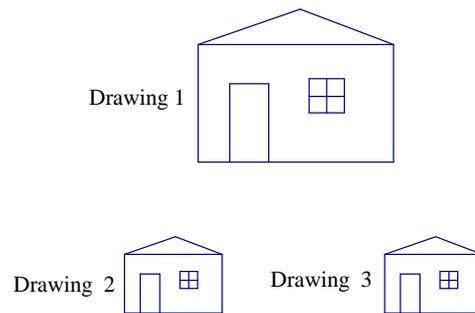


Lesson 11: Dilations from Different Centers

Classwork

Exploratory Challenge 1

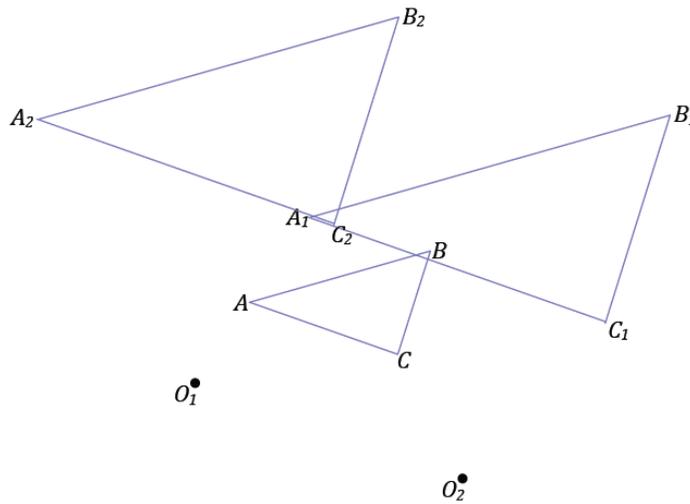
Drawing 2 and Drawing 3 are both scale drawings of Drawing 1.



- Determine the scale factor and center for each scale drawing. Take measurements as needed.
- Is there a way to map Drawing 2 onto Drawing 3 or map Drawing 3 onto Drawing 2?
- Generalize the parameters of this example and its results.

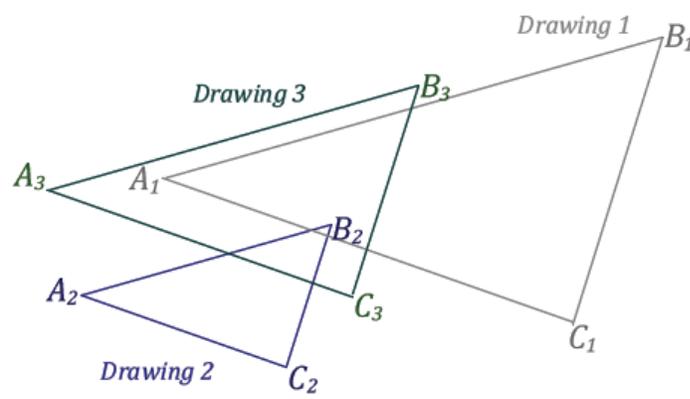
Exercise 1

Triangle ABC has been dilated with scale factor $\frac{1}{2}$ from centers O_1 and O_2 . What can you say about line segments A_1A_2 , B_1B_2 , C_1C_2 ?



Exploratory Challenge 2

If Drawing 2 is a scale drawing of Drawing 1 with scale factor r_1 , and Drawing 3 is a scale drawing of Drawing 2 with scale factor r_2 , what is the relationship between Drawing 3 and Drawing 1?



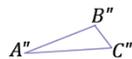
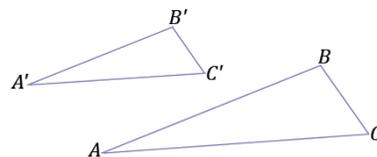
- a. Determine the scale factor and center for each scale drawing. Take measurements as needed.

- b. What is the scale factor going from Drawing 1 to Drawing 3? Take measurements as needed.
- c. Compare the centers of dilations of Drawing 1 (to Drawing 2) and of Drawing 2 (to Drawing 3). What do you notice about these centers relative to the center of the composition of dilations O_3 ?
- d. Generalize the parameters of this example and its results.

Exercise 2

Triangle ABC has been dilated with scale factor $\frac{2}{3}$ from center O_1 to get triangle $A'B'C'$, and then triangle $A'B'C'$ is dilated from center O_2 with scale factor $\frac{1}{2}$ to get triangle $A''B''C''$. Describe the dilation that maps triangle ABC to triangle $A''B''C''$. Find the center and scale factor for that dilation.

O_1 •



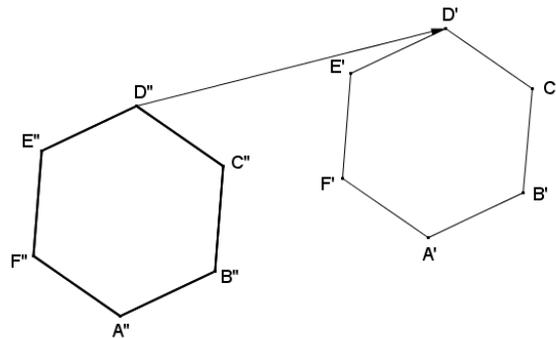
O_2 •

Lesson Summary

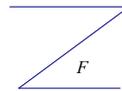
In a series of dilations, the scale factor that maps the original figure onto the final image is the product of all the scale factors in the series of dilations.

Problem Set

- In Lesson 7, the dilation theorem for line segments said that if two different length line segments in the plane were parallel to each other, then a dilation exists mapping one segment onto the other. Explain why the line segments must be different lengths for a dilation to exist.
- Regular hexagon $A'B'C'D'E'F'$ is the image of regular hexagon $ABCDEF$ under a dilation from center O_1 , and regular hexagon $A''B''C''D''E''F''$ is the image of regular hexagon $ABCDEF$ under a dilation from center O_2 . Points $A', B', C', D', E',$ and F' are also the images of points $A'', B'', C'', D'', E'',$ and F'' , respectively, under a translation along vector $\overrightarrow{D''D'}$. Find a possible regular hexagon $ABCDEF$.

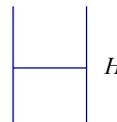


3. A dilation with center O_1 and scale factor $\frac{1}{2}$ maps figure F to figure F' . A dilation with center O_2 and scale factor $\frac{3}{2}$ maps figure F' to figure F'' . Draw figures F' and F'' , and then find the center O and scale factor r of the dilation that takes F to F'' .



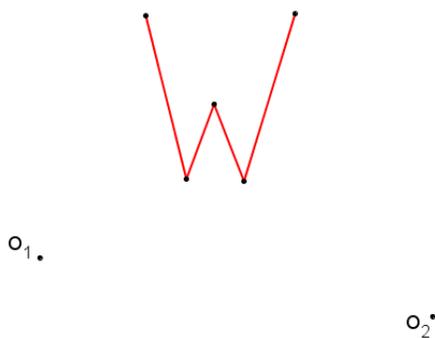
$O_1 \bullet \quad \bullet O_2$

4. If a figure T is dilated from center O_1 with a scale factor $r_1 = \frac{3}{4}$ to yield image T' , and figure T' is then dilated from center O_2 with a scale factor $r_2 = \frac{4}{3}$ to yield figure T'' . Explain why $T \cong T''$.
5. A dilation with center O_1 and scale factor $\frac{1}{2}$ maps figure H to figure H' . A dilation with center O_2 and scale factor 2 maps figure H' to figure H'' . Draw figures H' and H'' . Find a vector for a translation that maps H to H'' .



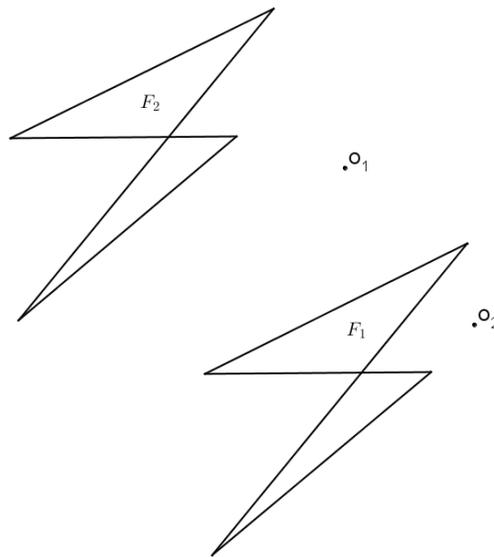
$O_1 \bullet \quad \bullet O_2$

6. Figure W is dilated from O_1 with a scale factor $r_1 = 2$ to yield W' . Figure W' is then dilated from center O_2 with a scale factor $r_2 = \frac{1}{4}$ to yield W'' .



- Construct the composition of dilations of figure W described above.
- If you were to dilate figure W'' , what scale factor would be required to yield an image that is congruent to figure W ?
- Locate the center of dilation that maps W'' to W using the scale factor that you identified in part (b).

7. Figures F_1 and F_2 in the diagram below are dilations of F from centers O_1 and O_2 , respectively.



- a. Find F .
 - b. If $F_1 \cong F_2$, what must be true of the scale factors r_1 and r_2 of each dilation?
 - c. If $F_1 \cong F_2$, what must be true of the scale factors r_1 and r_2 of each dilation?
8. Use a coordinate plane to complete each part below using $U(2,3)$, $V(6,6)$, and $W(6,-1)$.
- a. Dilate $\triangle UVW$ from the origin with a scale factor $r_1 = 2$. List the coordinate of image points U' , V' , and W' .
 - b. Dilate $\triangle UVW$ from $(0,6)$ with a scale factor of $r_2 = \frac{3}{4}$. List the coordinates of image points U'' , V'' , and W'' .
 - c. Find the scale factor, r_3 , from $\triangle U'V'W'$ to $\triangle U''V''W''$.
 - d. Find the coordinates of the center of dilation that maps $\triangle U'V'W'$ to $\triangle U''V''W''$.