|  |
| --- |
|  |

Lesson 17: Divisibility Tests for 3 and 9

Student Outcomes

* Students apply divisibility rules, specifically for and , to understand factors and multiples.

Lesson Notes

Students already have knowledge on the divisibility rules of , , , , and . Although those rules are not a focus for this lesson, they are revisited throughout the lesson. Also, emphasize the difference between factors and multiples throughout the lesson.

Classwork

Opening Exercise (5 minutes)

The Opening Exercise will help students review the divisibility tests for the numbers , , , , and .

Opening Exercise

Below is a list of numbers. Place each number in the circle(s) that is a factor of the number. You will place some numbers in more than one circle. For example, if were on the list, you would place it in the circles with , , and because they are all factors of .

MP.1

; ; ; ; ; ; ; ; ;

**100000000**

**8**

; ;

**5**

**4**

**2**

Discussion (8 minutes)

Discuss students’ results from the opening exercise. Students can either share their answers, or the teacher can conduct a poll (raising hands, standing up, electronically) to determine where students placed each number.

After sharing which numbers go in each circle, have students examine the numbers in the opening activity. Ask students to find shortcuts to determine in which group the number belongs just by looking at it.

**MP.3**

Ask students to share their short cuts or rules and discuss the divisibility rules for each number. Have students take notes in their handbooks.

Discussion

* Divisibility rule for : **If and only if its unit digit is , ,, , or.**

**MP.8**

* Divisibility rule for : **If and only if its last two digits are a number divisible by .**
* Divisibility rule for : **If and only if its unit digit is or .**
* Divisibility rule for : **If and only if its last three digits are a number divisible by .**
* Divisibility rule for : **If and only if its unit digit is .**
* Decimal numbers with fraction parts do not follow the divisibility tests.

Explain that students will learn two new divisibility rules today. The rules will be used to determine if numbers are divisible by or. Start with a number students already know have factors of and , so they can see that the rule works.

* What do the numbers ,, ,, and all have in common?
	+ *They are divisible by .*
* Calculate the sum of the digits for each given number. For example, the sum of the digits in the number is because .

Provide time for students to find the sums. Record sums on the board.

* What do all these sums have in common?
	+ *They are divisible by .*
* When the sum of a number’s digits is divisible by , the entire number is divisible by . Now let’s examine a different set of numbers: and . What do these numbers have in common?
	+ *They are divisible by .*
* Calculate the sum of the digits for each given number.

Provide time for students to find the sums. Record sums on the board.

* What do all the sums have in common?
	+ *They are divisible by .*
* When the sum of the digits is divisible by and , the entire number is divisible by . Let’s try to use this knowledge to determine if a large number is divisible by , , or both. The number is divisible by both and . (Show students on the calculator.) Find the sum of the digits.
* Are and both factors of ?
	+ *Yes.*
* Calculating the sum of a number’s digits helps us to determine if the number is divisible by or or both.

Introduce the divisibility rules for and . Have students record the rules in their handbooks.

* Divisibility rule for :  **If the sum of the digits is divisible by , then the number is divisible by .**
* Divisibility rule for : **If the sum of the digits is divisible by , then the number is divisible by .**

Through further discussion, explain to students that if a number is divisible by , it is also divisible by , but if a number is divisible by , it is not necessarily divisible by .

* Because , any number that is divisible by will also be divisible by .

Example 1 (5 minutes)

Example 1

*Scaffolding:*

* If needed, the teacher can also ask if is divisible by . Students may still struggle with the connection between the multiples of and .
* If students struggled with the opening exercise, the divisibility rules for , ,, , and can be reviewed in this example as well.

This example will show you how to apply the two new divisibility rules we just discussed.

Is divisible by or ? Why or why not?

* 1. What are the three digits in the number ?

, ,and

* 1. What is the sum of the three digits?

; the sum of the three digits is .

* 1. Is divisible by ?

Yes.

* 1. Is the entire number divisible by ? Why or why not?

The number is divisible by because the sum of the digits is divisible by .

This may be the place to help students recognize the difference between factors and multiples. Nine is a factor of because it is the product of and ; therefore, is a multiple of .

**MP.7**

* 1. Is the number divisible by ? Why or why not?

Three is a factor of because if is a factor of , then will also be a factor. OR

The number is divisible by because the sum of the digits is divisible by .

Example 2 (5 minutes)

The students have now seen one example of the two new divisibility rules. Allow students to work with a partner to decide whether a given number is divisible by and . If a majority of students are still struggling, the teacher may ask the same leading questions found in Example 1.

* Is divisible by or ? Why or why not?

Encourage students to check first because if is a factor, then students know that is also a factor. If is not divisible by , then students must check to see if is divisible by .

Example 2

Is divisible by or ? Why or why not?

The number is divisible by , but not by because the sum of the digits is , and is divisible by , but not by .

This is another opportunity to emphasize the difference between factors and multiples. Three is a factor of because the product of and is ; therefore, is a multiple of .

**MP.7**

Exercises 1–5 (13 minutes)

Students may work with partners or individually to complete the exercises. Remind students that they may circle more than one answer.

**MP.8**

Exercises 1–5

Circle ALL the numbers that are factors of the given number. Complete any necessary work in the space provided.

1. Is divisible by

Explain your reasoning for your choices.

The number is divisible by because is a factor of . I know this because the sum of the digits is , which is divisible by . The number is not divisible by because is not divisible by , and is not divisible by because the last two digits () are not divisible by .

1. Is divisible by

Explain your reasoning for your choices.

***The number is divisible by and because both and are factors of . I know this because the sum of the digits is , and is divisible by both and . The number is also divisible by because the unit digit is a .***

1. Is divisible by

Explain your reasoning for your choices.

The number is divisible by , but not , because is a factor of , but is not. I know this because the sum of the digits is , which is divisible by , but not . The number is not divisible by because it does not end with ,,,,or .

1. Is divisible by

Explain your reasoning for your choices.

The number is divisible by and because and are factors of . I know this because the sum of the digits is , which is divisible by and . The number is also divisible by because is a factor of . I know this because the unit digit is .

1. Is divisible by

Explain your reasoning for your choices.

The number is divisible by , but not divisible by , because is a factor of , but is not. I know this because the sum of the digits is , which is divisible by but not divisible by . The number is divisible by because the last three digits () is divisible by .

Closing (4 minutes)

* Without completing the division, how can you determine if a number is divisible by ?
	+ *Calculate the sum of the digits; if the sum of the digits is divisible by , the entire number is divisible by .*
* If a number is divisible by , will it be divisible by ? Explain your answer.
	+ *If a number is divisible by , the sum of the digits will be divisible by . Any number that is divisible by is also divisible by since .*
* If a number is divisible by , will it be divisible by ? Explain your answer.
	+ *If a number is divisible by , it may not be divisible by because has more multiples than .*

Lesson Summary

To determine if a number is divisible by or :

* Calculate the sum of the digits.
* If the sum of the digits is divisible by , the entire number is divisible by .
* If the sum of the digits is divisible by , the entire number is divisible by .

Note: If a number is divisible by , the number is also divisible by .

Exit Ticket (5 minutes)

Name \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ Date\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Lesson 17: Divisibility Tests for 3 and 9

Exit Ticket

1. Is divisible by ? If it is, write the number as the product of and another factor. If not, explain.
2. Is divisible by ? If it is, write the number as the product of and another factor. If not, explain.
3. Explain why is divisible by both and .

Exit Ticket Sample Solutions

1. Is divisible by ? If it is, write the number as the product of and another factor. If not, explain.

***The number is not divisible by because the sum of the digits is , which is not divisible by .***

1. Is divisible by ? If it is, write the number as the product of and another factor. If not, explain.

***The number is divisible by because the sum of the digits is , which is divisible by . Nine is a factor of because .***

1. Explain why is divisible by both and .

The number is divisible by both and because the sum of the digits is , which is divisible by both and .

Problem Set Sample Solutions

1. Is divisible by both and ? Why or why not?

The number is divisible by both and because the sum of the digits is , which is divisible by and .

1. Circle all the factors of from the list below.

1. Circle all the factors of from the list below.

1. Write a digit number that is divisible by both and . Explain how you know this number is divisible by and .

Answers will vary. Possible student response: The sum of the digits is divisible by , and that’s how I know the number is divisible by . The last digits are divisible by , so the entire number is divisible by .

1. Write a digit number that is divisible by both and . Explain how you know this number is divisible by and .

Answers will vary. Possible student response: The number ends with a or , so the entire number is divisible by . The sum of the digits is divisible by , so the entire number is divisible by .