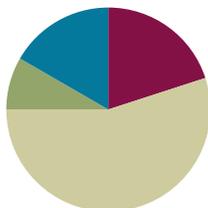


## Lesson 15

**Objective:** Understand and solve division problems with a remainder using the array and area models.

### Suggested Lesson Structure

|                       |                     |
|-----------------------|---------------------|
| ■ Fluency Practice    | (12 minutes)        |
| ■ Application Problem | (5 minutes)         |
| ■ Concept Development | (33 minutes)        |
| ■ Student Debrief     | (10 minutes)        |
| <b>Total Time</b>     | <b>(60 minutes)</b> |



### Fluency Practice (12 minutes)

- Show Values with Place Value Disks **4.NBT.1** (4 minutes)
- Divide with Remainders **4.NBT.6** (4 minutes)
- Number Sentences in an Array **4.NBT.** (4 minutes)

### Show Values with Place Value Disks (4 minutes)

Materials: (T) Thousands place value chart (Lesson 4 Template) (S) Personal white board, thousands place value chart (Lesson 4 Template)

Note: This fluency activity prepares students for Lesson 16's Concept Development.

T: (Project the place value chart with 2 tens disks and 4 ones disks.) On your personal white boards, write the number in standard form.

S: (Write 24.)

Repeat process for 5 tens and 3 ones; 4 tens and 1 one; 3 tens and 11 ones; and 3 tens and 17 ones.

T: (Write 32.) Say the number.

S: 32.

T: Show 32 using place value disks.

S: (Draw disks for 3 tens and 2 ones.)

Continue with the following possible sequence: 21 and 43.

**Divide with Remainders (4 minutes)**

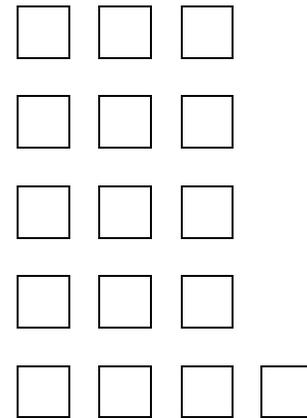
Note: This fluency activity provides maintenance of the fluency introduced in Lesson 14.

Repeat the process from Lesson 14 for the following possible sequence:  $6 \div 2$  and  $7 \div 2$ ;  $24 \div 3$  and  $25 \div 3$ ,  $12 \div 4$  and  $15 \div 4$ ,  $18 \div 6$  and  $21 \div 6$ , and  $45 \div 5$  and  $49 \div 5$ .

**Number Sentences in an Array (4 minutes)**

Materials: (S) Personal white board

Note: This fluency activity prepares students for this lesson’s Concept Development.



T: (Project a  $5 \times 3 + 1$  array.) How many boxes do you see altogether?

S: 16.

T: Let’s count by fives to check. (Point at columns as students count.)

S: 5, 10, 15.

T: Plus 1? (Point to the extra square outside of the rectangle.)

S: 16.

T: Count by threes to check.

S: 3, 6, 9, 12, 15.

T: Plus 1? (Point to the extra square outside of the rectangle.)

S: 16.

T: On your personal white boards, write two multiplication number sentences to show how many boxes are in this array.

S: (Write  $(5 \times 3) + 1 = 16$  and  $(3 \times 5) + 1 = 16$ .)

T: Write two division sentences for this array.

S: (Write  $16 \div 3 = 5$  with a remainder of 1 and  $16 \div 5 = 3$  with a remainder of 1.)

Repeat using the following possible sequence:  $(3 \times 6) + 1$  and  $(3 \times 4) + 2$ .

**Application Problem (5 minutes)**

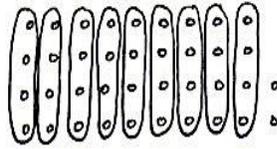
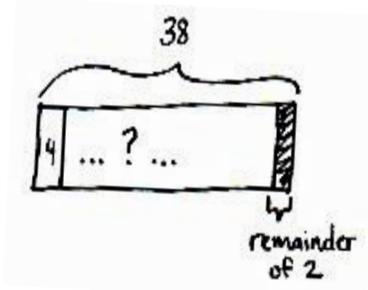
Chandra printed 38 photos to put into her scrapbook. If she can fit 4 photos on each page, how many pages will she use for her photos?

Note: This Application Problem relates to the objective of Lesson 14 in that students solve a division word problem with a remainder. Here, students interpret the remainder to determine the total number of scrapbook pages needed. This anticipates the last problem in this lesson.



**NOTES ON MULTIPLE MEANS OF REPRESENTATION:**

Modeling the array (rather than the tape diagram) may give students a clearer picture of the solution to the Application Problem. Encourage students to use the labels *photo* and *page*, if beneficial. Discuss how the equation informs the solution yet the picture reveals the solution.



$$38 \div 4 \quad 9 \times 4 = 36$$

$$Q = 9 \quad 36 + 2 = 38$$

$$R = 2$$

Chandra will need 10 pages because 9 pages only fits 36 photos, so the 10<sup>th</sup> page will fit the remaining 2 photos.

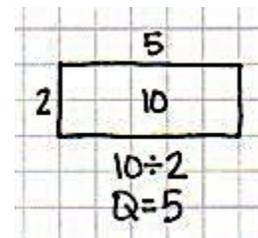
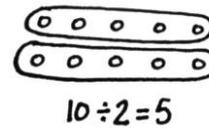
**Concept Development (33 minutes)**

Materials: (T/S) Square grid paper

**Problem 1: Solve a division problem with and without a remainder using the area model.**

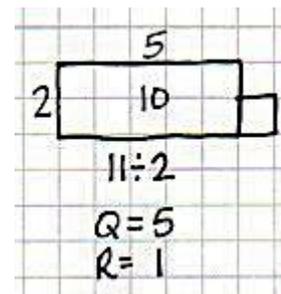
Display  $10 \div 2$ .

- T: Draw an array to represent  $10 \div 2$ . Explain to your partner how you solved.
- S: (Draw.) I drew 2 circles and placed 10 dots evenly among the circles. → I drew 10 dots as 2 rows of 5 dots.
- T: Let's use grid paper to draw a rectangle with an area of 10 square centimeters and one side length of 2 centimeters. Tell your partner how we can find the unknown side length.
- S: The area is 10, so we know it is 5. → If the width is 2 centimeters, that means the length is 5 centimeters, and 2 centimeters times 5 centimeters gives an area of 10 square centimeters. → We can count and mark off by twos until we get to 10.
- T: Discuss with your partner how the length of 5 centimeters is represented in the area model.
- S: The length is 5, and the quotient is 5. → The length of the area model represents the quotient of this division problem.



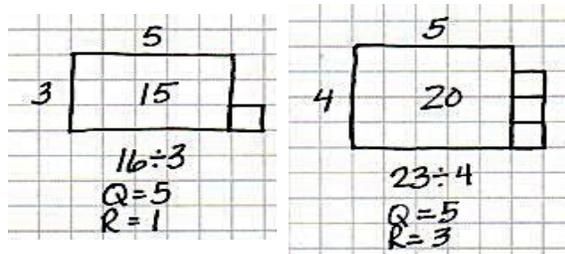
Display  $11 \div 2$ .

- T: With your partner, discuss how you would draw an area model for  $11 \div 2$ .
- S: Two can be the length or the width. → I can't just draw 2 rows of square units because of the remainder. → If I mark off 2 squares at a time, I count 2, 4, 6, 8, 10. I can't do another group of 2 because it would be 12. There aren't enough.
- T: Eleven square centimeters is the total area. Let's draw a rectangle starting with a width of 2 centimeters. We'll continue lengthening it until we get as close to 11 square centimeters as we can.



- S: A length of 5 centimeters and width of 2 centimeters is as close as we can get to 11 square centimeters. → We can't do  $2 \times 6$  because that's 12 square centimeters and the total area is 11 square centimeters.
- T: We can show a total area of 11 square centimeters by modeling 1 more square centimeter. The remainder of 1 represents 1 more square centimeter.

Repeat for  $16 \div 3$  and  $23 \div 4$ .

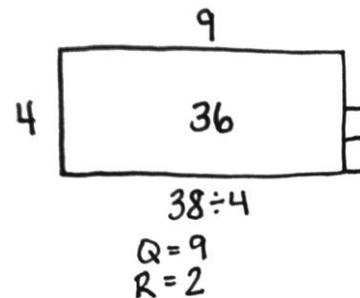
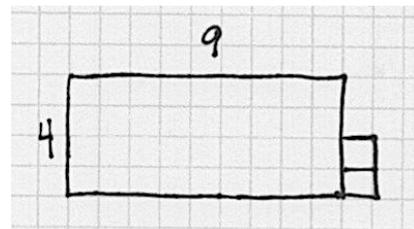
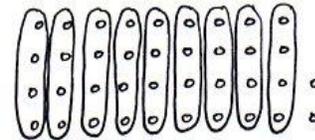


**Problem 2: Solve a division problem using an array and the area model.**

Display  $38 \div 4$

MP.4

- T: In the Application Problem, you drew an array (pictured to the right) to solve. Represent the same problem using the area model on grid paper. (Allow two minutes to work.)
- T: What do you notice about the array compared to the area model on graph paper?
- S: The area model is faster to draw. Thirty-eight dots is a lot to draw. → There are the same number of dots and squares when I used graph paper. → Both get us the same answer of a quotient 9 with a remainder of 2.
- T: Let's represent  $38 \div 4$  even more efficiently without grid paper since it's hard to come by grid paper every time you want to solve a problem.
- T: (Give students one minute to draw.) Talk to your partner about how the array model and grid paper model supported you in drawing the rectangle with a given structure.
- S: I knew the length was a little more than twice the width. → I knew that the remainder was half a column. → I knew that there was a remainder. It was really obvious with the array and grid paper.



**Problem Set (10 minutes)**

Students should do their personal best to complete the Problem Set within the allotted 10 minutes. For some classes, it may be appropriate to modify the assignment by specifying which problems they work on first. Some problems do not specify a method for solving. Students should solve these problems using the RDW approach used for Application Problems.

**Student Debrief (10 minutes)**

**Lesson Objective:** Understand and solve division problems with a remainder using the array and area models.

The Student Debrief is intended to invite reflection and active processing of the total lesson experience.

Invite students to review their solutions for the Problem Set. They should check work by comparing answers with a partner before going over answers as a class. Look for misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a conversation to debrief the Problem Set and process the lesson.

You may choose to use any combination of the questions below to lead the discussion.

- What does the quotient represent in the area model?
- When does the area model present a challenge in representing division problems?
- Explain to your partner how Problem 1, Parts (a) and (b) are similar. How are they different?
- How can Problem 3 and Problem 4 have the same remainder?
- How could you change the 43 in Problem 5 so that there would be the same quotient but with no remainder?
- The quotient represents a side length. The remainder consists of square units. Why?
- How is the whole represented in an area model?
- What new math vocabulary did we use today to communicate precisely?
- How did the Application Problem connect to today’s lesson?

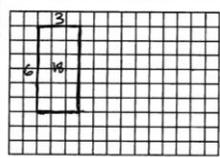
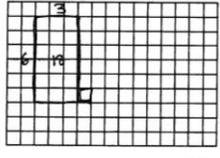


**NOTES ON MULTIPLE MEANS OF REPRESENTATION:**

Help English language learners distinguish between terms used for division: *division*, *divisor*, *quotient*, and *whole*. Label a division equation and post for future reference. Make a word web of synonyms for division that students can interchange, if desired. Encourage students to speak these words as they participate in the Debrief.

Lesson 15 Problem Set 4•3

Name: Jack Date: \_\_\_\_\_

| Show division using an array.  | Show division using an area model.  |
|--|---|
| <p>1. <math>18 \div 6</math></p>  <p>Quotient = <u>3</u><br/>Remainder = <u>0</u></p>  |  <p>Can you show <math>18 \div 6</math> with one rectangle? <u>yes</u></p>  |
| <p>2. <math>19 \div 6</math></p>  <p>Quotient = <u>3</u><br/>Remainder = <u>1</u></p> |  <p>Can you show <math>19 \div 6</math> with one rectangle? <u>no</u><br/>Explain how you showed the remainder:<br/>I outlined one more square unit.</p> |

COMMON CORE Lesson 15: Understand and solve division problems with a remainder using the array and area models. Date: 8/22/13 engage<sup>ny</sup> 3.E.22

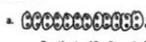
**Exit Ticket (3 minutes)**

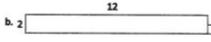
After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help you assess the students’ understanding of the concepts that were presented in the lesson today and plan more effectively for future lessons. You may read the questions aloud to the students.

Lesson 15 Problem Set 4•3

Solve using an array and an area model. The first one is done for you.

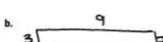
Example:  $25 \div 2$

a.   
Quotient = 12 Remainder = 1

b. 

3.  $29 \div 3$

a.   
Quotient = 9 Remainder = 2

b. 

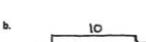
4.  $22 \div 5$

a.   
Quotient = 4 Remainder = 2

b. 

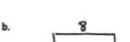
5.  $43 \div 4$

a.   
Quotient = 10 Remainder = 3

b. 

6.  $59 \div 7$

a.   
Quotient = 8 Remainder = 3

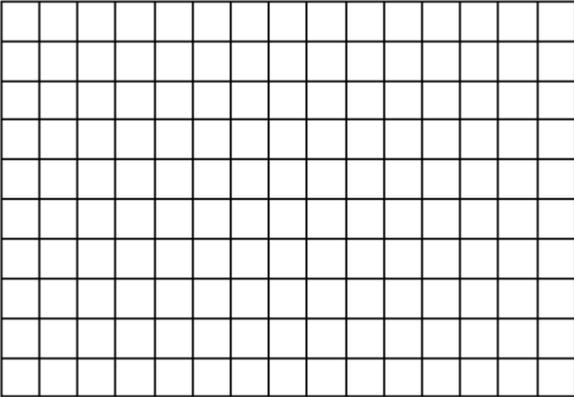
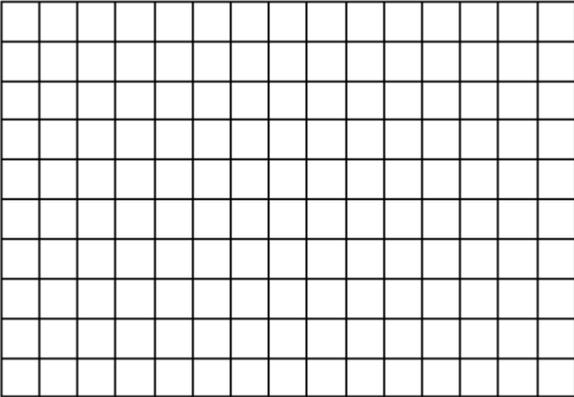
b. 

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Name \_\_\_\_\_

Date \_\_\_\_\_

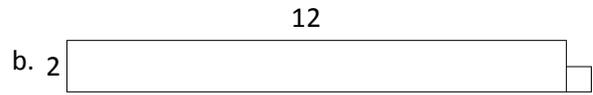
| Show division using an array.  | Show division using an area model.   |
|--|--|
| <p>1. <math>18 \div 6</math></p><br><br><br><br><br><br><br><p>Quotient = _____</p> <p>Remainder = _____</p> |  <p>Can you show <math>18 \div 6</math> with one rectangle? _____</p>  |
| <p>2. <math>19 \div 6</math></p><br><br><br><br><br><br><br><p>Quotient = _____</p> <p>Remainder = _____</p> |  <p>Can you show <math>19 \div 6</math> with one rectangle? _____</p> <p>Explain how you showed the remainder:</p> |

Solve using an array and an area model. The first one is done for you.

Example:  $25 \div 2$



Quotient = 12    Remainder = 1



3.  $29 \div 3$

a.

b.

4.  $22 \div 5$

a.

b.

5.  $43 \div 4$

a.

b.

6.  $59 \div 7$

a.

b.

Name \_\_\_\_\_

Date \_\_\_\_\_

Solve using an array and area model.

1.  $27 \div 5$

a.

b.

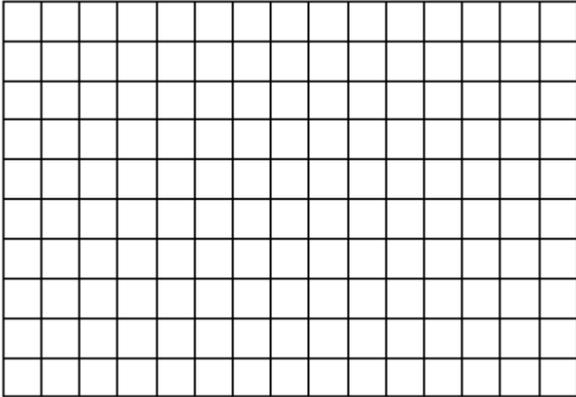
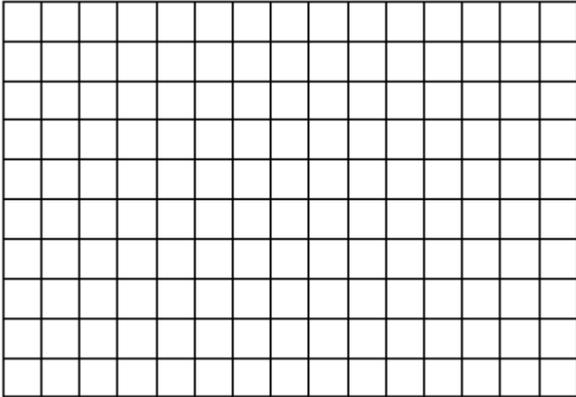
2.  $32 \div 6$

a.

b.

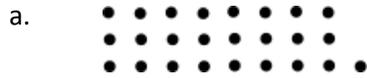
Name \_\_\_\_\_

Date \_\_\_\_\_

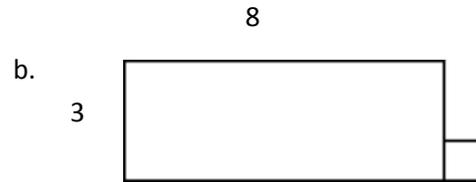
| Show division using an array.  | Show division using an area model.   |
|--|--|
| <p>1. <math>24 \div 4</math></p><br><br><br><br><br><br><br><p>Quotient = _____</p> <p>Remainder = _____</p> |  <p>Can you show <math>24 \div 4</math> with one rectangle? _____</p>  |
| <p>2. <math>25 \div 4</math></p><br><br><br><br><br><br><br><p>Quotient = _____</p> <p>Remainder = _____</p> |  <p>Can you show <math>25 \div 4</math> with one rectangle? _____</p> <p>Explain how you showed the remainder:</p> |

Solve using an array and area model. The first one is done for you.

Example:  $25 \div 3$



Quotient = 8    Remainder = 1



3.  $44 \div 7$

a.

b.

4.  $34 \div 6$

a.

b.

5.  $37 \div 6$

a.

b.

6.  $46 \div 8$

a.

b.