Lesson 18: Determining Surface Area of Three-Dimensional Figures

Student Outcomes

- Students determine that a right rectangular prism has six faces: top and bottom, front and back, and two sides. They determine that surface area is obtained by adding the areas of all the faces and develop the formula SA = 2lw + 2lh + 2wh.
- Students develop and apply the formula for the surface area of a cube as $SA = 6s^2$.

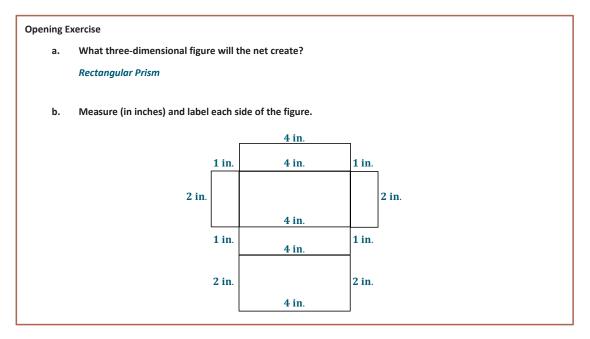
Lesson Notes

In order to complete this lesson, each student will need a ruler and the shape template that is attached to the lesson. To save time, teachers should have the shape template cut out for students.

Classwork

Opening Exercise (5 minutes)

In order to complete the Opening Exercise, each student needs a copy of the shape template that is already cut out.

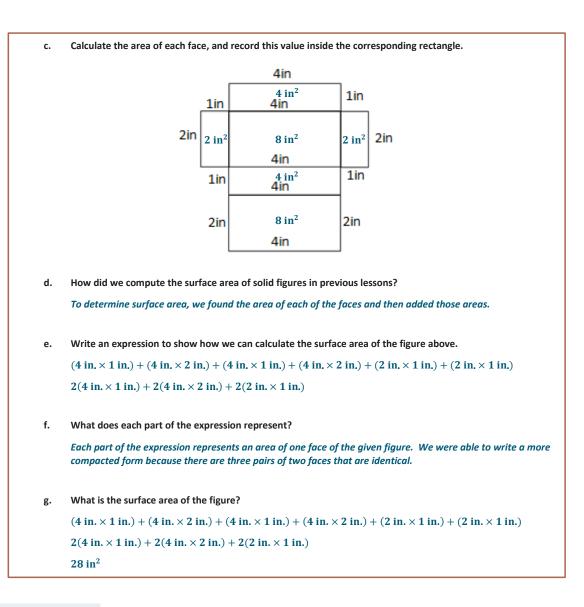




Determining Surface Area of Three-Dimensional Figures 2/5/15







Example 1 (8 minutes)

- Fold the net used in the Opening Exercise to make a rectangular prism. Have the two faces with the largest area be the bases of the prism.
- Fill in the second row of the table below.

Example 1

Fold the net used in the Opening Exercise to make a rectangular prism. Have the two faces with the largest area be the bases of the prism. Fill in the second row of the table below.

Area of Top (base)	Area of Bottom (base)	Area of Front	Area of Back	Area of Left Side	Area of Right Side
8 in ²	8 in ²	4 in ²	4 in ²	2 in ²	2 in ²



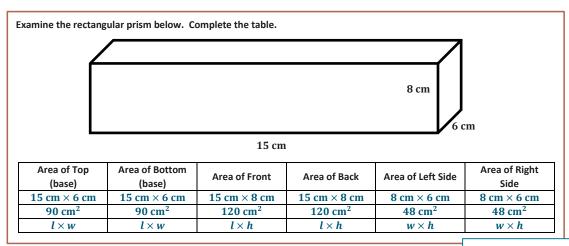
Lesson 18: Date: Determining Surface Area of Three-Dimensional Figures 2/5/15



- What do you notice about the areas of the faces?
 - Pairs of faces have equal areas.
- What is the relationship between the faces having equal area?
 - The faces that have the same area are across from each other. The bottom and top have the same area, the front and the back have the same area, and the two sides have the same area.
- How do we calculate the area of the two bases of the prism?
 - $length \times width$
- How do we calculate the area of the front and back faces of the prism?
 - $length \times height$
- How do we calculate the area of the right and left faces of the prism?
 - width \times height
- Using the name of the dimensions, fill in the third row of the table.

Area of Top (base)	Area of Bottom (base)	Area of Front	Area of Back	Area of Left Side	Area of Right Side
4 in. \times 2 in.	4 in. \times 2 in.	2 in. \times 2 in.	2 in. \times 2 in.	1 in. \times 2 in.	1 in. $ imes$ 2 in.
8 in ²	8 in ²	4 in ²	4 in ²	2 in ²	2 in ²
$l \times w$	$l \times w$	$l \times h$	$l \times h$	$w \times h$	$w \times h$

Examine the rectangular prism below. Complete the table.



When comparing the methods to finding surface area of the two rectangular prisms, can you develop a general formula?

> $SA = l \times w + l \times w + l \times h + l \times h + w \times h + w \times h$

Since we use the same expression to calculate the area of pairs of faces, we can use the distributive property to write an equivalent expression for the surface area of the figure that uses half as many terms.

Scaffolding:

Students may benefit from a poster or handout highlighting the length, width, and height of a three-dimensional figure. This poster may also include that l = length,

w = width, and h = height.



MP.8

Lesson 18: Date:

Determining Surface Area of Three-Dimensional Figures 2/5/15





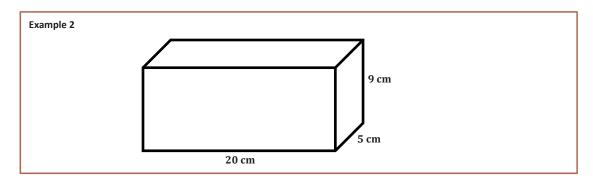
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- We have determined that there are two $l \times w$ dimensions. Let's record that as 2 times l times w, or simply $2(l \times w)$. How can we use this knowledge to alter other parts of the formula?
 - We also have two $l \times h$, so we can write that as $2(l \times h)$, and we can write the two $w \times h$ as $2(w \times h)$.
- Writing each pair in a simpler way, what is the formula to calculate the surface area of a rectangular prism? $SA = 2(l \times w) + 2(l \times h) + 2(w \times h)$
- Knowing the formula to calculate surface area makes it possible to calculate the surface area without a net.

Example 2 (5 minutes)

MP.8

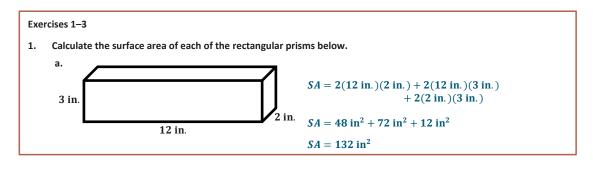
Work with students to calculate the surface area of the given rectangular prism.



- What are the dimensions of the rectangular prism?
 - The length is 20 cm, the width is 5 cm, and the height is 9 cm.
- We will use substitution in order to calculate the area. Substitute the given dimensions into the surface area formula.
 - ^o SA = 2(20 cm)(5 cm) + 2(20 cm)(9 cm) + 2(5 cm)(9 cm)
- Solve the equation. Remember to use order of operations.
 - $SA = 200 \text{ cm}^2 + 360 \text{ cm}^2 + 90 \text{ cm}^2$
 - $SA = 650 \text{ cm}^2$

Exercises 1–3 (17 minutes)

Students work individually to answer the following questions.





Determining Surface Area of Three-Dimensional Figures 2/5/15



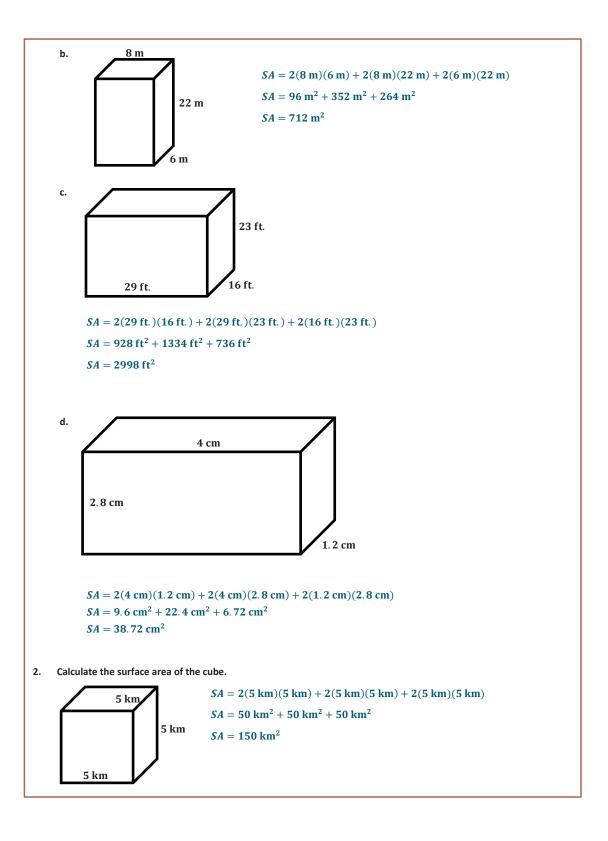
283

Lesson 18

6•5



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Lesson 18: Date: Determining Surface Area of Three-Dimensional Figures 2/5/15



	3. All the edges of a cube have the same length. Tony claims that the formula $SA = 6s^2$, where s is the length of each side of the cube, can be used to calculate the surface area of a cube.
	a. Use the dimensions from the cube in Problem 2 to determine if Tony's formula is correct.
	Tony's formula is correct because $SA = 6(5 \text{ km})^2 = 150 \text{ km}^2$, which is the same surface area when we use the surface area formula for rectangular prisms.
	b. Why does this formula work for cubes?
MP.3	Each face is a square, and to find the area of a square, you multiply the side lengths together. However, since the side lengths are the same, you can just square the side length. Also, a cube has 6 identical faces, so after calculating the area of one face, we can just multiply this area by 6 to determine the total surface area of the cube.
	c. Becca does not want to try to remember two formulas for surface area, so she is only going to remember the formula for a cube. Is this a good idea? Why or why not?
	Becca's idea is not a good idea. The surface area formula for cubes will only work for cubes because

Closing (5 minutes)

- Use two different ways to calculate the surface area of a cube with side lengths of 8 cm.
 - $SA = 2(8 \text{ cm} \times 8 \text{ cm}) + 2(8 \text{ cm} \times 8 \text{ cm}) + 2(8 \text{ cm} \times 8 \text{ cm})$
 - $SA = 128 \text{ cm}^2 + 128 \text{ cm}^2 + 128 \text{ cm}^2$

formula for rectangular prisms.

- $SA = 384 \text{ cm}^2$
- $SA = 6s^2$
 - $SA = 6(8 \text{ cm})^2$
 - $SA = 384 \text{ cm}^2$
- If you had to calculate the surface area of 20 different sized-cubes, which method would you prefer to use, and why?

rectangular prisms do not have 6 identical faces. Therefore, Becca also needs to know the surface area

Answers may vary, but most likely students will chose the formula for surface area of a cube because it is a shorter formula, so it would take less time.

Lesson Summary

Surface Area Formula for a Rectangular Prism: SA = 2lw + 2lh + 2wh

Surface Area Formula for a Cube: $SA = 6s^2$

Exit Ticket (5 minutes)







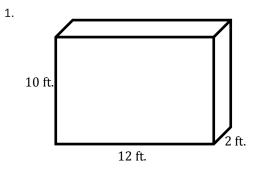
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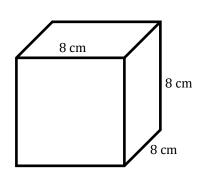
Lesson 18: Determining Surface Area of Three-Dimensional Figures

Exit Ticket

Calculate the surface area of each figure below. Figures are not drawn to scale.



2.





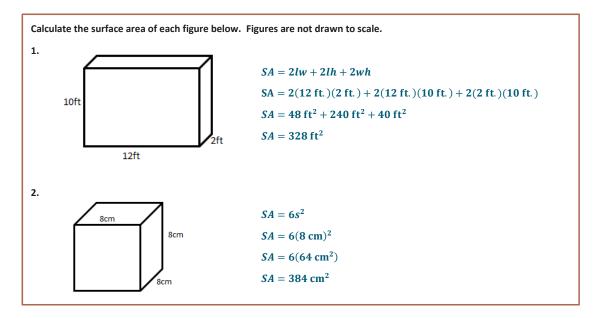
Lesson 18: Date: Determining Surface Area of Three-Dimensional Figures 2/5/15



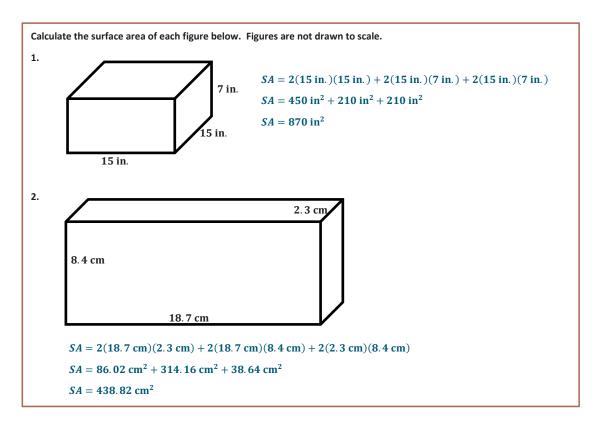
286



Exit Ticket Sample Solutions



Problem Set Sample Solutions





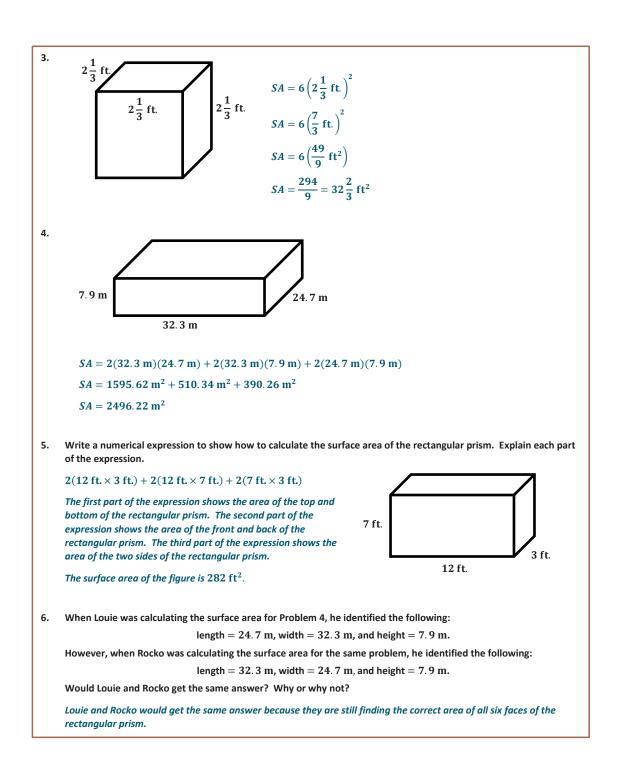
Lesson 18: Date: Determining Surface Area of Three-Dimensional Figures 2/5/15



287









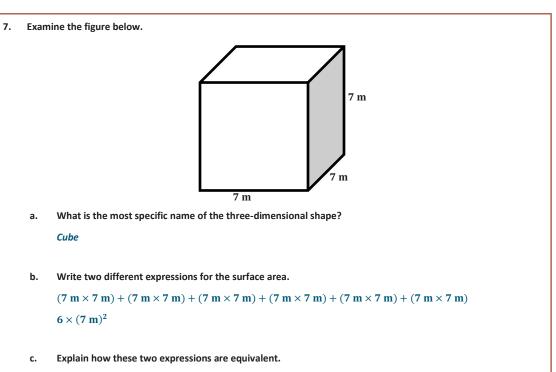
Lesson 18: Date: Determining Surface Area of Three-Dimensional Figures 2/5/15

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288



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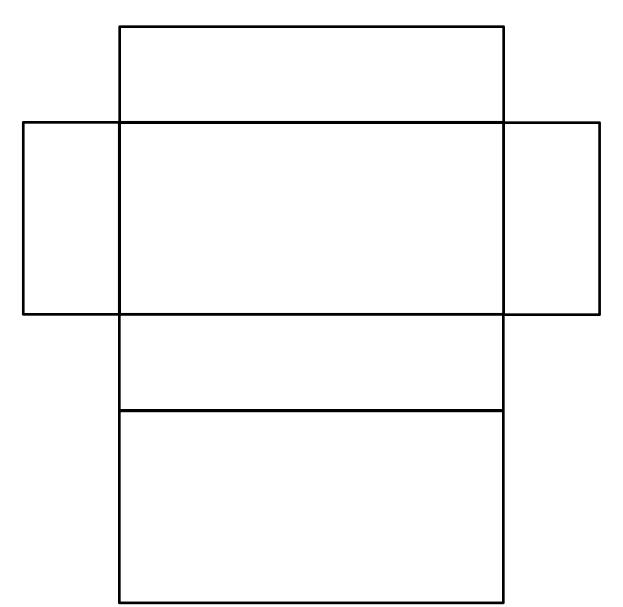
The two expressions are equivalent because the first expression shows $7 \text{ m} \times 7 \text{ m}$, which is equivalent to $(7 \text{ m})^2$. Also, the 6 represents the number of times the product $7 \text{ m} \times 7 \text{ m}$ is added together.





289







Determining Surface Area of Three-Dimensional Figures 2/5/15



