Lesson 6: Probability Distribution of a Discrete Random  
Variable

Classwork

Exercises 1–3: Credit Cards

Credit bureau data from a random sample of adults indicating the number of credit cards is summarized in the table below.

Table 1: Number of credit cards carried by adults

|  |  |
| --- | --- |
| Number of Credit Cards | Relative Frequency |
|  |  |
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1. Consider the chance experiment of selecting an adult at random from the sample. The number of credit cards is a discrete random variable. The table above sets up the probability distribution of this variable as a relative frequency. Make a histogram of the probability distribution of the number of credit cards per person based on the relative frequencies.
2. Answer the following questions based on the probability distribution.
   1. Describe the distribution.
   2. Is a randomly selected adult more likely to have credit cards or or more credit cards?
   3. Find the area of the bar representing credit cards.
   4. What is the area of all of the bars in the histogram? Explain your reasoning.
3. Suppose you asked each person in a random sample of people how many credit cards he or she has. Would the following surprise you? Explain why or why not in each case.
   1. Everyone in the sample owned at least one credit card.
   2. people had credit cards.
   3. people had at least credit cards.
   4. people had more than credit cards.

Exercises 4–7: Male and Female Pups

1. The probability that certain animals will give birth to a male or a female is generally estimated to be equal, or approximately . This estimate, however, is not always the case. Data are used to estimate the probability that the offspring of certain animals will be a male or a female. Scientists are particularly interested about the probability that an offspring will be a male or a female for animals that are at a high risk of survival. In a certain species of seals, two females are born for every male. The typical litter size for this species of seals is six pups.
   1. What are some statistical questions you might want to consider about these seals?
   2. What is the probability that a pup will be a female? A male? Explain your answer.
   3. Assuming that births are independent, which of the following can be used to find the probability that the first two pups born in a litter will be male? Explain your reasoning.
2. The probability distribution for the number of males in a litter of six pups is given below.

Table 2: Probability distribution of number of male pups per litter\*

|  |  |
| --- | --- |
| Number of male pups | Probability |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

\*The sum of the probabilities in the table is not equal to due to rounding.

Use the probability distribution to answer the following questions.

* 1. How many male pups will typically be in a litter?
  2. Is a litter more likely to have six male pups or no male pups?

1. Based on the probability distribution of the number of male pups in a litter of six given above, indicate whether you would be surprised in each of the situations. Explain why or why not.
   1. In every one of a female’s five litters of pups, there were fewer males than females.
   2. A female had only one male in two litters of pups.
   3. A female had two litters of pups that were all males.
   4. In a certain region of the world, scientists found that in litters born to different females, of them had four male pups.
2. How would the probability distribution change if the focus was the number of females rather than the number of males?

Lesson Summary

The probability distribution of a discrete random variable in table or graphical form describes the long-run behavior of a random variable.

Problem Set

1. Which of the following could be graphs of a probability distribution? Explain your reasoning in each case.

|  |  |
| --- | --- |
| a. | b. |
| c. | d. |

1. Consider randomly selecting a student from New York City schools and recording the value of the random variable number of languages in which the student can carry on a conversation. A random sample of students produced the following data.

Table 3: Number of languages spoken by random sample of students in New York City

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| Number of languages |  |  |  |  |  |  |  |
| Number of students |  |  |  |  |  |  |  |

* 1. Create a probability distribution of the relative frequencies of the number of languages students can use to carry on a conversation.
  2. If you took a random sample of students, would it be likely that of them only spoke one language? Why or why not?
  3. If you took a random sample of students, would you be surprised if of them spoke exactly languages? Why or why not?
  4. Would you be surprised if students spoke at least two languages? Why or why not?

1. Suppose someone created a special six-sided die. The probability distribution for the number of spots on the top face when the die is rolled is given in the table.

Table 5: Probability distribution of the top face when rolling a die

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Face | 1 | 2 | 3 | 4 | 5 | 6 |
| Probability |  |  |  |  |  |  |

* 1. If is an integer, what does have to be in order for this to be a valid probability distribution?
  2. Find the probability of getting a .
  3. What is the probability of rolling an even number?

1. The graph shows the relative frequencies of the number of pets for households in a particular community.



* 1. If a household in the community is selected at random, what is the probability that a household would have at least pet?
  2. Do you think it would be likely to have households with pets in a random sample of households? Why or why not?
  3. Suppose the results of a survey of households in a section of a city found of them did not have any pets. What comments might you make?