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Lesson 15: Equations of Graphs of Proportional Relationships Involving Fractions

Student Outcomes

* Students use equations and graphs to represent proportional relationships arising from ratios and rates involving fractions.
* Students interpret what points on the graph of the relationship mean in terms of the situation or context of the problem.

Classwork

Review with students the meaning of unit rate, the meaning of an ordered pair in the proportional relationship context, the meaning of , and the meaning of , from Lesson 10. The goal here is to help students see the relationship between the unit rate and the changes in and .

**Example 1 (10 minutes): Mother’s 10K Race**

**MP.1**

**&**

**MP.2**

Use the table to determine the constant of proportionality and remind students how this was done in earlier lessons. Help students to understand what the constant of proportionality means in the context of this problem.

* Discuss and model with students how to graph fractional coordinates so that the ordered pairs are as accurate as possible.

*Scaffolding:*

* A K race has a length of kilometers (approximately miles).
* Help students find ordered pairs from graphs that fall on coordinates that are easy to see.
* Have students use the coordinates to determine the constant of proportionality (unit rate).

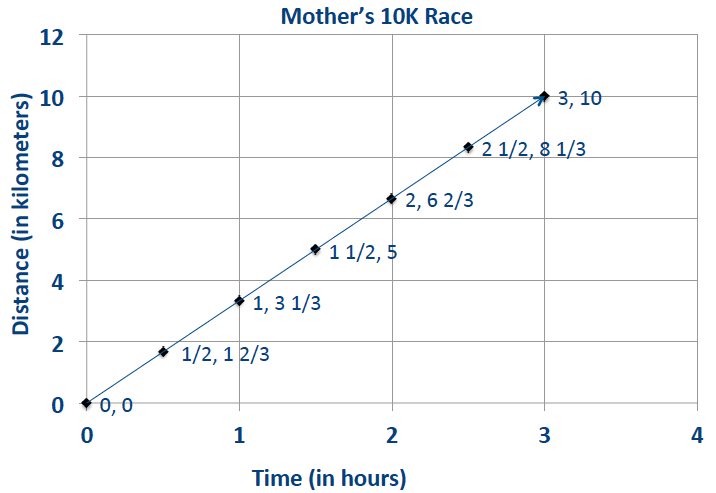
Example 1: Mother’s K Race

Sam’s mother has entered a K race. Sam and his family want to show their support for their mother, but they need to figure out where they should go along the race course. They also need to determine how long it will take her to run the race so that they will know when to meet her at the finish line. Previously, his mother ran a K race with a time of hours. Assume Sam’s mother will run the same rate as the previous race in order to complete the chart.

* Discuss with your partner: Can you find Sam’s mother’s average rate for the entire race based on her previous race time?
  + *km/h, or km/h*

Create a table that will show how far Sam’s mother has run after each half hour from the start of the race, and graph it on the coordinate plane to the right.

|  |  |
| --- | --- |
| *Time  (, in hours)* | *Distance Run  (, in km)* |
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* 1. What are some specific things you notice about this graph?

It forms a line through the origin; it relates time (in hours) to the distance run (in kilometers); the line through the origin means that the values are proportional.

* 1. What is the connection between the table and the graph?

The time (in hours) is on the horizontal axis, and the distance run (in kilometers) is on the vertical axis; the coordinates of the points on the line are the same as the pairs of numbers in the table.

* 1. What does the point represent in the context of this problem?

After hours, she has run km.

Discuss the responses with the class and draw a conclusion.

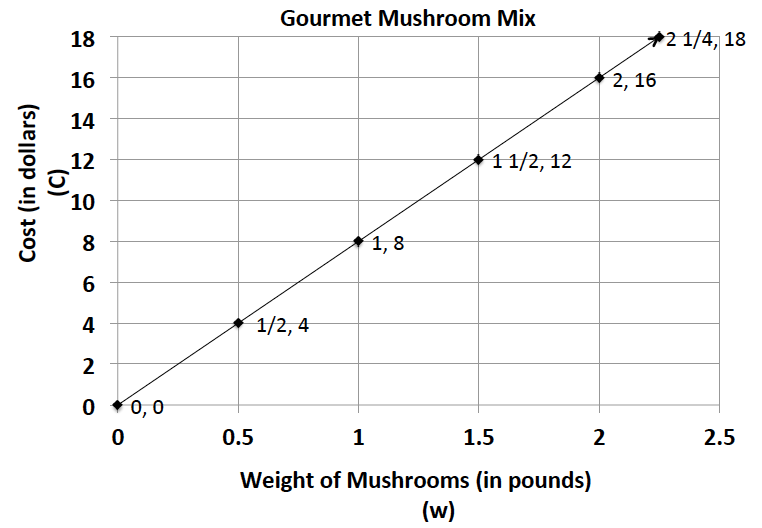
* Write an equation that models the data in the chart. Record the student responses so that they can see all responses.
* *, where represents the distance and represents the hours (or ).*

**Example 2** **(10** **minutes): Gourmet Cooking**

Students should write the equation from the data given and complete the ordered pairs in the table. Pose the questions to the students as a whole group, one question at a time:

Example 2: Gourmet Cooking

MP.1

After taking a cooking class, you decide to try out your new cooking skills by preparing a meal for your family. You have chosen a recipe that uses gourmet mushrooms as the main ingredient. Using the graph below, complete the table of values and answer the following questions.

|  |  |
| --- | --- |
| Weight  (in pounds) | Cost  (in dollars) |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

* 1. Is this relationship proportional? How do you know from examining the graph?

Yes, the relationship is proportional because the graph is a line that passes through the origin.

* 1. What is the unit rate for cost per pound?

. The unit rate is .

* 1. Write an equation to model this data.
  2. What ordered pair represents the unit rate, and what does it mean?

The unit rate is , which means that one pound of mushrooms costs .

* 1. What does the ordered pair mean in the context of this problem?

This means pounds of mushrooms cost .

* 1. If you could spend on mushrooms, how many pounds could you buy?

; . You can buy pounds of mushrooms with.

* 1. What would be the cost of pounds of mushrooms?

***;;* *;***

Have students share how they would find the cost for lb., oz. of mushrooms. Students convert lb., oz. to lb., then multiply the weight by to determine the cost of .

Discuss the usefulness of equations as models and how they help to determine very large or very small values that are difficult or impossible to see on a graph.

Students should complete these problems in cooperative groups, and then be assigned one problem per group to present in a gallery walk. As groups of students walk around the room to view the work, have them write feedback on sticky notes about presentations, clarity of explanations, etc. Students should compare their answers and have a class discussion after the walk about any solutions in which groups disagreed or found incomplete.

MP.2

Closing (5 minutes)

After the gallery walk, refer back to the graphs and charts that students presented.

* Are all graphs lines through the origin?
* Did each group write the equation that models the situation in their problem?
* Did each group find the correct constant of proportionality (unit rate) for their problem and describe its meaning in the context of the problem using appropriate units?

Lesson Summary

Proportional relationships can be represented through the use of graphs, tables, equations, diagrams, and verbal descriptions.

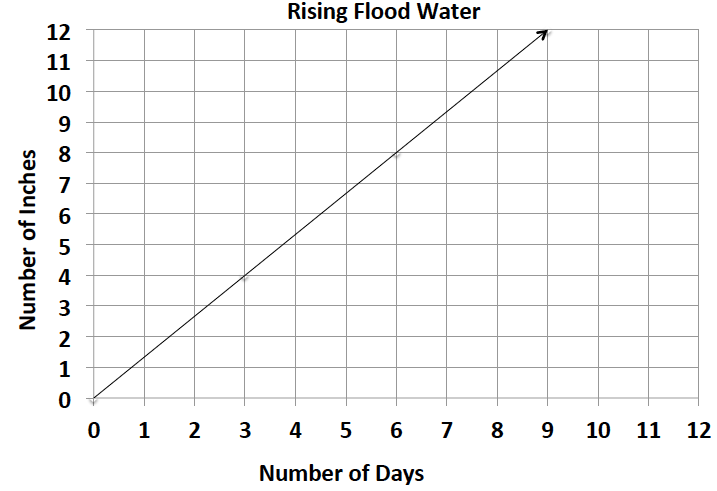
In a proportional relationship arising from ratios and rates involving fractions, *the graph* gives a visual display of *all values* of the proportional relationship, especially the quantities that fall between integer values.

Exit Ticket (5 minutes)

Name \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ Date\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

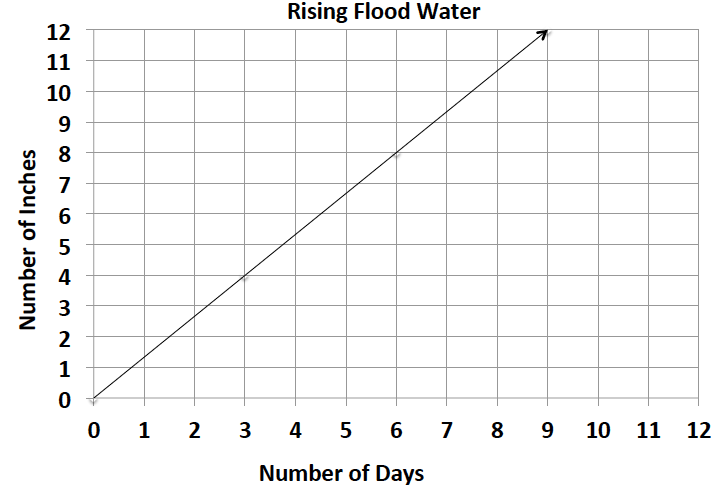
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Exit Ticket

Using the graph and its title:

1. Describe the relationship that the graph depicts.
2. Identify two points on the line and explain what they mean in the context of the problem.
3. What is the unit rate?
4. What point represents the unit rate?

Exit Ticket Sample Solutions

1. Describe the relationship that the graph depicts.

The graph shows that in days the water rose to inches. The water has risen at a constant rate. Therefore, the water has risen inches per day.

1. Identify two points on the line and explain what they mean in the context of the problem.

means that by theth day, the water rose inches; means that by the th day, the water rose inches.

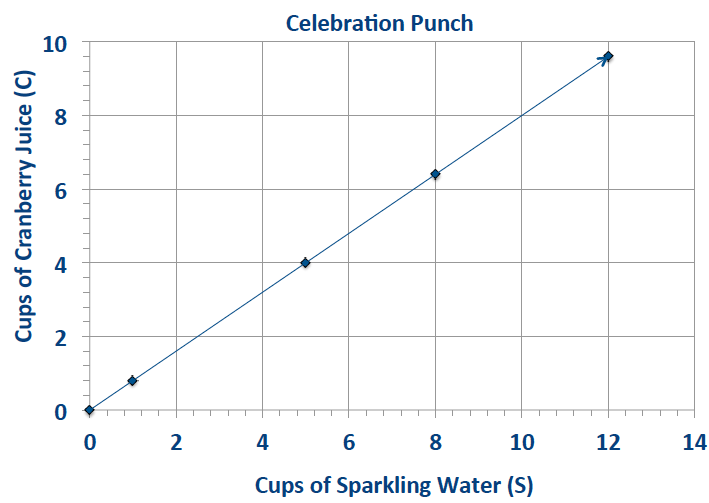
1. What is the unit rate?

The unit rate in inches per day is .

1. What point represents the unit rate?

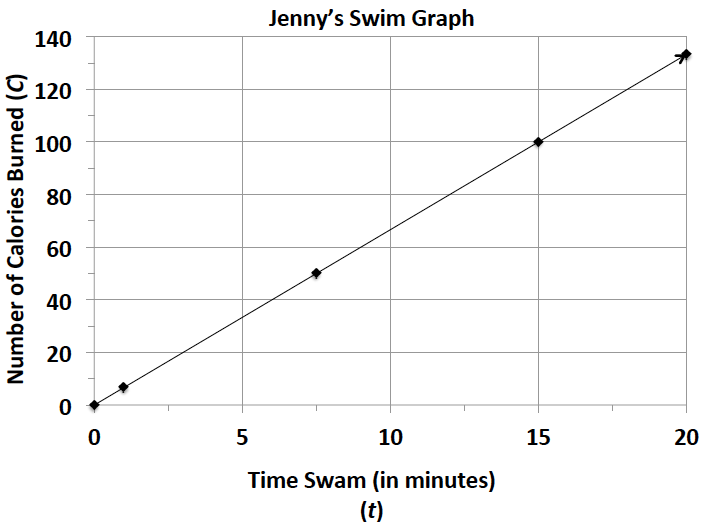
The point that shows the unit rate is

Problem Set Sample Solutions

1. Students are responsible for providing snacks and drinks for the Junior Beta Club Induction Reception. Susan and Myra were asked to provide the punch for the students and family members who will attend the event. The chart below will help Susan and Myra determine the proportion of cranberry juice to sparkling water that will be needed to make the punch. Complete the chart, graph the data, and write the equation that models this proportional relationship.

|  |  |
| --- | --- |
| Sparkling Water (, in cups) | Cranberry Juice  (, in cups) |
|  |  |
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, where represents the number of cups of cranberry juice and represents the number of cups of sparkling water.

1. Jenny is a member of a summer swim team.

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* 1. Using the graph, determine how many calories she burns in one minute?

Jenny burns calories every minutes, so she burns calories each minute.

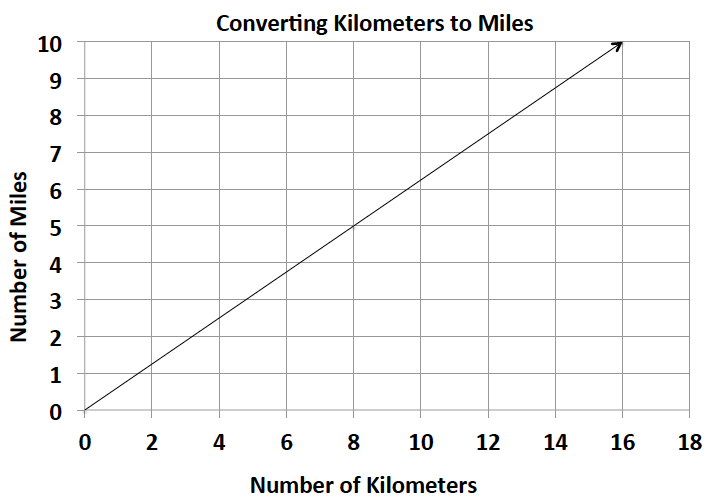
* 1. Use the graph to determine the equation that models the number of calories Jenny burns within a certain number of minutes.

, where represents the number of calories burned and represents the time she swims in minutes.

* 1. How long will it take her to burn off a -calorie smoothie that she had for breakfast?

It will take Jenny minutes of swimming to burn off the smoothie she had for breakfast.

1. Students in a world geography class want to determine the distances between cities in Europe. The map gives all distances in kilometers. The students want to determine the number of miles between towns so they can compare distances with a unit of measure with which they are already familiar. The graph below shows the relationship between a given number of kilometers and the corresponding number of miles.



* 1. Find the constant of proportionality, or the rate of miles per kilometer, for this problem and write the equation that models this relationship.

The constant of proportionality is .

The equation that models this situation is , where represents the number of miles, and represents the number of kilometers.

* 1. What is the distance in kilometers between towns that are miles apart?

The distance between towns that are miles apart is km.

* 1. Describe the steps you would take to determine the distance in miles between two towns that are kilometers apart?

Solve the equation . To find the number of miles for km, multiply by .   
miles.

1. During summer vacation, Lydie spent time with her grandmother picking blackberries. They decided to make blackberry jam for their family. Her grandmother said that you must cook the berries until they become juice and then combine the juice with the other ingredients to make the jam.
   1. Use the table below to determine the constant of proportionality of cups of juice to cups of blackberries.

|  |  |
| --- | --- |
| Cups of Blackberries | Cups of Juice |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

;One cup of juice is produced when cups of blackberries are cooked.

* 1. Write an equation that will model the relationship between the number of cups of blackberries and the number of cups of juice.

, where represents the number of cups of juice and represents the number of cups of blackberries.

* 1. How many cups of juice were made from cups of berries? How many cups of berries are needed to make cups of juice?

cups of juice are made from cups of berries.  
 cups of berries are needed to make cups of juice.