

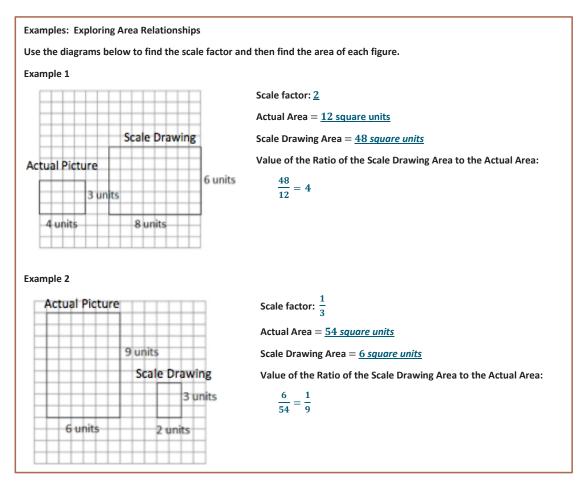
Student Outcomes

- Students identify the scale factor.
- Given a scale drawing, students compute the area in the actual picture.

Classwork

Examples (13 minutes): Exploring Area Relationships

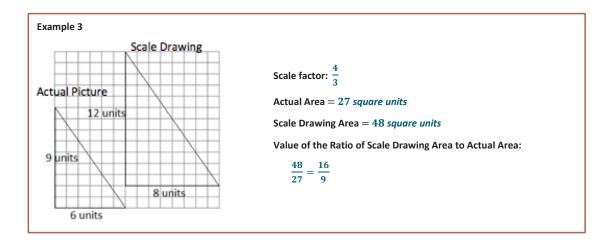
In this series of examples, students will identify the scale factor. Students can find the areas of the two figures and calculate the ratio of the areas. As students complete a few more examples, they can be guided to the understanding that the ratio of areas is the square of the scale factor.



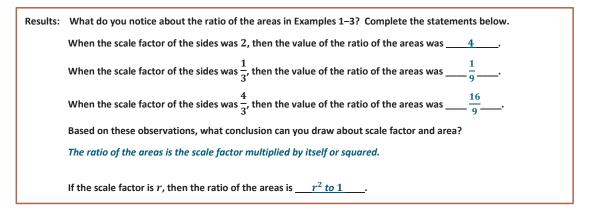


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Guide students through completing the results statements on the student materials.



- Why do you think this is? Why do you think it is squared (opposed to cubed or something else)?
 - When you are comparing areas, you are dealing with two dimensions instead of comparing one linear measurement to another.
- How might you use this information in working with scale drawings?
 - In working with scale drawings, you could take the scale factor, r, and calculate r² to determine the relationship between the area of the scale drawing and the area of the actual picture. Given a blueprint for a room, the scale drawing dimensions could be used to find the scale drawing area and could then be applied to determine the actual area. The actual dimensions would not be needed.
- Suppose a rectangle has an area of 12 square meters. If the rectangle is enlarged by a scale factor of three, what is the area of the enlarged rectangle based on Examples 1–3? Look and think carefully!
 - If the scale factor is 3, then the ratio of scale drawing area to actual area is 3^2 to 1^2 or 9 to 1. So, if its area is 12 square meters before it is enlarged to scale, then the enlarged rectangle will have an area of $12 \cdot \left(\frac{9}{1}\right)$, or $12 \cdot 9$, resulting in an area of 108 square meters.



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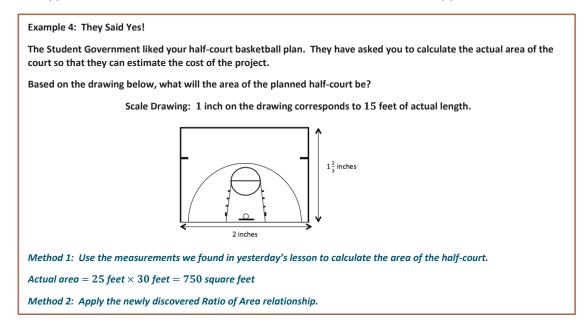






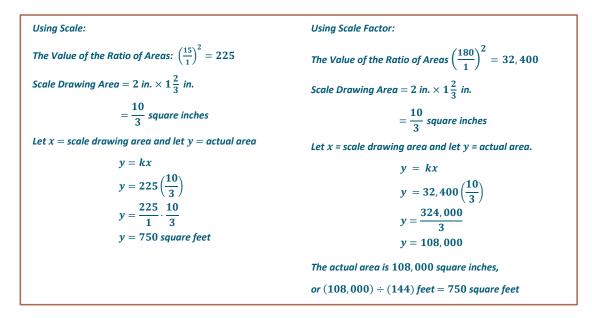
Complete Example 4 as a class, asking the guiding questions below. Have students use the space in their student materials to record calculations and work.

Give students time to answer the question, possibly choosing to apply what was discovered in Examples 1–3. Allow for discussion of approaches described below and for students to decide what method they prefer.



MP.2

Note to teachers: This can be applied to the given scale with no unit conversions (shown on left) or to the scale factor (shown on right). Both options are included here as possible student work and would provide for a rich discussion of why they both work and what method is preferred. See guiding questions below.



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Ask students to share how they found their answer. Use guiding questions to find all three options as noted above.

- What method do you prefer?
- Is there a time you would choose one method over the other?
 - If we don't already know the actual dimensions, it might be faster to use Method 1 (ratio of areas). If we are re-carpeting a room based upon a scale drawing, we could just take the dimensions from the scale drawing, calculate area, and then apply the ratio of areas to find the actual amount of carpet we need to buy.

Guide students to complete the follow-up question in their student materials.

Does the actual area you found reflect the results we found from Examples 1–3? Explain how you know. Yes, the scale of 1 inch to 15 feet has a scale factor of 180, so the ratio of area should be $(180)^2$, or 32.400 The drawing area is $(2)\left(1\frac{2}{3}\right)$, or $\frac{10}{3}$ square inches. The actual area is 25 feet by 30 feet, or 750 square feet, or 108,000 square inches. The value of the ratio of the areas is $\frac{108,000}{\frac{10}{3}}$, or $\frac{324,000}{10}$, or 32,400.

It would be more efficient to apply this understanding to the scale, eliminating the need to convert units.

If we use the scale of $\frac{15}{1}$, then the ratio of area is $\frac{225}{1}$.

The drawing area is $(2)(1\frac{2}{3})$, or $\frac{10}{3}$ square inches.

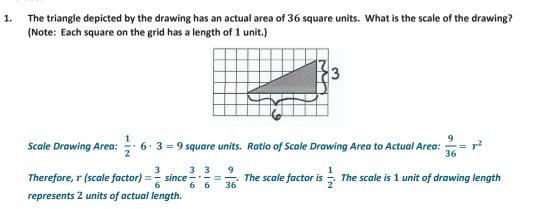
The actual area is 25 feet by 30 feet or 750 square feet.

The ratio of area is
$$\frac{750}{\frac{10}{3}}, \frac{2250}{10}, \text{ or } \frac{225}{1}$$

Exercises (15 minutes)

Allow time for students to answer independently then share results.

Exercises



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What do you think the

considering three dimensions?

For example, if the scale factor comparing length on a pair of

cubes is $\frac{1}{3}$, what is the ratio of volumes for the same cubes?

relationship is when

Scaffolding:

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For Exercise 2, allow students time to measure the drawings of the apartments using a ruler and then compare measurements with a partner. Students then continue to complete parts (a)–(f) with a partner. Allow students time to share responses. Sample answers to questions are given below.



Scaffolding:

Since the given scale is

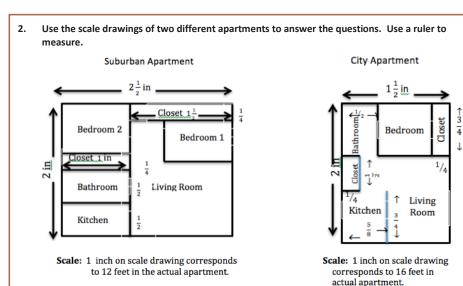
necessary that students

compute the actual areas

different for each drawing, it is

before comparing the areas in Exercise 2 parts (a)–(c).

Guide students to choose measuring units based upon how the scale is stated. For example, since 1 inch represents 12 feet, it would make sense to measure the drawing in inches.



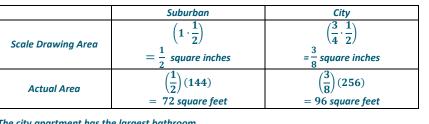
ind the scale drawing area for both apartments, and then use it to find the actual area of both apartme			
	Suburban	City	
Scale Drawing Area	$\left(2\frac{1}{2}\right)(2)$ = 5 square inches	$(2)\left(1\frac{1}{2}\right)$ = 3 square inches	
Actual Area	5(12 ²) 5(144) = 720 square feet	3(16 ²) 3(256) = 768 square feet	

Which apartment has closets with more square footage? Justify your thinking. b.

	Suburban	City
Scale Drawing Area	$\left(1\cdot\frac{1}{4}\right) + \left(1\frac{1}{2}\cdot\frac{1}{4}\right)$ $\frac{1}{4} + \frac{3}{8} = \frac{5}{8} \text{ square inches}$	$\left(\frac{1}{4} \cdot \frac{3}{4}\right) + \left(\frac{1}{2} \cdot \frac{1}{4}\right)$ $\frac{3}{16} + \frac{1}{8} = \frac{5}{16} \text{ square inches}$
Actual Area	$\left(\frac{5}{8}\right)(144) = 90$ square feet	$\left(\frac{5}{16}\right)(256) = 80$ square feet

The suburban apartment has greater square footage in the closet floors.

Which apartment has the largest bathroom? Justify your thinking. c.





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а.



A one-year lease for the suburban apartment costs \$750 per month. A one-year lease for the city apartment costs \$925. Which apartment offers the greater value in terms of the cost per square foot?
 The suburban cost per square foot is ⁷⁵⁰/₇₂₀ or approximately \$1.04 per square foot. The city cost per square foot is ⁹²⁵/₇₆₈ or approximately \$1.20 per square foot. The suburban apartment offers a greater value (cheaper cost per square foot), \$1.04 versus \$1.20.

Closing (2 minutes)

- When given a scale drawing, how do we go about finding the area of the actual object?
 - Method 1: Compute each actual length based upon the given scale and then use the actual dimensions to compute the actual area.
 - Method 2: Compute the area based upon the given scale drawing dimensions and then use the square of the scale to find actual area.
- Describe a situation where you might need to know the area of an object given a scale drawing or scale model.
 - A time where you might need to purchase materials that are priced per area, something that has a limited amount of floor space to take up, or when comparing two different blueprints

Lesson Summary	
Given the scale factor, r , representing the relationship between scale drawing length and actual length, the square of this scale factor, r^2 , represents the relationship between the scale drawing area and the actual area.	•
For example, if 1 inch on the scale drawing represents 4 inches of actual length, then the scale factor, r , is $\frac{1}{4}$. On this same drawing, 1 square inch of scale drawing area would represent 16 square inches of actual area since r^2 is $\frac{1}{2}$.	
<u>16</u> .	

Exit Ticket (5 minutes)

Scaffolding:

Extension to Exit Ticket: Ask students to show multiple methods for finding the area of the dining room.



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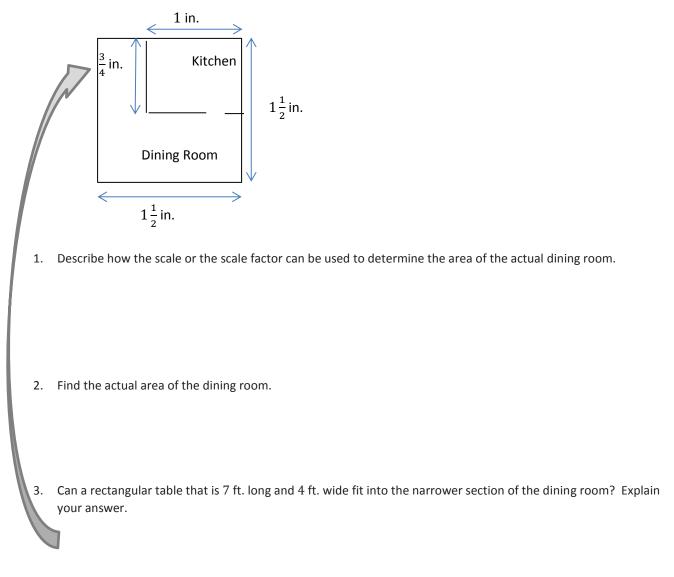
Name _____

Date

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Exit Ticket

A 1-inch length in the scale drawing below corresponds to a length of 12 feet in the actual room.





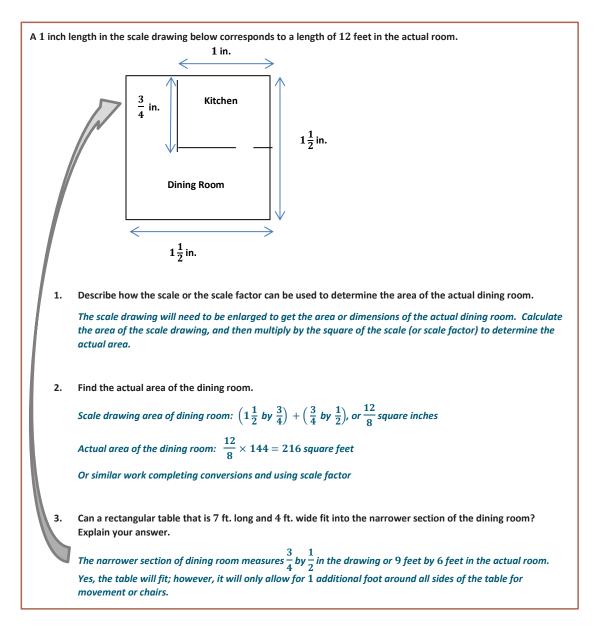
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Exit Ticket Sample Solutions





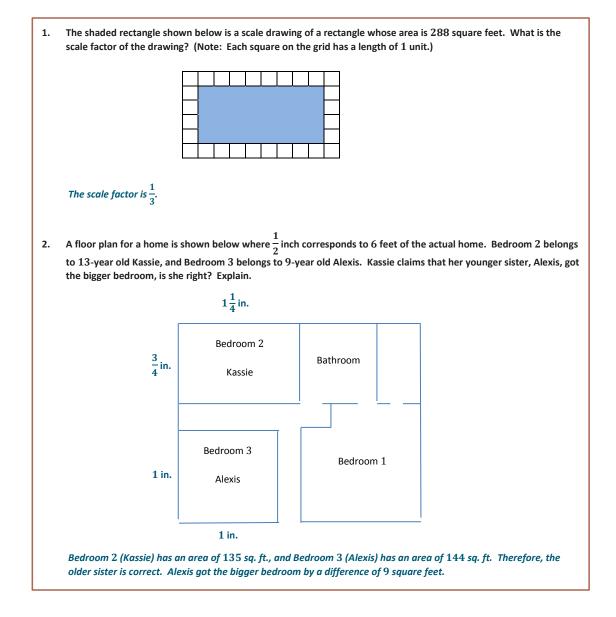
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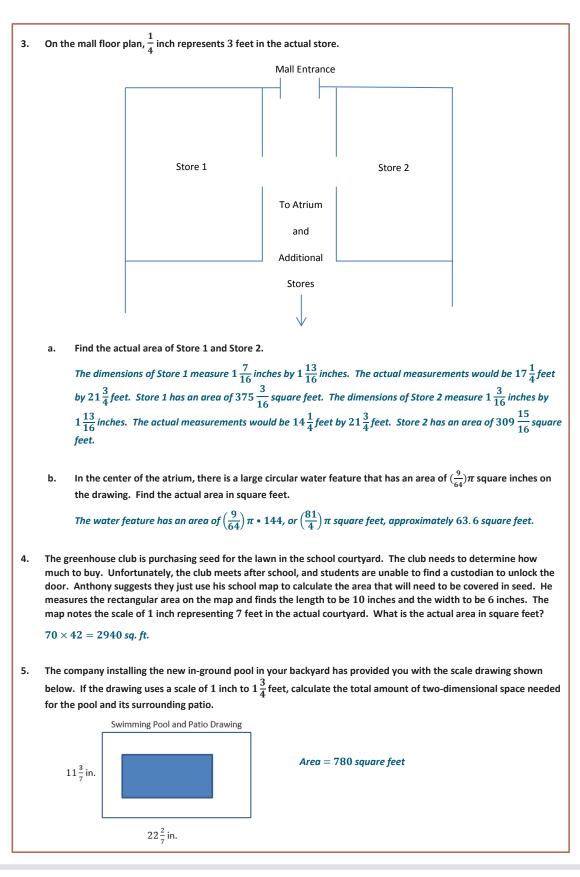
Problem Set Sample Solutions













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