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## Lesson 4: The Relationship of Division and Subtraction

## Student Outcomes

- Students build and clarify the relationship of division and subtraction by determining that $12 \div x=4$ means $12-x-x-x-x=0$.


## Lesson Notes

Students will continue to use the squares from Lessons 1-3 to create tape diagrams. Each pair of students will need 30 squares to complete the activities.

## Classwork

## Discussion (20 minutes)

Provide each pair of students with a collection of 30 squares so they can use these squares to create tape diagrams throughout the lesson.

- Build a tape diagram that has 20 squares.

- Divide the tape diagram into 4 equal sections.

- How many squares are in each of the 4 sections?
- 5
- Write a number sentence to demonstrate what happened.

$$
\text { ㅁ } \quad 20 \div 4=5
$$

- Combine your squares again to have a tape diagram with 20 squares.

- Now, subtract 4 squares from your tape diagram.

- Write an expression to demonstrate what happened.
- 20-4
- Subtract 4 more squares, and alter your expression to represent the new tape diagram.

- Subtract 4 more squares, and alter your expression to represent the new tape diagram.
$\square$

- Subtract 4 more squares, and alter your expression to represent the new tape diagram.

- Last time, subtract 4 more squares, and alter your expression to an equation in order to represent a number sentence showing the complete transformation of the tape diagram.
- No squares should remain.
- $20-4-4-4-4-4=0$
- Let's take a look at the process we took to determine the difference to be zero.

Discuss the process step by step to determine that the number of times the divisor was subtracted from the dividend is the same number as the quotient.
$\left.\begin{array}{l}20-4=16 \\ 16-4=12 \\ 12-4=8 \\ 8-4=4 \\ 4-4=0\end{array}\right] \quad\left[\begin{array}{c} \\ \text { Subtracted } 5 \text { times. } \\ \text { Quotient is } 5 .\end{array}\right.$

- Do you recognize a relationship between $20 \div 4=5$ and $20-4-4-4-4-4=0$ ? If so, what is it?
- Possible answer: If you subtract the divisor from the dividend 5 times (the quotient), there will be no remaining squares.
- Let's take a look at a similar problem, $20 \div 5=4$, to see if the quotient is the number of times the divisor is subtracted from the dividend.
- Let's create a number sentence when we subtract the divisor.


$$
\text { व } 20-5-5-5-5=0
$$

Discuss the process to determine that the number of times the divisor is subtracted from the dividend is the same number as the quotient.


- Determine the relationship between $20 \div 5=4$ and

$$
\begin{aligned}
& 20-5-5-5-5=0 . \\
& \quad \quad 20 \div 5=4 \text { is equivalent to } 20-5-5-5-5=0 .
\end{aligned}
$$

- Is this relationship always true? Let's try to prove that it is.

Model the following set of tape diagrams with leading questions for discussion.

- $x$ is a number. What does $20 \div x=5$ mean?
- Exactly five $x$ 's can be subtracted from twenty.

$20-x-x-x-x-x$
- What must $x$ be in this division sentence?
- 4
- Let's keep taking $x$ away until we reach zero.

Model taking each $x$ away and creating subtraction expressions to record.

- Build a subtraction expression.

$$
\text { ㅁ } \quad 20-x-x-x-x-x=0
$$



- Is $20-4-4-4-4-4=0$ ?

> - Yes.

- Develop two equations using numbers and letters to show the relationship of division and subtraction.
- Possible answers: $20 \div x=5$ and

$$
20-x-x-x-x-x=0
$$

- Or $20 \div x=5$ means that 5 can be subtracted exactly $x$ number of times from 20. Is it true when $x=4$ ?
- To determine if $x=4$, let's keep taking $x$ away until we reach zero.

Model taking each $x$ away and creating subtraction expressions to record by following the diagram to the right.

- Build a subtraction equation.

$$
\text { ㅁ } \quad 20-5-5-5-5=0
$$

- What two operations are we relating in the problems we completed?
- Division and subtraction


## Exercise 1 ( 10 minutes)

Students work in pairs to answer the following questions.



## Exercise 2 ( 5 minutes)

## Exercise 2

Answer each question using what you have learned about the relationship of division and subtraction.
a. If $12 \div x=3$, how many times would $x$ have to be subtracted from 12 in order for the answer to be zero? What is the value of $x$ ?
$3 ; x=4$
b. $\quad 36-f-f-f-f=0$. Write a division sentence for this repeated subtraction sentence. What is the value of $f$ ?
$36 \div 4=f$ or $36 \div f=4 ; f=9$
c. If $24 \div b=12$, which number is being subtracted $\mathbf{1 2}$ times in order for the answer to be zero? Two

## Closing ( 5 minutes)

Display the graphic organizer provided at the end of the lesson. Copies of the organizer can be made for students to follow along and record.

- In each of the circles, we can place an operation to satisfy the organizer. In the last four lessons, we have discovered that each operation has a relationship with other operations, whether they are inverse operations or they are repeats of another.

Place the addition symbol in the upper left-hand circle.

- Let's start with addition. What is the inverse operation of addition?

- Subtraction

Place the subtraction symbol in the upper right-hand circle.

- After our discussion today, repeated subtraction can be represented by which operation?
- Division

Place the division symbol in the lower right-hand circle.

- Which operation is the inverse of division?
- Multiplication

Place the multiplication symbol in the lower left-hand circle.

- Let's see if this is correct. Is multiplication the repeat operation of
 addition?
- Yes

Understanding the relationships of operations is going to be instrumental when solving equations later in this unit.

## Exit Ticket (5 minutes)

Name $\qquad$ Date $\qquad$

## Lesson 4: The Relationship of Division and Subtraction

Exit Ticket

1. Represent $56 \div 8=7$ using subtraction. Explain your reasoning.
2. Explain why $30 \div x=6$ is the same as $30-x-x-x-x-x-x=0$. What is the value of $x$ in this example?

## Exit Ticket Sample Solutions

1. Represent $56 \div 8=7$ using subtraction. Explain your reasoning.

56-7-7-7-7-7-7-7-7=0 because
$56-7=49 ; 49-7=42 ; 42-7=35 ; 35-7=28 ; 28-7=21 ; 21-7=14 ; 14-7=7 ; 7-7=0$.
OR
$56-8-8-8-8-8-8-8=0$ because
$56-8=48 ; 48-8=40 ; 40-8=32 ; 32-8=24 ; 24-8=16 ; 16-8=8 ; 8-8=0$.
2. Explain why $30 \div x=6$ is the same as $30-x-x-x-x-x-x=0$. What is the value of $x$ in this example?
$30 \div 5=6$, so $x=5$. When I subtract 5 from 30 six times, the result is zero. Division is a repeat operation of subtraction.

## Problem Set Sample Solutions

| Build subtraction equations using the indicated equations. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Division <br> Equation | Divisor Indicates the Size of the Unit | Tape Diagram | What is $x, y, z$ ? |
| 1. | $24 \div x=4$ | $24-x-x-x-x=0$ | $24-x-x-x-x=0 ; x=6$ units in each group | $x=6$ |
| 2. | $36 \div x=6$ | $36-x-x-x-x-x-x=0$ |  | $x=6$ |
| 3. | $28 \div y=7$ | $28-y-y-y-y-y-y-y=0$ | $28-y-y-y-y-y-y-y=0 ; y=4$ units in each group | $y=4$ |
| 4. | $30 \div y=5$ | $30-y-y-y-y-y=0$ | $30-y-y-y-y-y=0 ; y=6$ units in each group | $y=6$ |
| 5. | $16 \div z=4$ | $16-z-z-z-z=0$ |  | $z=4$ |



## Graphic Organizer Reproducible


repeat
repeat


