

Student Outcomes

Students build and clarify the relationship of division and subtraction by determining that $12 \div x = 4$ means 12 - x - x - x - x = 0.

Lesson Notes

Students will continue to use the squares from Lessons 1–3 to create tape diagrams. Each pair of students will need 30 squares to complete the activities.

Classwork

Discussion (20 minutes)

Provide each pair of students with a collection of 30 squares so they can use these squares to create tape diagrams throughout the lesson.

•	Build a tape diagram that has 20 squares.		
•	Divide the tape diagram into 4 equal sections.		
•	How many squares are in each of the 4 sections?		
	° 5		
•	Write a number sentence to demonstrate what happened.		
	$20 \div 4 = 5$		
•	Combine your squares again to have a tape diagram with 20 squares.		
•	Now, subtract 4 squares from your tape diagram.		
	Write an expression to demonstrate what happened.		
	$\sim 20-4$		
•	Subtract 4 more squares, and alter your expression to represent the new tape diagram.		
	$\sim 20 - 4 - 4$		
•	Subtract 4 more squares, and alter your expression to represent the new tape diagram.		
	20 - 4 - 4 - 4		



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• Subtract 4 more squares, and alter your expression to represent the new tape diagram.

$$20 - 4 - 4 - 4 - 4$$

- Last time, subtract 4 more squares, and alter your expression to an equation in order to represent a number sentence showing the complete transformation of the tape diagram.
 - No squares should remain.
 - $\circ \quad 20 4 4 4 4 4 = 0$
- Let's take a look at the process we took to determine the difference to be zero.

Discuss the process step by step to determine that the number of times the divisor was subtracted from the dividend is the same number as the quotient.



- Do you recognize a relationship between $20 \div 4 = 5$ and 20 4 4 4 4 = 0? If so, what is it?
 - Possible answer: If you subtract the divisor from the dividend 5 times (the quotient), there will be no remaining squares.
- Let's take a look at a similar problem, 20 ÷ 5 = 4, to see if the quotient is the number of times the divisor is subtracted from the dividend.
- Let's create a number sentence when we subtract the divisor.

20 - 5 - 5 - 5 - 5 = 0

Discuss the process to determine that the number of times the divisor is subtracted from the dividend is the same number as the quotient.



- Determine the relationship between $20 \div 5 = 4$ and 20 5 5 5 5 = 0.
 - $20 \div 5 = 4$ is equivalent to 20 5 5 5 5 = 0.
- Is this relationship always true? Let's try to prove that it is.

Model the following set of tape diagrams with leading questions for discussion.

- *x* is a number. What does $20 \div x = 5$ mean?
 - Exactly five *x*'s can be subtracted from twenty.
 - What must *x* be in this division sentence?
 - 4

Let's keep taking x away until we reach zero.



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Lesson 4

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$$20 - x - x - x$$

$$20 - x - x - x - x$$



$$20-x-x-x-x-x$$



This work is licensed under a <u>Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License</u> Model taking each x away and creating subtraction expressions to record.

Build a subtraction expression.

^a
$$20 - x - x - x - x - x = 0$$

Is
$$20 - 4 - 4 - 4 - 4 - 4 = 0$$
?

Yes.

- Develop two equations using numbers and letters to show the relationship of division and subtraction.
 - Possible answers: $20 \div x = 5$ and 20 - x - x - x - x - x = 0
- Or $20 \div x = 5$ means that 5 can be subtracted exactly x number of times from 20. Is it true when x = 4?
- To determine if x = 4, let's keep taking x away until we reach zero.

Model taking each x away and creating subtraction expressions to record by following the diagram to the right.

Build a subtraction equation.

Exercise 1 (10 minutes)

- 20 5 5 5 5 = 0
- What two operations are we relating in the problems we completed?
 - Division and subtraction

Students work in pairs to answer the following questions.





20 - x - x - x - x = 0 or 20 - 5 - 5 - 5 - 5 = 0





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Division Equation	Divisor Indicates the Number of Units	Tape Diagram	What is <i>x</i> , <i>y</i> , <i>z</i> ?
$12 \div x = 4$	12 - 4 - 4 - 4 = 0	12 - 4 - 4 = 0; x = 3 groups	<i>x</i> = 3
$18 \div x = 3$	18 - 3 - 3 - 3 - 3 - 3 - 3 = 0	18 - 3 - 3 - 3 - 3 - 3 = 0; x = 6 groups	<i>x</i> = 6
$35 \div y = 5$	35 - 5 - 5 - 5 - 5 - 5 - 5 - 5 = 0	35 - 5 - 5 - 5 - 5 - 5 - 5 = 0; y = 7 groups	<i>y</i> = 7
$42\div z=6$	42-6-6-6-6-6-6=0	42-6-6-6-6-6-6=0;z=7 groups	<i>z</i> = 7

Exercise 2 (5 minutes)

Exercise 2			
Answer each question using what you have learned about the relationship of division and subtraction.			
a. If $12 \div x = 3$, how many times would x have to be subtracted from 12 in order for the answer to be What is the value of x?			
	3; <i>x</i> = 4		
b.	36 - f - f - f - f = 0. Write a division sentence for this repeated subtraction sentence. What is the value of f ?		
	$36 \div 4 = f \text{ or } 36 \div f = 4; f = 9$		
с.	If $24 \div b = 12$, which number is being subtracted 12 times in order for the answer to be zero?		
	Тwo		

Closing (5 minutes)

Display the graphic organizer provided at the end of the lesson. Copies of the organizer can be made for students to follow along and record.

 In each of the circles, we can place an operation to satisfy the organizer. In the last four lessons, we have discovered that each operation has a relationship with other operations, whether they are inverse operations or they are repeats of another.

Place the addition symbol in the upper left-hand circle.

- Let's start with addition. What is the inverse operation of addition?
 - Subtraction





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Place the subtraction symbol in the upper right-hand circle.

- After our discussion today, repeated subtraction can be represented by which operation?
 - Division

Place the division symbol in the lower right-hand circle.

- Which operation is the inverse of division?
 - Multiplication

Place the multiplication symbol in the lower left-hand circle.

- Let's see if this is correct. Is multiplication the repeat operation of addition?
 - Yes

Understanding the relationships of operations is going to be instrumental when solving equations later in this unit.

Exit Ticket (5 minutes)









Name _____

Date _____

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Exit Ticket

1. Represent $56 \div 8 = 7$ using subtraction. Explain your reasoning.

2. Explain why $30 \div x = 6$ is the same as 30 - x - x - x - x - x - x = 0. What is the value of x in this example?









Exit Ticket Sample Solutions

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Represent 56 ÷ 8 = 7 using subtraction. Explain your reasoning.
56 - 7 - 7 - 7 - 7 - 7 - 7 - 7 - 7 = 0 because
56 - 7 = 49; 49 - 7 = 42; 42 - 7 = 35; 35 - 7 = 28; 28 - 7 = 21; 21 - 7 = 14; 14 - 7 = 7; 7 - 7 = 0.
OR
56 - 8 - 8 - 8 - 8 - 8 - 8 - 8 = 0 because
56 - 8 = 48; 48 - 8 = 40; 40 - 8 = 32; 32 - 8 = 24; 24 - 8 = 16; 16 - 8 = 8; 8 - 8 = 0.
Explain why 30 ÷ x = 6 is the same as 30 - x - x - x - x - x = 0. What is the value of x in this example?
30 ÷ 5 = 6, so x = 5. When I subtract 5 from 30 six times, the result is zero. Division is a repeat operation of subtraction.
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Problem Set Sample Solutions

	Build subtraction equations using the indicated equations.				
	Division Equation	Divisor Indicates the Size of the Unit	Tape Diagram	What is <i>x</i> , <i>y</i> , <i>z</i> ?	
1.	$24 \div x = 4$	24-x-x-x-x=0	24 - x - x - x = 0; x = 6 units in each group	<i>x</i> = 6	
2.	$36 \div x = 6$	36-x-x-x-x-x=0	36-x-x-x-x-x=0;x=6 units in each group	<i>x</i> = 6	
3.	$28 \div y = 7$	28 - y - y - y - y - y - y - y = 0	28 - y - y - y - y - y - y = 0; y = 4 units in each group	<i>y</i> = 4	
4.	$30 \div y = 5$	30 - y - y - y - y - y = 0	30 - y - y - y - y = 0; y = 6 units in each group	<i>y</i> = 6	
5.	$16 \div z = 4$	16-z-z-z-z=0	16 - z - z - z = 0; z = 4 units in each group	<i>z</i> = 4	



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NYS COMMON CORE MATHEMATICS CURRICULUM



	Division Equation	Divisor Indicates the Number of Units	Tape Diagram	What is <i>x, y, z</i> ?
1.	$24 \div x = 4$	24 - 4 - 4 - 4 - 4 - 4 - 4 = 0	24-4-4-4-4-4=0; x = 6 groups	<i>x</i> = 6
2.	$36 \div x = 6$	36-6-6-6-6-6=0	36-6-6-6-6-6=0; x = 6 groups	<i>x</i> = 6
3.	$28 \div y = 7$	28 - 7 - 7 - 7 - 7 = 0	28 - 7 - 7 - 7 = 0; y = 4 groups	<i>y</i> = 4
4.	$30 \div y = 5$	30 - 5 - 5 - 5 - 5 - 5 - 5 = 0	30-5-5-5-5=0; y = 6 groups	<i>y</i> = 6
5.	$16 \div z = 4$	16 - 4 - 4 - 4 - 4 = 0	16 - 4 - 4 - 4 = 0; z = 4 groups	<i>z</i> = 4



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Graphic Organizer Reproducible





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