

Lesson 4: Construct a Perpendicular Bisector

Student Outcome

 Students construct a perpendicular bisector and discover the relationship between symmetry with respect to a line and a perpendicular bisector.

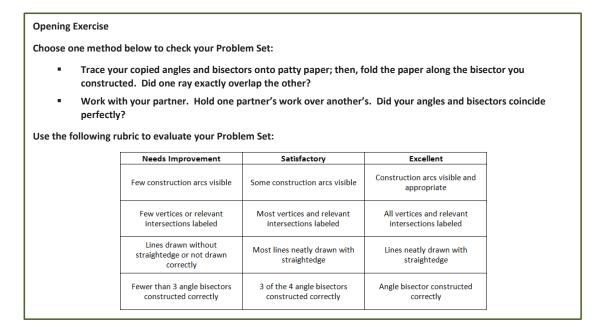
Lesson Notes

In Lesson 4, students learn to construct perpendicular bisectors and apply the construction to problems. Students continue to write precise instructions for constructions. The importance of specific language continues throughout the construction lessons. The steps for constructing an angle bisector from the previous lesson flow nicely into the steps for constructing a perpendicular bisector.

The Opening Exercise is another opportunity for students to critique their work. Students use a rubric to assess the Lesson 3 Problem Set on angle bisectors. Determine where students feel they are making errors (i.e., if they score low on the rubric). In the Discussion, students make a connection between Lesson 3 and Lesson 4 as an angle bisector is linked to a perpendicular bisector. Students should understand that two points are symmetric with respect to a line if and only if the line is the perpendicular bisector of the segment that joins the two points. Furthermore, students should be comfortable with the idea that any point on the perpendicular bisector is equidistant from the endpoints of the segment. Lastly, students will extend the idea behind the construction of a perpendicular bisector to construct a perpendicular to a line from a point not on the line.

Classwork

Opening Exercise (5 minutes)





Lesson 4: Date: Construct a Perpendicular Bisector 10/10/14

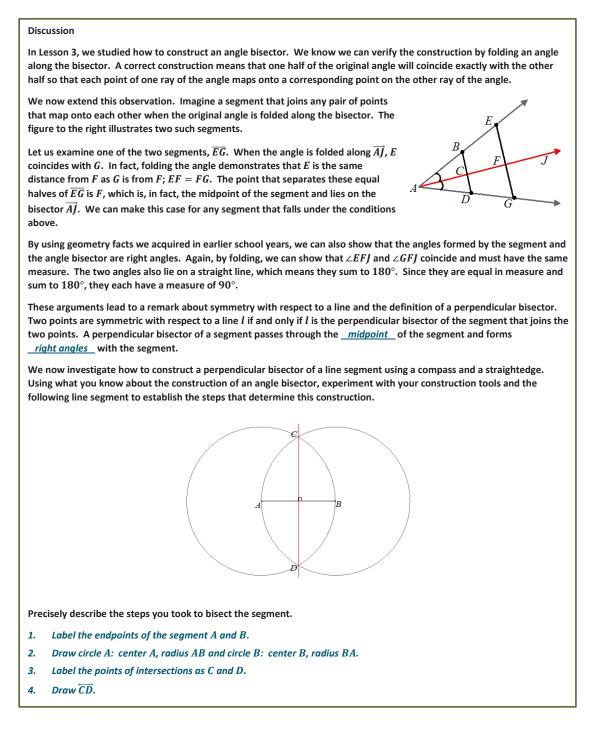
engage^{ny}





Mathematical Modeling Exercise (37 minutes)

In addition to the discussion, have students participate in a kinesthetic activity that illustrates the idea of an angle bisector. Ask students to get out of their seats and position themselves at equal distances from two adjacent classroom walls. The students form the bisector of the (likely right) angle formed at the meeting of the adjacent walls.





Lesson 4: Date: Construct a Perpendicular Bisector 10/10/14





engage

Now that you are familiar with the construction of a perpendicular bisector, we must make one last observation. Using your compass, string, or patty paper, examine the following pairs of segments: i. \overline{AC} . \overline{BC} D $\overline{AD}, \overline{BD}$ ii. AE, BE iii. Based on your findings, fill in the observation below. **Observation:** Any point on the perpendicular bisector of a line segment is <u>equidistant</u> from the endpoints of the line segment. Mathematical Modeling Exercise You know how to construct the perpendicular bisector of a segment. Now, you will investigate how to construct a perpendicular to a line ℓ from a point A not on ℓ . Think about how you have used circles in constructions so far and why the perpendicular bisector construction works the way it does. The first step of the instructions has been provided for you. Discover the construction and write the remaining steps. Step 1. Draw circle A: center A, with radius so that circle A intersects line ℓ in two points. Step 2: Label the two points of intersection as B and C. Step 3: Draw circle B: center B, radius BC. Step 4: Draw circle C: center C, radius CB. Step 5: Label the unlabeled intersection of circle B and circle C as D. Step 6: Draw AD. **Relevant Vocabulary** <u>Right Angle</u>: An angle is called a *right angle* if its measure is 90° . Perpendicular: Two lines are perpendicular if they intersect in one point and if any of the angles formed by the intersection of the lines is a 90° (right) angle. Two segments or rays are perpendicular if the lines containing them are perpendicular lines. Equidistant: A point A is said to be equidistant from two different points B and C if AB = AC. A point A is said to be equidistant from a point B and a line l if the distance between A and l is equal to AB.

Exit Ticket (3 minutes)



Construct a Perpendicular Bisector 10/10/14

engage^{ny}





32



Name

Date

Lesson 4: Construct a Perpendicular Bisector

Exit Ticket

Divide the following segment AB into four segments of equal length.









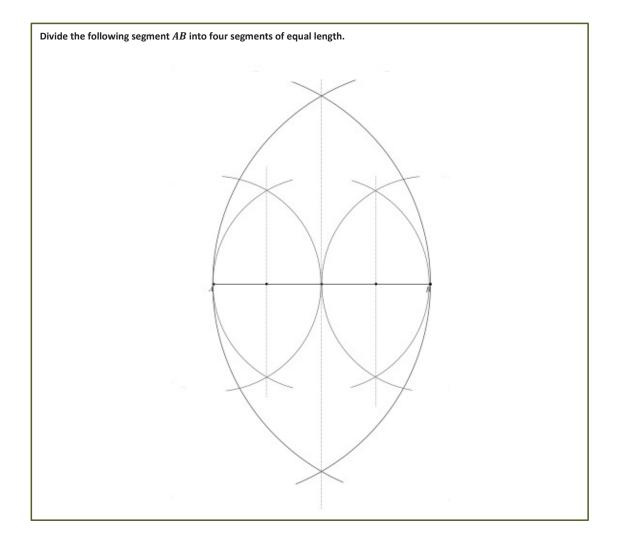
33







Exit Ticket Sample Solution





Construct a Perpendicular Bisector 10/10/14





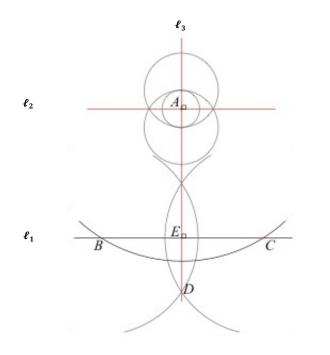


Problem Set Sample Solutions

1. During this lesson, you constructed a perpendicular line to a line ℓ from a point A not on ℓ . We are going to use that construction to construct parallel lines.

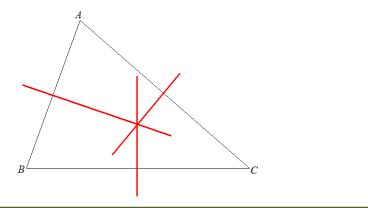
To construct parallel lines ℓ_1 and ℓ_2 :

- i. Construct a perpendicular line ℓ_3 to a line ℓ_1 from a point A not on ℓ_1 .
- ii. Construct a perpendicular line ℓ_2 to ℓ_3 through point *A*. *Hint:* Consider using the steps behind Problem 4 in the Lesson 3 Problem Set to accomplish this.



2. Construct the perpendicular bisector of \overline{AB} , \overline{BC} , and \overline{CA} on the triangle below. What do you notice about the segments you have constructed?

Students should say that the three perpendicular bisectors pass through a common point. (Students may additionally conjecture that this common point is equidistant from the vertices of the triangle.)





MP.5

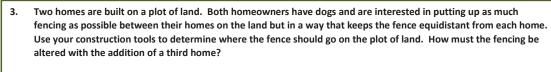
Lesson 4: Date: Construct a Perpendicular Bisector 10/10/14

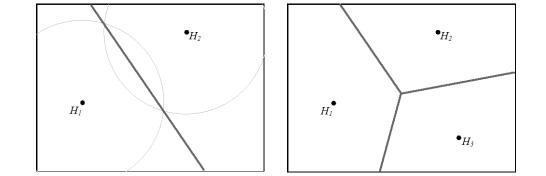
engage^{ny}



This work is licensed under a <u>Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.</u>









Construct a Perpendicular Bisector 10/10/14



