Lesson 6: Unknown Angle Problems with Inscribed Angles in Circles

Classwork

Opening Exercise

In a circle, a chord and a diameter are extended outside of the circle to meet at point . If , and , find



Let

In Reason

 Reason

 Reason

In Reason

 Reason

Exercises 1–4

Find the value in each figure below, and describe how you arrived at the answer.

|  |  |
| --- | --- |
| 1. Hint: Thales’ theorem
 | 1.
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| 1.
 | 1.
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Lesson Summary:

**Theorems:**

* **The inscribed angle theorem**: The measure of a central angle is twice the measure of any inscribed angle that intercepts the same arc as the central angle
* **Consequence of inscribed angle theorem**: Inscribed angles that intercept the same arc are equal in measure.
* If , , , and are four points with and on the same side of line , and angles and are congruent, then , , , and all lie on the same circle.

 **Relevant Vocabulary**

* Central angle: A *central angle* of a circle is an angle whose vertex is the center of a circle.
* Inscribed angle: An *inscribed* *angle* is an angle whose vertex is on a circle, and each side of the angle intersects the circle in another point.
* Intercepted arc: An angle *intercepts* an arc if the endpoints of the arc lie on the angle, all other points of the arc are in the interior of the angle, and each side of the angle contains an endpoint of the arc. An angle inscribed in a circle intercepts exactly one arc, in particular, the arc intercepted by a right angle is the semicircle in the interior of the angle.

Problem Set

In Problems 1–5, find the value .











1. If , express in terms of .



* 1. Find the value .



* 1. Suppose the . Prove that .
1. In the figure below, three identical circles meet at , and , E respectively. . , , and , , lie on straight lines.

Prove is a parallelogram.



**Proof**:



Join and .

 Reason: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

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 Alternate angles are equal.

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 Corresponding angles are equal.

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 Corresponding angles are equal.

 is a parallelogram.