Lesson 26: Ruling Out Chance

Classwork

Opening Exercise

Previously, you considered the random assignment of tomatoes into two distinct groups of tomatoes each called Group A and Group B. With each random assignment, you calculated “Diff” = , the difference between the mean weight of the tomatoes in Group A and the mean weight of the tomatoes in Group B.

1. Summarize in writing what you learned in the last lesson. Share your thoughts with a neighbor.
2. Recall that of these tomatoes are from plants that received a nutrient treatment in the hope of growing bigger tomatoes. But what if the treatment was ***not*** effective? What difference would you expect to find between the group means?

Exercises 1–2: The Distribution of “Diff” and Why “0” is Important

In the previous lesson, instances of the tomato randomization were considered. Imagine that the random assignment was conducted an additional times, and "Diff" values were computed from these random assignments. The results are shown graphically below in a dot plot where each dot represents the "Diff" value that results from a random assignment:

This dot plot will serve as your *randomization distribution* for the "Diff" statistic in this tomato randomization example. The dots are placed at increments of ounces.

1. Given the distribution picture above, what is the *approximate* value of the median and mean of the distribution? Specifically, do you think this distribution is centered near a value that implies "No Difference" between Group A and Group B?
2. Given the distribution pictured above and based on the simulation results, determine the approximate probability of obtaining a "Diff" value in the cases described in (a), (b), and (c).
   1. of ounces or more
   2. of ounces or less
   3. within ounces of ounces
   4. How do you think these probabilities could be useful to people that are designing experiments?

Exercises 3-5: Statistically Significant "Diff" Values

In the context of a randomization distribution that is based upon the assumption that there is no real difference between the groups, consider a "Diff" value of to be "statistically significant" if there is a low probability of obtaining a result that is as extreme as or more extreme than .

1. Using that definition and your work above, would you consider any of the "Diff" values below to be statistically significant? Explain.
   1. ounces

* 1. ounces

* 1. Values within ounces of ounces

1. In the previous lessons, you obtained "Diff" values of ounces, ounces, and ounces for different tomato randomizations. Would you consider any of those values to be "statistically significant" for this distribution? Explain.

1. Recalling that "Diff" is the mean weight of the Group A tomatoes minus the mean weight of the Group B tomatoes, how would you explain the meaning of a "Diff" value of ounces in this case?

**Exercises 6-8: The Implication of Statistically Significant "Diff" Values**

Keep in mind that for reasons mentioned earlier, the randomization distribution above is demonstrating what is likely to happen *by chance alone* if the treatment was *not* effective. As stated in the previous lesson, you can use this randomization distribution to assess whether or not the *actual* difference in means *obtained from your experiment* (the difference between the mean weight of the actual control group tomatoes and the mean weight of the actual treatment group tomatoes) is consistent with usual chance behavior. The logic is as follows:

* If the observed difference is “extreme” and not typical of chance behavior, it may be considered “statistically significant” and possibly not the result of chance behavior.
* If the difference is not the result of chance behavior, then maybe the difference did not just happen by chance alone.
* If the difference did not just happen by chance alone, maybe the difference you observed is caused by the treatment in question, which, in this case, is the nutrient. In the context of our example, a statistically significant "Diff" value provides evidence that the nutrient treatment did in fact yield heavier tomatoes on average.

1. For reasons that will be explained in the next lesson, for your tomato example, "Diff" values that are *positive* and statistically significant will be considered as good evidence that your nutrient treatment did in fact yield heavier tomatoes on average. Again, using the randomization distribution shown earlier in the lesson, which (if any) of the following "Diff" values would you consider to be statistically significant and lead you to think that the nutrient treatment did, in fact, yield heavier tomatoes on average? Explain for each case.

Diff = , Diff = , Diff = , Diff = , Diff = , Diff =

1. In the first random assignment in the previous lesson, you obtained a “Diff” value of ounces. Earlier in this lesson, you were asked to consider if this might be a "statistically significant" value. Given the distribution shown in this lesson, if you had obtained a "Diff" value of ounces ***in your experiment*** and the Group A tomatoes had been the “treatment” tomatoes that received the nutrient, would you say that the “Diff” value was extreme enough to support a conclusion that the nutrient treatment yielded heavier tomatoes on average? Or, do you think such a “Diff” value may just occur by chance when the treatment is ineffective? Explain.
2. In the second random assignment in the previous lesson, you obtained a “Diff” value of ounces. Earlier in this lesson, you were asked to consider if this might be a "statistically significant" value. Given the distribution shown in this lesson, if you had obtained a "Diff" value of ounces ***in your experiment*** and the Group A tomatoes had been the “treatment” tomatoes that received the nutrient, would you say that the “Diff” value was extreme enough to support a conclusion that the nutrient treatment yielded heavier tomatoes on average? Or do you think such a “Diff” value may just occur by chance when the treatment is ineffective? Explain.

Problem Set

Lesson Summary

In the previous lesson, the concept of randomly separating tomatoes into groups and comparing the means of each group was introduced. The randomization distribution of the difference in means that is created from multiple occurrences of these random assignments demonstrates what is likely to happen *by chance alone* if the nutrient treatment is *not* effective. When the results of your tomato growth experiment are compared to that distribution, you can then determine if the tomato growth experiment’s results were typical of chance behavior.

If the results appear typical of chance behavior and near the center of the distribution (that is, not relatively very far from a “Diff” of ), then there is little evidence that the treatment was effective. However, if it appears that the experiment's results are not typical of chance behavior, then, maybe, the difference you are observing didn't just happen by chance alone. It may indicate a statistically significant difference between the treatment group and the control group, and the source of that difference might be (in this case) the nutrient treatment.

In each of the cases below, calculate the "Diff" value as directed, and write a sentence explaining what the "Diff" value means in context. Write the sentence for a general audience.

1. Group A: dieters lost an average of pounds.

Group B: non-dieters lost an average of pounds over the same time period.

Calculate and interpret "Diff" = the mean of Group A minus the mean of Group B.

1. Group A: students were on average seconds faster in their meter run times after following a new training regimen.

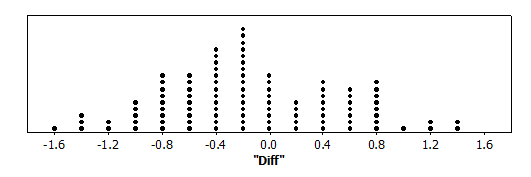
Group B: students were on average seconds slower in their meter run times after not following any new training regimens.

Calculate and interpret "Diff" = the mean of Group A minus the mean of Group B.

1. Group A: squash that have been grown in an irrigated field have an average weight of pounds.

Group B: squash that have been grown in a non-irrigated field have an average weight of pounds.

Calculate and interpret "Diff" = the mean of Group A minus the mean of Group B.

1. ****Using the randomization distribution shown in the Exit Ticket, what is the probability of obtaining a "Diff" value of — or less?
2. Would a "Diff" value of or less be considered a “statistically significant difference”? Why or why not?
3. Using the randomization distribution shown in the Exit Ticket, what is the probability of obtaining a "Diff" value of or less?
4. Would a "Diff" value of or less be considered a “statistically significant difference”? Why or why not?