  $s$  three different ways.



## Problem Set

1. a. Write two equivalent expressions that represent the rectangular array below.



- b. Verify informally that the two equations are equivalent using substitution.
2. You and your friend made up a basketball shooting game. Every shot made from the free throw line is worth 3 points, and every shot made from the half-court mark is worth 6 points. Write an equation that represents the total amount of points,  $P$ , if  $f$  represents the number of shots made from the free throw line, and  $h$  represents the number of shots made from half-court. Explain the equation in words.
3. Use a rectangular array to write the products in standard form.
- a.  $2(x + 10)$   
b.  $3(4b + 12c + 11)$
4. Use the distributive property to write the products in standard form.
- a.  $3(2x - 1)$                       g.  $(40s + 100t) \div 10$   
b.  $10(b + 4c)$                       h.  $(48p + 24) \div 6$   
c.  $9(g - 5h)$                       i.  $(2b + 12) \div 2$   
d.  $7(4n - 5m - 2)$                       j.  $(20r - 8) \div 4$   
e.  $a(b + c + 1)$                       k.  $(49g - 7) \div 7$   
f.  $(8j - 3l + 9)6$                       l.  $(14g + 22h) \div \frac{1}{2}$
5. Write the expression in standard form by expanding and collecting like terms.
- a.  $4(8m - 7n) + 6(3n - 4m)$   
b.  $9(r - s) + 5(2r - 2s)$   
c.  $12(1 - 3g) + 8(g + f)$