

## **Student Outcomes**

- Students determine a linear function given a verbal description of a linear relationship between two quantities.
- Students interpret linear functions based on the context of a problem.
- Students sketch the graph of a linear function by constructing a table of values, plotting points, and connecting points by a line.

## **Lesson Notes**

In this first lesson, students construct linear functions based on verbal descriptions of bivariate data. They graph the linear functions by creating a table of values, plotting points, and drawing the line. Throughout this lesson, provide students with the opportunity to explain the functions in terms of the equation of the line and the relationship between the two variables. Emphasize the context with students as they explain the rates of change and the initial values.

## Classwork

## Example 1 (2–3 minutes): Logging On

Read through the example as a class. Convey to students that the information presented in the example can be organized into ordered pairs or points. Minutes can be represented by x and cost by y.

#### Example 1: Logging On

Lenore has just purchased a tablet computer, and she is considering purchasing an internet access plan so that she can connect to the Internet wirelessly from virtually anywhere in the world. One company offers an internet access plan so that when a person connects to the company's wireless network, the person is charged a fixed access fee for connecting, PLUS an amount for the number of minutes connected based upon a constant usage rate in dollars per minute.

Lenore is considering this company's plan, but the company's advertisement does not state how much the fixed access fee for connecting is, nor does it state the usage rate. However, the company's website says that a 10-minute session costs 0.40, a 20-minute session costs 0.70, and a 30-minute session costs 1.00. Lenore decides that she will use these pieces of information to determine both the fixed access fee for connecting and the usage rate.

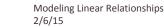
## Exercises 1–6 (10 minutes)

This exercise set introduces students to constant rate of change and initial value and how those values are used to construct a function to model a situation. Pose each exercise to the class, one at a time, using the following questions to encourage discussion.

After Exercise 1, discuss as a class the need to graph this real-world problem only in the first quadrant. Begin by asking students the following:

- If we used the entire coordinate plane to graph this line, what would the negative x values represent?
  - The *x*-axis represents minutes. So, time would be negative, which does not make sense in the context of the problem.







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For Exercise 2, use the table to demonstrate constant rate of change to students.

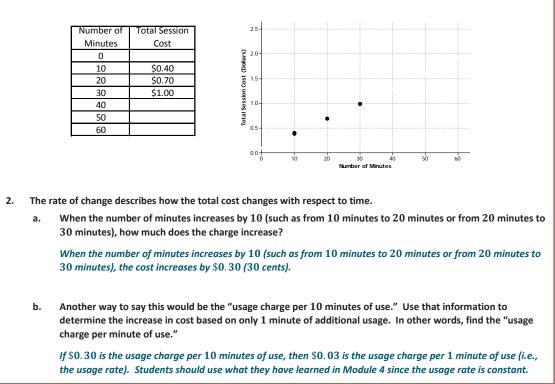
How could we use the table to determine the constant rate of change?

Number of	Total Session	Ţ	
Minutes	Cost		
0		]	
10	\$0.40	5	+ \$0.30
20	\$0.70	R	
30	\$1.00		+ \$0.30
40		]	
50		]	
60		l	

#### Exercises 1–6

1. Lenore makes a table of this information and a graph where *number of minutes* is represented by the horizontal axis and *total session cost* is represented by the vertical axis. Plot the three given points on the graph. These three points appear to lie on a line. What information about the access plan suggests that the correct model is indeed a linear relationship?

The amount charged for the minutes connected is based upon a constant usage rate in dollars per minute.





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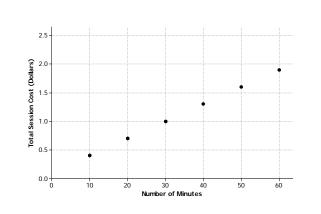




3. The company's pricing plan states that the usage rate is constant for any number of minutes connected to the Internet. In other words, the increase in cost for 10 more minutes of use (the value that you calculated above) will be the same whether you increase from 20 to 30 minutes, 30 to 40 minutes, etc. Using this information, determine the total cost for 40 minutes, 50 minutes, and 60 minutes of use. Record those values in the table, and plot the corresponding points on the graph in Exercise 1.

#### Consider the following table and graphs.

Number of Minutes	Total Session Cost
0	
10	\$0.40
20	\$0.70
30	\$1.00
40	<b>\$1.30</b>
50	\$ <b>1</b> .60
60	\$1.90

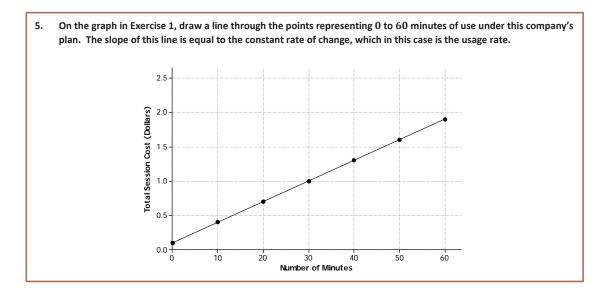


4. Using the table and the graph in Exercise 1, compute the hypothetical cost for 0 minutes of use. What does that value represent in the context of the values that Lenore is trying to figure out?

Since there is a \$0.30 decrease in cost for each decrease of 10 minutes of use, one could subtract \$0.30 from the cost value for 10 minutes and arrive at the hypothetical cost value for 0 minutes. That cost would be 0.10. Students may notice that such a value follows the regular pattern in the table. (This value could also be found from the graph after completing Exercise 6.)

Convey to students that this is known as the initial value.

- Why is this a hypothetical cost?"
  - Because it is impossible to connect for 0 minutes; the connection will always be for some interval of time.





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6. Using *x* for the number of minutes and *y* for total cost in dollars, write a function to model the linear relationship between minutes of use and total cost.

#### y = 0.03x + 0.10

# Example 2 (2–3 minutes): Another Rate Plan

Provide students time to read the example. As a whole group, summarize this alternative rate plan.

#### Example 2: Another Rate Plan

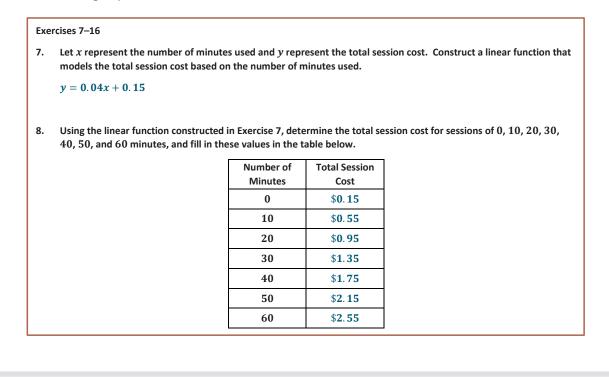
A second wireless access company has a similar method for computing its costs. Unlike the first company that Lenore was considering, this second company explicitly states its access fee is 0.15, and its usage rate is 0.04 per minute.

Total Session Cost = \$0.15 + \$0.04(number of minutes)

- How is this plan presented differently?
  - In this case, we are given the access fee and usage rate with an equation. In the first example, just data points were given.
- Based on the work with the first set of problems, how do you think the two plans are different?
  - The values for the access fee and usage charge per minute are different, or the initial value and the rate of change are different.

# Exercises 7–9 (7 minutes)

Allow students to work independently on these exercises. After most students have completed the problems, discuss problems as a whole group.





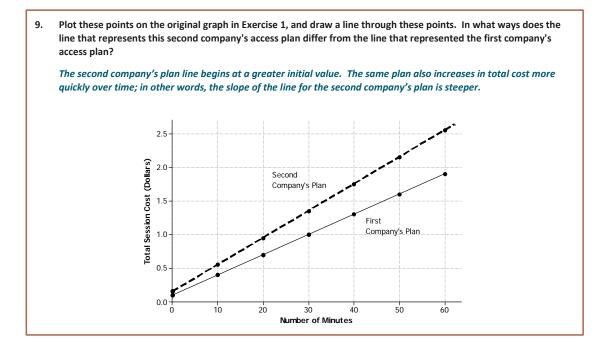
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8.6

Lesson 1





# Exercises 10–12 (7 minutes)

MP3 download sites are a popular forum for selling music. Different sites offer pricing that depend on whether or not you want to purchase an entire album or individual songs "à la carte." One site offers MP3 downloads of individual songs with the following price structure: a \$3\$ fixed fee for monthly subscription PLUS a charge of \$0.25 per song.

10. Using *x* for the number of songs downloaded and *y* for the total monthly cost, construct a linear function to model the relationship between the number of songs downloaded and the total monthly cost.

Since \$3 is the initial cost, and there is a 25 cent increase per song, the function would be

y = 3 + 0.25x or y = 0.25x + 3.

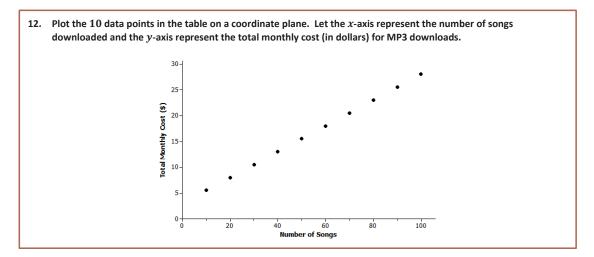
11. Construct a table to record the total monthly cost (in dollars) for MP3 downloads of 10 songs, 20 songs, and so on up to 100 songs.

Number of Songs	<b>Total Monthly Cost</b>
10	<b>\$5.50</b>
20	\$8.00
30	\$10.50
40	\$13.00
50	\$15.50
60	\$18.00
70	\$ <b>20</b> . <b>50</b>
80	\$23.00
90	\$ <b>25</b> .50
100	\$ <b>28.00</b>

COMMON CORE

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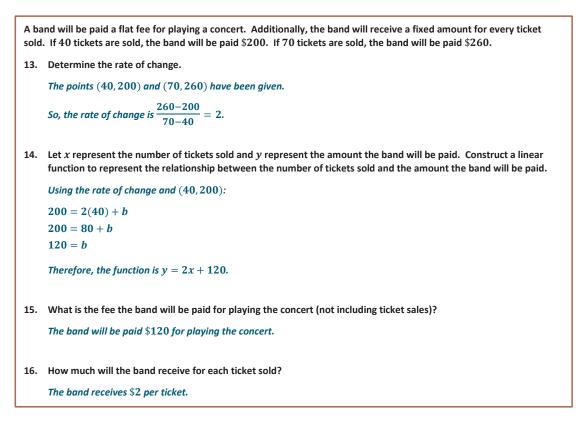
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# Exercises 13-16 (7-8 minutes)

Read through the problem as a class. The data in this exercise set is presented as two points given in context. Point out the difference by asking students the following:

- How is the data in this problem different from the data in the MP3 problem?
  - In this problem, the data can be organized as ordered pairs. In the MP3 problem, a rate of change and initial value were given.



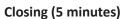


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Consider posing the following questions; allow a few student responses for each.

- In Exercise 9 when the two pricing models that Lenore was considering were both displayed on the same graph, was there ever a point at which the second company's model was a better, less expensive choice than the first company's model?
  - No, the second company always had the more expensive plan; its line was always above the other company's line.
- When comparing the equations of the two models, which value in the second company's model (the \$0.15 access fee or \$0.04 cost per minute) led you to think that it would increase at a faster rate than the first model?
  - The \$0.04 cost per minute led me to believe it would increase at a faster rate. The other company's plan only increased at a rate of \$0.03 per minute.

Lesson S	ummary
	unction can be used to model a linear relationship between two types of quantities. The graph of a linear is a straight line.
A linear f a line in v	unction can be constructed using a rate of change and initial value. It can be interpreted as an equation o vhich
•	The rate of change is the slope of the line and describes how one quantity changes with respect to another quantity.
	The initial value is the $y$ -intercept.

# Exit Ticket (5 minutes)







Lesson 1 8•6

Name

# Lesson 1: Modeling Linear Relationships

# **Exit Ticket**

A rental car company offers a rental package for a midsize car. The cost is comprised of a fixed \$30 administrative fee for the cleaning and maintenance of the car plus a rental cost of \$35 per day.

1. Using *x* for the number of days and *y* for the total cost in dollars, construct a function to model the relationship between the number of days and the total cost of renting a midsize car.

- 2. The same company is advertising a deal on compact car rentals. The linear function y = 30x + 15 can be used to model the relationship between the number of days (x) and the total cost (y) of renting a compact car.
  - a. What is the fixed administrative fee?

b. What is the rental cost per day?







# **Exit Ticket Sample Solutions**

A rental car company offers a rental package for a midsize car. The cost is comprised of a fixed \$30 administrative fee for the cleaning and maintenance of the car plus a rental cost of \$35 per day.
1. Using *x* for the number of days and *y* for the total cost in dollars, construct a function to model the relationship between the number of days and the total cost of renting a midsize car. *y* = 35*x* + 30
2. The same company is advertising a deal on compact car rentals. The linear function *y* = 30*x* + 15 can be used to model the relationship between the number of days (*x*) and the total cost (*y*) of renting a compact car.
a. What is the fixed administrative fee? *The administrative fee is* \$15.
b. What is the rental cost per day? *It costs* \$30 *per day to rent the compact car.*

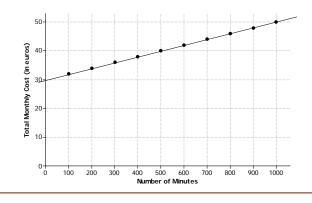
# **Problem Set Sample Solutions**

1.	Recall that Lenore was investigating two wireless access plans. Her friend in Europe says that he uses a plan in				
which he pays a monthly fee of $30$ euros plus $0.02$ euros per minute of use.					

a. Construct a table of values for his plan's monthly cost based on 100 minutes of use for the month, 200 minutes of use, and so on up to 1,000 minutes of use. (The charge of 0.02 euros per minute of use is equivalent to 2 euros per 100 minutes of use.)

Number of Minutes	Total Monthly Cost (€)
100	32.00
200	34.00
300	36.00
400	38.00
500	40.00
600	42.00
700	44.00
800	46.00
900	48.00
1,000	50.00

b. Plot these 10 points on a carefully labeled graph, and draw the line that contains these points.





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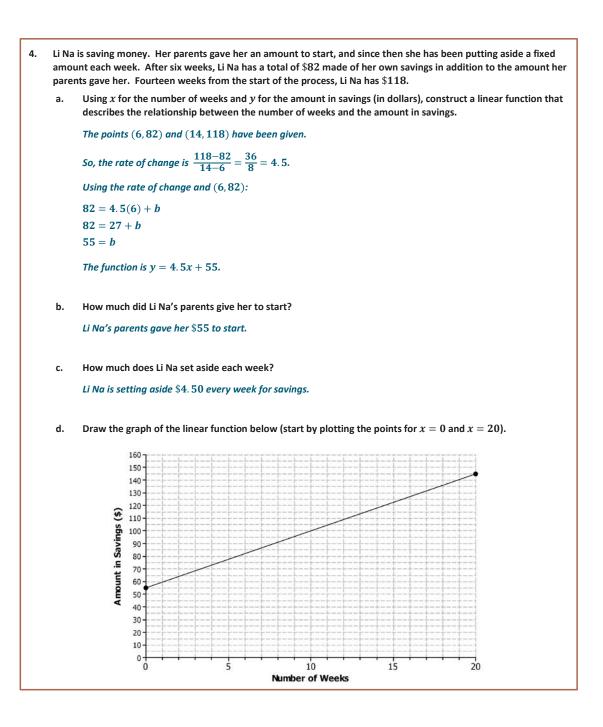

	c.	Let <i>x</i> represent min that determines mo				-	cost in eur	ros. Construct a linear f	unction
		y = 30 + 0.02x							
	d.	Use the function to the graph, would it						e. If you were to add th	is point to
		The cost for 750 mi	inutes would	be €45. T	he point (7	50,45) wo	uld be on t	he line.	
		A shipping company charges a $4.45$ handling fee in addition to $0.27$ per pound to ship a package.							
2.	A shi			-				to snip a раскаge. a linear function that de	termines
	u.	the cost of shipping	•	5	cost of sing	ping in doi			ternines
		y = 4.45 + 0.27x							
	b.	Which line (solid, de Explain.	otted, or dasl	hed) on the	e graph bel	ow represei	nts the ship	pping company's pricing	method?
		The solid line would						e is 0.27. The dashed lin e starts at an initial valu	
		٤	8+		+			+	
		:	7.						
			6						
		( <u>s</u>	5	3				   	
		Cost (dollars)	4		***				
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3.	-	wants to add new mo wing: Total Monthly				-	site offers i	ts downloading service	using the
	a.	Write a sentence (a determines the pric					could use o	on its website to explain	ı how it
		<i>"We charge a</i> \$5.2	5 subscription	n fee plus 3	30 cents pe	r song."			
	b.	-		-				monthly cost in dollars. ded and the total mont	
		y = 5.25 + 0.30x							
	c.	Determine the cost	of download	ling 10 son	igs.				
		<b>5</b> .25 + 0.30(10) =	= \$8.25						



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