

Lesson 23: Solving Equations Using Algebra

Student Outcomes

- Students use algebra to solve equations (of the form px + q = r and p(x + q) = r, where p, q, and r are specific rational numbers); using techniques of making zero (adding the additive inverse) and making one (multiplying by the multiplicative inverse) to solve for the variable.
- Students identify and compare the sequence of operations used to find the solution to an equation algebraically, with the sequence of operations used to solve the equation with tape diagrams. They recognize the steps as being the same.
- Students solve equations for the value of the variable using inverse operations; by making zero (adding the
 additive inverse) and making one (multiplying by the multiplicative inverse).

Classwork



As in Lesson 22, students continue solving equations using properties of equality and inverse operations to relate their steps to the steps taken when solving problems algebraically. In this lesson, students decontextualize word problems to create equations that model given situations. Students justify their solutions by comparing their algebraic steps to the steps taken when using a tape diagram. Have the students work in cooperative groups and share out their solutions on chart paper. Use the class discussion as a way to have students view the differences in problem-solving approaches.

Exercises (35 minutes)

Exe	rcises		
1.	Youth Group Trip The youth group is going on a trip to an amusement park in another part of the state. The trip costs each group member \$150, which includes \$85 for the hotel and two one-day combination entrance and meal plan passes.		
	a.	Write an equation representing the cost of the trip. Let P be the cost of the park pass. 85 + 2P = 150	<i>Scaffolding:</i> Provide a review card showing examples of fraction multiplication and division for students who do
			not have adequate prerequisite skills.



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Closing (5 minutes)

- How do we translate a word problem into an equation? For instance, in Exercise 1 about the youth group trip, what key words and statements helped you determine the operations and values used in the equation?
 - Answers will vary, but students should talk about key words to determine the total value, the constant value, and the coefficient.
- How do we make sense of a word problem and model it with an equation?
 - Answers will vary and may be similar to the previous question.



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Lesson Summary

Equations are useful to model and solve real-world problems. The steps taken to solve an algebraic equation are the same steps used in an arithmetic solution.

Exit Ticket (5 minutes)



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Exit Ticket

Andrew's math teacher entered the seventh-grade students in a math competition. There was an enrollment fee of \$30 and also an \$11 charge for each packet of 10 tests. The total cost was \$151. How many tests were purchased?

Set up an equation to model this situation, solve it using if-then statements, and justify the reasons for each step in your solution.





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Exit Ticket Sample Solutions

And rew's math teacher entered the seventh-grade students in a math competition. There was an enrollment fee of 30 and also an 11 charge for each packet of 10 tests. The total cost was 151. How many tests were purchased?

Set up an equation to model this situation, solve it using if-then statements, and justify the reasons for each step in your solution.

Let p = the number of test packets. Enrollment fee + cost of test = 151 If: 30 + 11p = 151Then: 30 - 30 + 11p = 151 - 30 Subtraction property of equality for the additive inverse of 30 If: 0 + 11p = 121Then: 11p = 121Additive identity If: 11p = 121Then: $\frac{1}{11}(11p) = \frac{1}{11}(121)$ Multiplication property of equality using the multiplicative inverse of 11 If: 1p = 11Then: p = 11Multiplicative identity Andrew's math teacher bought 11 packets of tests. There were 10 tests in each packet, and $10 \times 11 = 110$. So, there were 110 tests purchased.

Problem Set Sample Solutions

For Exercises 1–4, solve each equation algebraically using if-then statements to justify your steps.1.
$$\frac{2}{3}x - 4 = 20$$
If: $\frac{2}{3}x - 4 = 20$ *Then*: $\frac{2}{3}x - 4 = 20 + 4$ Addition property of equality using the additive inverse of -4 *If*: $\frac{2}{3}x + 0 = 24$ *Then*: $\frac{2}{3}x = 24$ *Additive identityIf*: $\frac{2}{3}x = 24$ *Then*: $(\frac{3}{2})\frac{2}{3}x = (\frac{3}{2})24$ *Multiplication property of equality using the multiplicative inverse of* $\frac{2}{3}$ *If*: $1x = 36$ *Then*: $x = 36$ *Multiplicative identity*



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2.	$4 = \frac{-1+x}{2}$	
	<i>If:</i> $4 = \frac{-1+x}{2}$	
	<i>Then:</i> 2 (4) = 2 $\left(\frac{-1+x}{2}\right)$	Multiplication property of equality using the multiplicative inverse of $rac{1}{2}$
	<i>lf:</i> $8 = 1(-1+x)$	
	<i>Then:</i> $8 = -1 + x$	Multiplicative identity
	<i>If:</i> $8 = -1 + x$	
	<i>Then:</i> $8 - (-1) = -1 - (-1) + x$	Subtraction property of equality for the additive inverse of -1
	<i>If:</i> $9 = 0 + x$	
	<i>Then:</i> $9 = x$	Additive identity
3.	12(x+9) = -108	
	lf: 12(x+9) = -108	
	Then: $\left(\frac{1}{12}\right) 12(x+9) = \left(\frac{1}{12}\right)(-108)$	Multiplication property of equality using the multiplicative inverse of 12
	<i>lf:</i> $1(x+9) = -9$	
	<i>Then:</i> $x + 9 = -9$	Multiplicative identity
	<i>lf:</i> $x + 9 = -9$	
	<i>Then:</i> $x + 9 - 9 = -9 - 9$	Subtraction property of equality for the additive inverse of 9
	<i>lf:</i> $x + 0 = -18$	
	<i>Then:</i> $x = -18$	Additive identity
4.	5x + 14 = -7	
	lf: 5x + 14 = -7	
	Then: $5x + 14 - 14 = -7 - 14$	Subtraction property of equality for the additive inverse of 14
	<i>lf:</i> $5x + 0 = -21$	
	<i>Then:</i> $5x = -21$	Additive identity
	<i>lf:</i> $5x = -21$	
	<i>Then:</i> $\left(\frac{1}{5}\right) 5x = \left(\frac{1}{5}\right) (-21)$	Multiplication property of equality using the multiplicative inverse of 5
	<i>lf</i> : $1x = -4.2$	
	<i>Then:</i> $x = -4.2$	Multiplicative identity



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For Exercises 5–7, write an equation to represent each word problem. Solve the equation showing the steps and then state the value of the variable in the context of the situation. 5. A plumber has a very long piece of pipe that is used to run city water parallel to a major roadway. The pipe is cut into two sections. One section of pipe is 12 ft. shorter than the other. If $\frac{3}{4}$ of the length of the shorter pipe is 120 ft., how long is the longer piece of the pipe? Let x = the longer piece of pipe *lf*: $\frac{3}{4}(x-12) = 120$ Then: $\frac{4}{3}\left(\frac{3}{4}\right)(x-12) = \left(\frac{4}{3}\right)120$ Multiplication property of equality using the multiplicative inverse of $\frac{3}{4}$ *lf*: 1(x - 12) = 160*Then:* x - 12 = 160Multiplicative identity *lf*: x - 12 = 160Then: x - 12 + 12 = 160 + 12Addition property of equality for the additive inverse of -12*If:* x + 0 = 172*Then:* x = 172Additive identity The longer piece of pipe is 172 ft. Bob's monthly phone bill is made up of a \$10 fee plus \$0.05 per minute. Bob's phone bill for July was \$22. Write an equation to model the situation using m to represent the number of minutes. Solve the equation to determine the number of phone minutes Bob used in July. Let m = the number of phone minutes Bob used *lf*: 10 + 0.05 m = 22Then: 10 - 10 + 0.05 m = 22 - 10 Subtraction property of equality for the additive inverse of 10 *lf*: 0 + 0.05 m = 12Then: 0.05 m = 12Additive identity *lf:* 0.05 m = 12*Then:* $\left(\frac{1}{0.05}\right) 0.05 \ m = \left(\frac{1}{0.05}\right) 12$ Multiplication property of equality using the multiplicative inverse of 0.05

Multiplicative identity



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lf: 1m = 240*Then:* m = 240

Bob used 240 phone minutes in July.



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7. Kym switched cell phone plans. She signed up for a new plan that will save her \$3.50 per month compared to her old cell phone plan. The cost of the new phone plan for an entire year is \$294. How much did Kym pay per month under her old phone plan? Let n = the amount Kym paid per month for her old cell phone plan *lf*: 294 = 12(n - 3.50)*Then:* $\left(\frac{1}{12}\right)(294) = \left(\frac{1}{12}\right)12(n-3.50)$ Multiplication property of equality using the multiplicative inverse of 12 *lf*: 24.5 = 1 (n - 3.50)*Then:* 24.5 = n - 3.50Multiplicative identity 24.5 = n - 3.50If: Then: 24.5 + 3.50 = n - 3.50 + 3.50Addition property of equality for the additive inverse of -3.50If: 28 = n + 0*Then:* 28 = nadditive identity Kym paid \$28 per month for her old cell phone plan.



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