

Lesson 10: Understanding Multiplication of Integers

Student Outcomes

- Students practice and justify their understanding of multiplication of integers by using the Integer Game. For example, 3 × 5 corresponds to what happens to your score if you get three 5 cards; 3 × (-5) corresponds to what happens to your score if you get three -5 cards; (-3) × 5 corresponds to what happens to your score if you lose three 5 cards; and (-3) × (-5) corresponds to what happens to your score if you lose three -5 cards.
- Students explain that multiplying by a positive integer is repeated addition and that adding a number multiple times has the same effect as removing the opposite value the same number of times (e.g., 5 × 3 = (-5) × (-3) and 5 × (-3) = (-5) × 3).
- Students use the properties and facts of operations to extend multiplication of whole numbers to multiplication of integers.

Classwork

Exercise 1 (4 minutes)

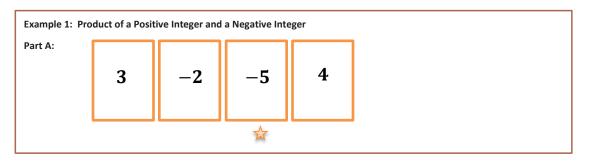
In groups of four, students play one round of the Integer Game using the Integer Game Outline as a reference if needed.

Exercise 1: Integer Game Revisited

In groups of four, play one round of the Integer Game (see Integer Game outline for directions).

Example 1 (16 minutes): Product of a Positive Integer and a Negative Integer

Part A: Instruct students to record the values of their cards on the images in Part A. One of the four card images has a \star beneath it. The \star is used to indicate which of the four cards to copy (or multiply) in Part B.



Part B: Instruct students to copy the value of the card with the \star beneath it from Part A on each card with a \star beneath it in Part B. The three remaining card values from Part A are entered in the three remaining card images in Part B. Students now have a total of six integer cards.

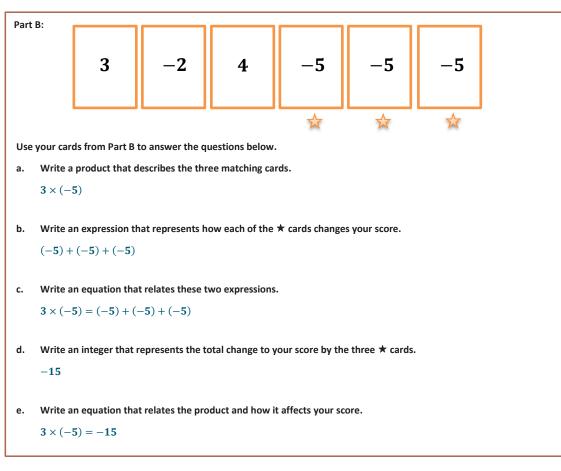


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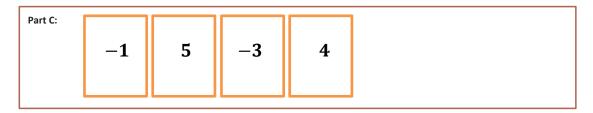
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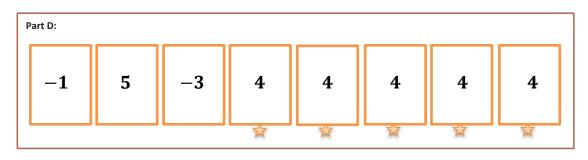




Part C: Instruct students to record the values of their cards on the images in Part C. The teacher chooses one of the four values and instructs the class to place a * beneath it to indicate which card will be cloned (multiplied) in Part D.



Part D: Instruct students to record the value of the card with the \star beneath it from Part C on each image with a \star beneath it in Part D. Also, rewrite the values of the three remaining cards on the other three images. Students now have a total of eight integer cards.

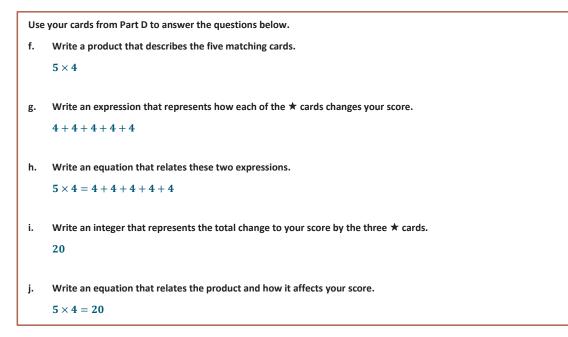




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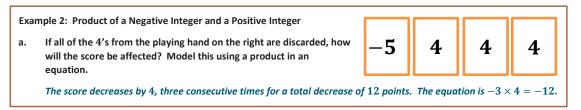
Students write conclusions using their own words in the student materials.

k. Use the expression 5 × 4 to relate the multiplication of a positive valued card to addition. *Multiplying a positive integer card is repeated addition of the positive integer card and increases your score*. 5 × 4 = 4 + 4 + 4 + 4 + 4 = 20
I. Use the expression 3 × (-5) to relate the multiplication of a negative valued card to addition. *Multiplying a negative integer card is repeated addition of the negative integer card and decreases your score*. 3 × (-5) = (-5) + (-5) + (-5) = -15

Example 2 (5 minutes): Product of a Negative Integer and a Positive Integer

• If $3 \times (a)$ represents putting three cards with the value *a* into your playing hand, what would $(-3) \times (a)$ represent?

The student materials provide the sample playing hand from the Integer Game shown below.

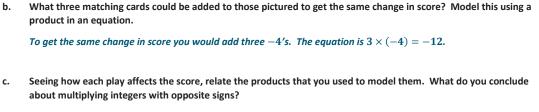




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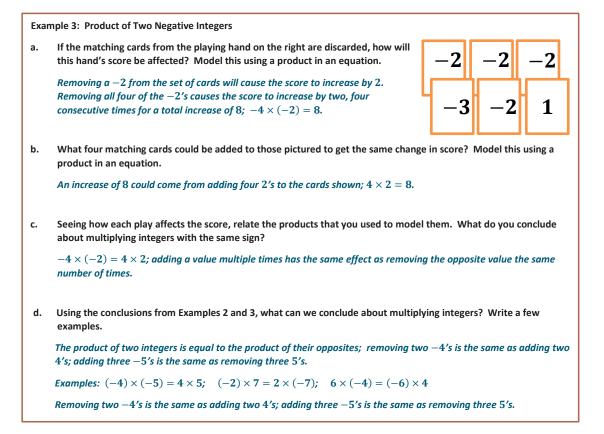


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(-3) \times 4 = 3 \times (-4); adding a value multiple times has the same effect as removing the opposite value the same number of times.
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Example 3 (5 minutes): Product of Two Negative Integers

Using the meaning of $(-3) \times (a)$ from Example 2, what does $(-3) \times (a)$ represent if the value of a is negative?

The student materials provide the sample playing hand from the Integer Game shown below.





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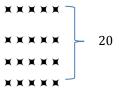




Closing (5 minutes)

This closing question extends prior knowledge about multiplication of whole numbers as a collection of equal-sized groups onto the family of integers.

• After examining the effects of multiple cards of equal value on scores in the Integer Game, how can we use the representation of 4×5 below to help explain what $4 \times (-5)$ means?



If one row of stars has a value of (-5), then four rows must have a total of -20.

Lesson Summary

Multiplying integers is repeated addition and can be modeled with the Integer Game. If $3 \times a$ corresponds to what happens to your score if you get three cards of value a, then $(-3) \times a$ corresponds to what happens to your score if you lose three cards of value a. Adding a number multiple times has the same effect as removing the opposite value the same number of times (e.g., $a \times b = (-a) \times (-b)$ and $a \times (-b) = (-a) \times b$.)

Exit Ticket (10 minutes)







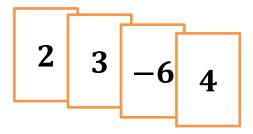
Name

Date

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Exit Ticket

1. Natalie is playing the Integer Game and only shows you the four cards shown below. She tells you that the rest of her cards have the same values on them and match one of these four cards.



a. If all of the matching cards will increase her score by 18, what are the matching cards?

b. If all of the matching cards will decrease her score by 12, what are the matching cards?

 A hand of six integer cards has one matching set of two or more cards. If the matching set of cards is removed from the hand, the score of the hand will increase by six. What are the possible values of these matching cards? Explain. Write an equation using multiplication showing how the matching cards yield an increase in score of six.

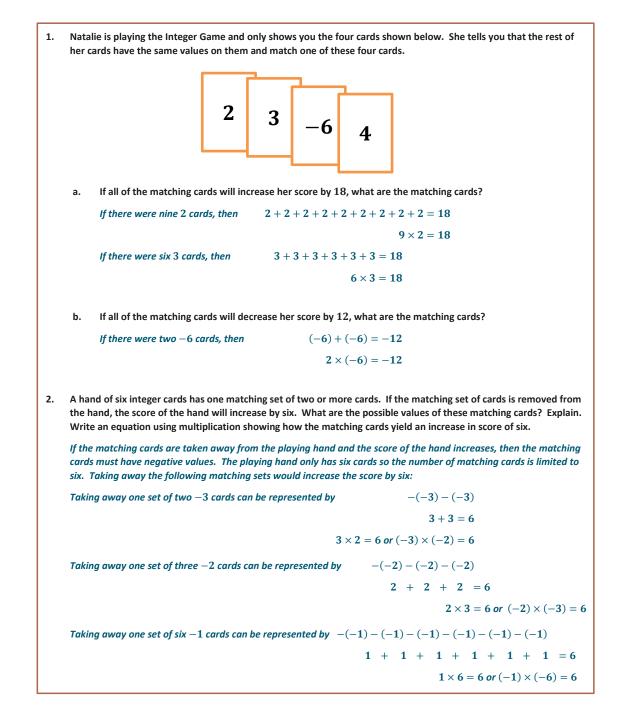


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Exit Ticket Sample Solutions





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Problem Set Sample Solutions

1. Describe sets of two or more matching integer cards that satisfy the criteria in each part below: Cards increase the score by eight points. a. Picking up: eight 1's, four 2's, or two 4's OR Removing: eight -1's, four -2's, or two -4's b. Cards decrease the score by 9 points. Picking up: nine -1's or three -3's OR Removing: nine 1's or three 3's c. Removing cards that increase the score by 10 points. Ten -1's, five -2's or two -5's Positive cards that decrease the score by 18 points. d. Removing eighteen 1's, nine 2's, six 3's, three 6's, or two 9's. 2. You have the integer cards shown at the right when your teacher tells you to choose a card to multiply four times. If your goal is to get your score as close to zero as possible, which card would you choose? Explain 5 -3 how your choice changes your score. -4 3 The best choice to multiply is the -3. The cards currently have a score of one. The new score with the -3 multiplied by 4, is -8. The scores where the other cards are multiplied by 4 are 10, -11, and 16; all further from zero. 3. Sherry is playing the Integer Game and is given a chance to discard a set of matching cards. Sherry determines that if she discards one set of cards her score will increase by 12. If she discards another set, then her score will decrease by eight. If her matching cards make up all six cards in her hand, what cards are in Sherry's hand? Are there any other possibilities? There are two possibilities: 2, 2, 2, 2, -6, -6 OR -3, -3, -3, -3, 4, 4



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