

Lesson 18: Analyzing Residuals

Student Outcomes

- Students use a graphing calculator to construct the residual plot for a given data set.
- Students use a residual plot as an indication of whether the model used to describe the relationship between two numerical variables is an appropriate choice.

Lesson Notes

In this lesson, students continue to construct residual plots. Residual plots are analyzed to determine if the points are scattered at random around the horizontal line (indicating a linear relationship) or if the points have a pattern (indicating a nonlinear relationship).

Classwork

The previous lesson shows that when data is fitted to a line, a scatter plot with a curved pattern produces a residual plot that shows a clear pattern. You also saw that when a line is fit, a scatter plot where the points show a straight-line pattern results in a residual plot where the points are randomly scattered.

Example 1 (10 minutes): The Relevance of the Pattern in the Residual Plot

This is another opportunity to reinforce why the particular patterns in the scatter plots result in the corresponding MP.2 patterns in the residual plots. Pose these questions:

- Why does the first scatter plot result in an arch shape in the residual plot?
 - The points in the scatter plot are not in a straight line.
- Why does the second scatter plot result in a U shape in the residual plot?
 - The points in the scatter plot are not in a straight line.
- Why does the third scatter plot result in a random scatter of points in the residual plot?
 - The points seem to be linear.

Explain how the patterns in the residual plot show us whether a linear model is a good fit for the data.

- If the points in a residual plot are random, a linear model is the best fit.
- If the points have a pattern, a line is not the best fit.

Pose the following question to students to connect back to previous lessons:

- If a linear model is not the best fit for the first and second scatter plots, what type of model might be more appropriate?
 - Exponential or (possibly) quadratic.



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Example 2 (10 minutes): Why Do You Need the Residual Plot?

Ask students the following:

MP.3



It is not a good fit. There is a nonlinear relationship.

The point is that because the scale on the vertical axis of the residual plot exaggerates the vertical deviations, the residual plot shows detail of the pattern in the residuals that is not easily seen in the scatter plot.





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How did this residual plot result from the original scatter plot?

The residuals are the vertical deviations from the least-squares line in the original scatter plot. Because of the change of scale, tiny vertical deviations can be shown as much larger distances from the zero line in the residual plot. Therefore, a very subtle curvature in the original relationship can be seen more clearly in the residual plot. This is why you draw residual plots.

Exercises 1–3 (15 minutes): Volume and Temperature

Let students work with a partner on Exercises 1–3. Then discuss and confirm answers as a class.



Although it might be clear from the scatter plot given here that there is a curved relationship between the two variables, this detail cannot however be seen in the low-resolution graph produced by a calculator.



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Closing (5 minutes)

Discuss the Lesson Summary with students.

Lesson Si	ummary
-	After fitting a line, the residual plot can be constructed using a graphing calculator. A curve or pattern in the residual plot indicates a nonlinear relationship in the original data set. A random scatter of points in the residual plot indicates a linear relationship in the original data set.

Exit Ticket (5 minutes)







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Exit Ticket

1. If you see a clear curve in the residual plot, what does this say about the original data set?

2. If you see a random scatter of points in the residual plot, what does this say about the original data set?







Exit Ticket Sample Solutions

If you see a clear curve in the residual plot, what does this say about the original data set? 1.

A clear curve in the residual plot shows that the variables in the original data set have a nonlinear relationship.

2. If you see a random scatter of points in the residual plot, what does this say about the original data set?

A random scatter of points in the residual plot shows that a straight line is an appropriate model for the relationship between the two variables in the original data set.

Problem Set Sample Solutions





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