

Lesson 10: Interpreting Graphs of Proportional

Relationships

Student Outcomes

- Students consolidate their understanding of equations representing proportional relationships as they interpret what points on the graph of a proportional relationship mean in terms of the situation or context of the problem, including the point (0, 0).
- Students are able to identify and interpret in context the point (1, r) on the graph of a proportional relationship where r is the unit rate.

Classwork

MP.1

MP.2

Examples (15 minutes)

Example 1 is a review of previously taught concepts, but the lesson will be built upon this example. Pose the challenge to the students to complete the table.

Have students work individually and then compare and critique each other's work with a partner.

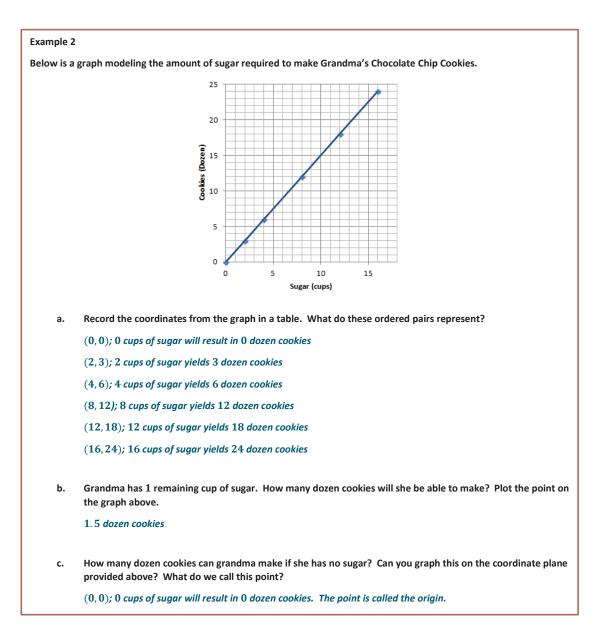
useo	ate a table comparin d to the amount of c	ng the amount of flour cookies.	Is the number of cookies proportional to the amount of flour used? Explain why or why	What is the unit rate of cookies to flour $(\frac{y}{x})$, and what is the		
	Number of Cups of Flour	Number of Dozens of Cookies	not.	meaning in the context of the problem?		
	3	4	Yes, because there exists a constant, $\frac{4}{3}$ or $1\frac{1}{3}$, such that	$1\frac{1}{3}$		
	6 12	8 16	constant, $\frac{1}{3}$ or $1\frac{1}{3}$, such that each measure of the cups of flour multiplied by the constant gives the corresponding measure of cookies.	$\frac{1}{3}$ 1 $\frac{1}{3}$ dozen cookies, or 16 cookies for 1 cup of flour		
Cookies (Dozen)	del the relationship of th	on a graph.	Does the graph show the two quantities being proportional to each other? Explain. The points appear on a line that passes through the origin (0, 0).	Write an equation that can be used to represent the relationship. $D = 1\frac{1}{3}F, D = 1.\overline{3}F, \text{ or}$ $D = \frac{4}{3}F$ D represents the number of dozens of cookies F represents the number of cups of flour		



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Generate class discussion using the following questions to lead to the conclusion that the point (1, r) must be on the graph and what it means.

- How is the unit rate of $\frac{y}{r}$, or in this case $\frac{B}{4}$, related to the graph?
 - ^{\Box} The unit rate must be the value of the *y*-coordinate of the point on the graph, which has an *x*-coordinate of one.
- What quantity is measured along the horizontal axis?
 - D The number of cups of sugar
- When you plot the ordered pair (A, B), what does A represent?
 - The amount of sugar, in cups, that is needed to make B dozen cookies



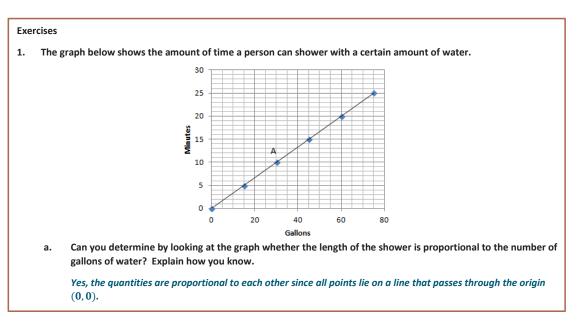
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- What quantity is measured along the vertical axis?
 - The amount of cookies (number of dozens)
- When you plot the point (A, B), what does B represent?
 - D The total amount of cookies, in dozens, that can be made with A cups of sugar
- What is the unit rate for this proportional relationship?
 - ° 1.5
- Starting at the origin, if you move one unit along the horizontal axis, how far would you have to move vertically to reach the line you graphed?
 - 1.5 units
- Continue moving one unit at a time along the horizontal axis. What distance, vertically, did you move?
 - 1.5 units
- Why are we always moving 1.5 units vertically?
 - The unit rate is 1.5 dozen cookies for every 1 cup of sugar. The vertical axis, or y-value, represents the number of dozens of cookies. Since the unit rate is 1.5, every vertical move would equal the unit rate of 1.5 units.
- Do you think the vertical move will always be equal to the rate when moving 1 unit horizontally whenever two quantities that are proportional are graphed?
 - Yes, the vertical distance will always be equal to the unit rate when moving one unit horizontally on the axis.
- Graphs of different proportional relationship have different points, but what point must be on every graph of a
 proportional relationship? Explain why.
 - The point (1,r) or unit rate must be on every graph because the unit rate describes the change in the vertical distance for every 1 unit change in the horizontal axis.

Exercises (20 minutes)

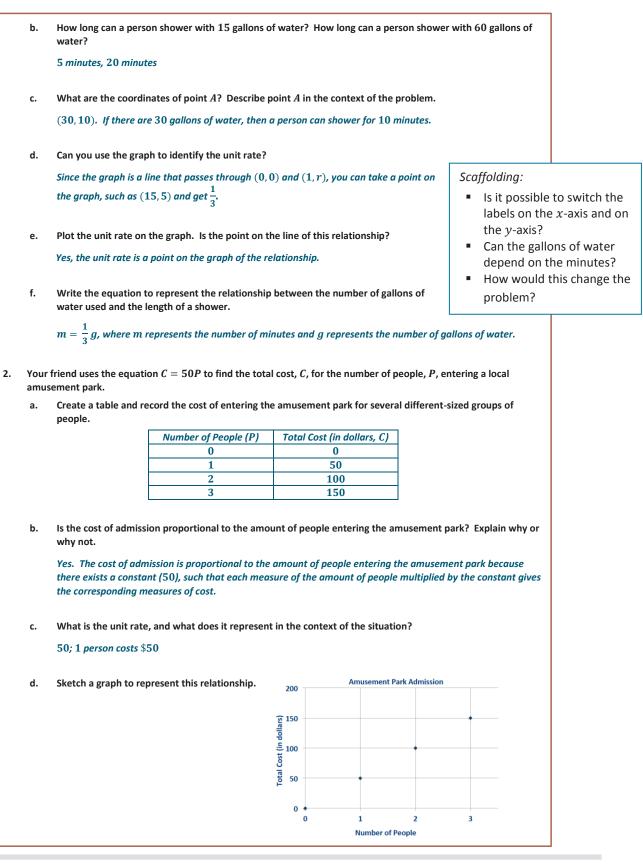




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What points must be on the graph of the line if the two quantities represented are proportional to each other? Explain why and describe these points in the context of the problem.

(0,0) and (1,50). If 0 people enter the park, then the cost would be 0. If 1 person enters the park, the cost would be 50. For every 1-unit increase along the horizontal axis, the change in the vertical distance is 50 units.

f. Would the point (5, 250) be on the graph? What does this point represent in the context of the situation? Yes, the point (5, 250) would be on the graph because 5(50) = 250. The meaning is that it would cost a total of \$250 for 5 people to enter the amusement park.

Closing (5 minutes)

e.

- What points are always on the graph of two quantities that are proportional to each other?
 - ^D The points (0,0) and (1,r), where *r* is the unit rate, are always on the graph.
- How can you use the unit rate of $\frac{y}{x}$ to create a table, equation, or graph of a relationship of two quantities that are proportional to each other?
 - In a table, you can multiply each x-value by the unit rate to obtain the corresponding y-value, or you can divide every y-value by the unit rate to obtain the corresponding x-value. You can use the equation y = kx and replace the k with the unit rate of $\frac{y}{x}$. In a graph, the points (1, r) and (0,0) must appear on the line of the proportional relationship.
- How can you identify the unit rate from a table, equation, or graph?
 - From a table, you can divide each y-value by the corresponding x-value. If the ratio y : x is equivalent for the entire table, then the value of the ratio, $\frac{y}{x}$, is the unit rate, and the relationship is proportional. In an equation in the form y = kx, the unit rate is the number represented by the k. If a graph of a line passes through the origin and contains the point (1, r), r representing the unit rate, then the relationship is proportional.
- How do you determine the meaning of any point on a graph that represents two quantities that are proportional to each other?
 - Any point (*A*, *B*) on a graph that represents a proportional relationship represents a number *A* corresponding to the *x*-axis or horizontal unit, and *B* corresponds to the *y*-axis or vertical unit.

Lesson Summary

The points (0,0) and (1,r), where r is the unit rate, will always appear on the line representing two quantities that are proportional to each other.

- The unit rate, *r*, in the point (1, *r*) represents the amount of vertical increase for every horizontal increase of 1 unit on the graph.
- The point (0, 0) indicates that when there is zero amount of one quantity, there will also be zero amount of the second quantity.

These two points may not always be given as part of the set of data for a given real-world or mathematical situation, but they will always appear on the line that passes through the given data points.

Exit Ticket (5 minutes)







Name _____

Date_____

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Exit Ticket

Great Rapids White Water Rafting Company rents rafts for 125 per hour. Explain why the point (0,0) and (1,125) are on the graph of the relationship, and what these points mean in the context of the problem.









Exit Ticket Sample Solutions

Great Rapids White Water Rafting Company rents rafts for 125 per hour. Explain why the point (0, 0) and (1, 125) are on the graph of the relationship, and what these points mean in the context of the problem.

Every graph of a proportional relationship must include the points (0,0) and (1,r). The point (0,0) is on the graph because 0 can be multiplied by the constant to determine the corresponding value of 0. The point (1,125) is on the graph because it is the unit rate. On the graph, for every 1 unit change on the horizontal axis, the vertical axis will change by 125 units. The point (0,0) means 0 hours of renting a raft would cost \$0, and (1,125) means 1 hour of renting the raft would cost \$125.

Problem Set Sample Solutions

	a.	What does the point $({\bf 5}, {\bf 290})$ represent in the context of the situation?		Jaguar's Speed: Time and Distance					
				-					
		In 5 seconds, a jaguar can run 290 feet.	000 (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	-	/ 10, 560				
				-					
			Distance (in feet) 000 005 000 006	-					
	b.	What does the point $(3, 174)$ represent in the context of the situation?	008 Jista		5, 290				
			200	3, 174					
		A jaguar can run 174 feet in 3 seconds.	100						
			0	★ 1, 58 ★ 0, 0					
	c.	Is the distance run by the jaguar proportional to		0	5	10	15		
		the time? Explain why or why not.		Tim	e (in seconds)				
		Yes, the distance run by the jaguar is proportional that passes through the origin $(0,0)$.	to the th		, account in	. <u>9</u> . apri 5100	e a mie		
(d.	Write an equation to represent the distance run by the jaguar. Explain or model your reasoning.							
		y = 58x							
		The constant of proportionality, or unit rate of $\frac{y}{x}$ is 58 and can be substituted into the equation y							
		place of k.							
	Chan	npionship t-shirts sell for \$22 each.							
	a.	What point(s) must be on the graph for the quantities to be proportional to each other?							
		(0,0), (1,22)							
	b.	What does the ordered pair $(5,110)$ represent in the context of this problem?							
		5 t-shirts will cost \$110.							
		How many t-shirts were sold if you spent a total of \$88?							
	c.	How many t-shirts were sold if you spent a total o	f \$88?						



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3.

4.

а.

b.

The graph represents the total cost of renting a car. The **Car Rental Fee** 400 cost of renting a car is a fixed amount each day, • 6, 375 regardless of how many miles the car is driven. 350 **I**S What does the ordered pair (4, 250) represent? 300 문 250 4 250 It would cost \$250 to rent a car for 4 days. Е. 200 Cost 150 100 To • 2, 125 What would be the cost to rent the car for a week? Explain or model your reasoning. • 1.62.5 50 Since the unit rate is 62.5, the cost for a week 0 0,0 0 2 4 would be 62.5(7) = \$437.50. Number of Days Jackie is making a snack mix for a party. She is using cashews and peanuts. The table below shows the relationship of the number of packages of cashews she needs to the number of cans of peanuts she needs to make the mix. **Packages of Cashews Cans of Peanuts** 0 0 1 2 2 4

6

8

What points must be on the graph for the number of cans of peanuts to be proportional to the number of a. packages of cashews? Explain why.

(0,0) and (1,2). All graphs of proportional relationships are lines that pass through the origin (0,0) and the unit rate (1, r).

b. Write an equation to represent this relationship.

> y = 2x, where x represents the number of packages of cashews and y represents the number of cans of peanuts.

c. Describe the ordered pair (12, 24) in the context of the problem.

In the mixture, you will need 12 packages of cashews and 24 cans of peanuts.

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5. The following table shows the amount of candy and price paid.

Amount of Candy (in pounds)	2	3	5
Cost (in dollars)	5	7.5	12.5

Is the cost of the candy proportional to the amount of candy? a.

Yes, because there exists a constant, 2.5, such that each measure of the amount of candy multiplied by the constant gives the corresponding measure of cost.

- Write an equation to illustrate the relationship between the amount of candy and the cost. b.
 - y = 2.5x

Using the equation, predict how much it will cost for 12 pounds of candy. c.

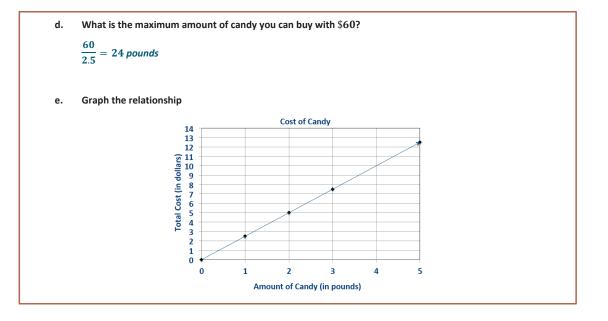
2.5(12) = \$30



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