



Student Outcomes

- Students apply properties of logarithms to solve exponential equations.
- Students relate solutions to f(x) = g(x) to the intersection point(s) on the graphs of y = f(x) and y = g(x)in the case where f and g are constant or exponential functions.

Lesson Notes

Much of our previous work with logarithms in Topic B provided students with the particular skills needed to manipulate logarithmic expressions and solve exponential equations. Although students have solved exponential equations in earlier lessons in Topic B, this is the first time that they solve such equations in the context of exponential functions. In this lesson, students solve exponential equations of the form $ab^{ct} = d$ using properties of logarithms developed in Lessons 12 and 13 (F-LE.A.4). For an exponential function f, students solve equations of the form f(x) = c and write a logarithmic expression for the inverse (**F-BF.B.4a**). Additionally, students solve equations of the form f(x) = g(x)where f and g are either constant or exponential functions (A-REI.D.11). Examples of exponential functions in this lesson draw from Lesson 7, in which the growth of a bacteria population was modeled by the function $P(t) = 2^t$, and Lesson 23, in which students modeled the growth of an increasing number of beans with a function $f(t) = a(b^t)$, where $a \approx 1$ and $b \approx 1.5$.

Students will need to use technology to calculate logarithmic values and to graph linear and exponential functions.

Classwork

Opening Exercise (4 minutes)

The Opening Exercise is a simple example of solving an exponential equation of the form $ab^{ct} = d$. Allow students to work independently or in pairs to solve this problem. Circulate around the room to check that all students know how to apply a logarithm to solve this problem. Students can choose to use either a base 2 or base 10 logarithm.

Opening Exercise

In Lesson 7, we modeled a population of bacteria that doubled every day by the function $P(t) = 2^t$, where t was the time in days. We wanted to know the value of t when there were 10 bacteria. Since we did not know about logarithms at the time, we approximated the value of t numerically, and we found that P(t) = 10 at approximately $t \approx 3.32$ days.

Use your knowledge of logarithms to find an exact value for t when P(t) = 10, and then use your calculator to approximate that value to 4 decimal places.

Since $P(t) = 2^t$, we need to solve $2^t = 10$.

 $2^{t} = 10$ $t\log(2) = \log(10)$ log(2) $t \approx 3.3219$

Thus, the population will reach 10 bacteria in approximately 3.3219 days.



Lesson 24: Solving Exponential Equations 11/17/14



Date:





Discussion (2 minutes)

Ask students to describe their solution method for the Opening Exercise. Make sure that solutions are discussed using both base 10 and base 2 logarithms. If all students used the common logarithm to solve this problem, then present the following solution using the base 2 logarithm:

$$2^{t} = 10$$
$$\log_{2}(2^{t}) = \log_{2}(10)$$
$$t = \log_{2}(10)$$
$$t = \frac{\log(10)}{\log(2)}$$
$$t = \frac{1}{\log(2)}$$
$$t \approx 3.3219$$

The remaining exercises ask students to solve equations of the form f(x) = c or f(x) = g(x), where f and g are exponential functions (F-LE.A.4, F-BF.B.4a, A-REI.D.11). For the remainder of the lesson, allow students to work either independently or in pairs or small groups on the exercises. Circulate to ensure students are on task and solving the equations correctly. After completing Exercises 1–4, debrief students to check for understanding, and ensure they are using appropriate strategies to complete problems accurately before moving on to Exercises 5–10.



Exe	rcises			
1.	Fiona modeled her data from the bean-flipping experiment in Lesson 23 by the function $f(t) = 1.263(1.357)^t$, and Gregor modeled his data with the function $g(t) = 0.972(1.629)^t$.			
	a.	 Without doing any calculating, determine which student, Fiona or Gregor, accumulated 100 beans first. Explain how you know. 		
	Since the base of the exponential function for Gregor's model, 1.629, is larger than the base of the exponential function for Fiona's model, 1.357, Gregor's model will grow more quickly than Fiona's, and he will accumulate 100 beans before Fiona does.			
	b.	Using Fiona's model	Scaffolding:	
		i. How many trials would be needed for her to accumulate 100 beans? We need to solve the equation $f(t) = 100$ for t.	Have struggling students begin this exercise with functions $f(t) = 7(2^t)$ and $g(t) = 4(3^t)$	
	$1.263(1.357)^t = 100$		f(t) = f(2) and $g(t) = f(3)$.	
		$1.357^t = \frac{100}{1.263}$		
		$t \log(1.357) = \log\left(\frac{100}{1.263}\right)$		
		$t \log(1.357) = \log(100) - \log(1.263)$ 2 - log(1.263)		
		$t = \frac{2 - \log(1.253)}{\log(1.357)}$		
		$t \approx 14.32$		
	So, it takes 15 trials for Fiona to accumulate 100 beans.			



Lesson 24: Solving Exponential Equations 11/17/14



Date:



Lesson 24 M3

ALGEBRA II

ii. How many trials would be needed for her to accumulate 1,000 beans? We need to solve the equation f(t) = 1000 for t. $1.263(1.357)^t = 1000$ $1.357^t = \frac{1000}{1.263}$ $t\log(1.357) = \log\left(\frac{1000}{1.263}\right)$ $t \log(1.357) = \log(1000) - \log(1.263)$ $t = \frac{3 - \log(1.263)}{\log(1.357)}$ $t \approx 21.86$ So, it takes 22 trials for Fiona to accumulate 1,000 beans. Using Gregor's model ... c. How many trials would be needed for him to accumulate 100 beans? i. We need to solve the equation g(t) = 100 for t. $0.972(1.629)^t = 100$ $1.629^t = \frac{100}{0.972}$ $t \log(1.629) = \log\left(\frac{100}{0.972}\right)$ $t \log(1.629) = \log(100) - \log(0.972)$ $t = \frac{2 - \log(0.972)}{\log(1.629)}$ $t \approx 9.50$ So, it takes 10 trials for Gregor to accumulate 100 beans. ii. How many trials would be needed for him to accumulate 1,000 beans? We need to solve the equation g(t) = 1000 for t. $(0.972(1.629)^t = 1000)$ $1.629^t = \frac{1000}{0.972}$ $t\log(1.629) = \log\left(\frac{1000}{0.972}\right)$ $t \log(1.629) = \log(1000) - \log(0.972)$ $t = \frac{3 - \log(0.972)}{\log(1.629)}$ $t \approx 14.21$ So, it takes 15 trials for Gregor to accumulate 1,000 beans. Was your prediction in part (a) correct? If not, what was the error in your reasoning? d. Responses will vary. Either students made the correct prediction, or they did not recognize that the base b determines the growth rate of the exponential function so the larger base 1.629 causes Gregor's function to grow much more guickly than Fiona's.



Lesson 24: S Date: 1

Solving Exponential Equations 11/17/14



383









Solving Exponential Equations 11/17/14











Lesson 24: Sc Date: 11



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Lesson 24: Date: Solving Exponential Equations 11/17/14

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Debrief students after they complete Exercises 1–4 to ensure understanding of the exercises and strategies used to solve the exercises before continuing. Exercises 5–10 let students solve exponential functions using what they know about logarithms. After completing Exercises 5–10, debrief students about when it is necessary to use logarithms to solve exponential equations and when it is not. Exercises 7, 8, and 9 are examples of exercises that do not require logarithms to solve but may be appropriate to solve with logarithms depending on the preferences of students.

Exercise 5–10 (7 minutes)

For the following functions f and g, solve the equation f(x) = g(x). Express your solutions in terms of logarithms. 5. $f(x) = 10(3.7)^{x+1}$, $g(x) = 5(7.4)^x$ $10(3.7)^{x+1} = 5(7.4)^x$ $2(3,7)^{x+1} = 7.4^x$ $\log(2) + \log(3.7^{x+1}) = \log(7.4^x)$ log(2) + (x + 1) log(3.7) = x log(7.4) $\log(2) + x \log(3.7) + \log(3.7) = x \log(7.4)$ $\log(2) + \log(3.7) = x(\log(7.4) - \log(3.7))$ $log(7.4) = x log(\frac{7.4}{3.7})$ Scaffolding: Challenge advanced $\log(7.4) = x \log(2)$ students to solve Exercise 6 $x = \frac{\log(7.4)}{\log(2)}$ in more than one way, for example, by using first the logarithm base 5 and then $f(x) = 135(5)^{3x+1}, g(x) = 75(3)^{4-3x}$ the logarithm base 3, and 6. compare the results. $135(5)^{3x+1} = 75(3)^{4-3x}$ Advanced students should $9(5)^{3x+1} = 5(3)^{4-3x}$ be able to solve Exercises $\log(9) + (3x + 1)\log(5) = \log(5) + (4 - 3x)\log(3)$ 7–9 without logarithms by $2\log(3) + 3x\log(5) + \log(5) = \log(5) + 4\log(3) - 3x\log(3)$ expressing each function $3x(\log(5) + \log(3)) = 4\log(3) - 2\log(3)$ with a common base, but $3x \log(15) = 2 \log(3)$ logarithms may be easier $x = \frac{2\log(3)}{3\log(15)}$ and more reliable for students struggling with the exponential properties. 7. $f(x) = 100^{x^3 + x^2 - 4x}, g(x) = 10^{2x^2 - 6x}$ $100^{x^3 + x^2 - 4x} = 10^{2x^2 - 6x}$ $(10^2)^{x^3 + x^2 - 4x} = 10^{2x^2 - 6x}$ $2(x^3 + x^2 - 4x) = 2x^2 - 6x$ $x^3 + x^2 - 4x = x^2 - 3x$ $x^3 - x = 0$ $x(x^2-1)=0$ x(x+1)(x-1) = 0x = 0, x = -1, or x = 1

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 $f(x) = 48(4^{x^2+3x}), g(x) = 3(8^{x^2+4x+4})$ 8. $48(4^{x^2+3x}) = 3(8^{x^2+4x+4})$ $16(4^{x^2+3x}) = 8^{x^2+4x+4}$ $2^4 ((2^2)^{x^2+3x}) = (2^3)^{x^2+4x+4}$ $2^{2x^2+6x+4} = 2^{3x^2+12x+12}$ $2x^2 + 6x + 4 = 3x^2 + 12x + 12$ $x^2 + 6x + 8 = 0$ (x+4)(x+2) = 0x = -4 or x = -2 $f(x) = e^{\sin^2(x)}, g(x) = e^{\cos^2(x)}$ 9. $e^{\sin^2(x)} = e^{\cos^2(x)}$ $\sin^2(x) = \cos^2(x)$ sin(x) = cos(x) or sin(x) = -cos(x) $x = \frac{\pi}{4} + k\pi$ or $x = \frac{3\pi}{4} + k\pi$ for all integers k10. $f(x) = (0.49)^{\cos(x) + \sin(x)}, \ g(x) = (0.7)^{2\sin(x)}$ $(0.49)^{\cos(x)+\sin(x)} = (0.7)^{2\sin(x)}$ $\log((0.49)^{\cos(x)+\sin(x)}) = \log(0.7)^{2\sin(x)})$ $(\cos(x) + \sin(x))\log(0.49) = 2\sin(x)\log(0.7)$ $(\cos(x) + \sin(x))\log(0.7^2) = 2\sin(x)\log(0.7)$ $2(\cos(x) + \sin(x))\log(0.7) = 2\sin(x)\log(0.7)$ $2\cos(x) + 2\sin(x) = 2\sin(x)$ $\cos(x) = 0$ $x = \frac{\pi}{2} + k\pi$ for all integers k

Closing (3 minutes)

Ask students to respond to the following prompts either in writing or orally to a partner.

- Describe two different approaches to solving the equation $2^{x+1} = 3^{2x}$. Do not actually solve the equation.
 - You could begin by taking the logarithm base 10 of both sides, or the logarithm base 2 of both sides.
 (Or, you could even take the logarithm base 3 of both sides.)
- Could the graphs of two exponential functions $f(x) = 2^{x+1}$ and $g(x) = 3^{2x}$ ever intersect at more than one point? Explain how you know.
 - No. The graphs of these functions will always be increasing. They will intersect at one point, but once they cross once they cannot cross again. For large values of x, the quantity 3^{2x} will always be greater than 2^{x+1} , so the graph of g will end up above the graph of f after they cross.





- Discuss how the starting value and base affect the graph of an exponential function and how this can help you compare exponential functions.
 - The starting value determines the y-intercept of an exponential function, so it determines how large or small the function is when x = 0. The base is ultimately more important and determines how quickly the function increases (or decreases). When comparing exponential functions, the function with the larger base will always overtake the function with the smaller base no matter how large the value when x = 0.
- If $f(x) = 2^{x+1}$ and $g(x) = 3^{2x}$, is it possible for the equation f(x) = g(x) to have more than one solution?
 - No. Solutions to the equation f(x) = g(x) correspond to x-values of intersection points of the graphs of y = f(x) and y = g(x). Since these graphs can intersect no more than once, the equation can have no more than one solution.

Exit Ticket (4 minutes)





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Lesson 24

M3

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Date

Lesson 24: Solving Exponential Equations

Exit Ticket

Consider the functions $f(x) = 2^{x+6}$ and $g(x) = 5^{2x}$.

a. Use properties of logarithms to solve the equation f(x) = g(x). Give your answer as a logarithmic expression, and approximate it to two decimal places.

b. Verify your answer by graphing the functions y = f(x) and y = g(x) in the same window on a calculator, and sketch your graphs below. Explain how the graph validates your solution to part (a).







Exit Ticket Sample Solutions



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Lesson 24: Solving Date: 11/17/

Solving Exponential Equations 11/17/14

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Problem Set Sample Solutions

1. Solve the following equations. $2 \cdot 5^{x+3} = 6250$ a. $5^{x+3} = 3125$ $5^{x+3} = 5^5$ x + 3 = 5x = 2b. $3 \cdot 6^{2x} = 648$ $6^{2x} = 216$ $6^{2x} = 6^3$ 2x = 3 $x=\frac{3}{2}$ $5 \cdot 2^{3x+5} = 10240$ c. $2^{3x+5} = 2048$ $2^{3x+5} = 2^{11}$ 3x + 5 = 113x = 6x = 2d. $4^{3x-1} = 32$ $4^{3x-1} = 2^5$ $2^{2 \cdot (3x-1)} = 2^5$ 6x - 2 = 56x = 7 $x=\frac{7}{6}$ $3 \cdot 2^{5x} = 216$ e. $2^{5x} = 72$ $5x \cdot \ln(2) = \ln(72)$ $x = \frac{\ln(72)}{5 \cdot \ln(2)}$ $x \approx 1.234$ Note: Students can also use common logs to solve for the solution.







 $5 \cdot 11^{3x} = 120$

 $7 \cdot 9^x = 5405$

 $\sqrt{3} \cdot 3^{3x} = 9$

 $\log(400) \cdot 8^{5x} = \log(160000)$

f.

g.

h.

i.

2.



ALGEBRA II

 $11^{3x} = 24$ $3x \cdot \ln(11) = \ln(24)$ $x = \frac{\ln(24)}{3 \cdot \ln(11)}$ $x \approx 0.442$ Note: Students can also use common logs to solve for the solution. $9^{x} = \frac{5405}{7}$ $x \cdot \ln(9) = \ln\left(\frac{5405}{7}\right)$ $x = \frac{\ln\left(\frac{5405}{7}\right)}{\ln(9)}$ $x \approx 3.026$ Note: Students can also use common logs to solve for the solution. Solution using properties of exponents: $3^{\frac{1}{2}} \cdot 3^{3x} = 3^2$ $3^{\frac{1}{2}+3x} = 3^{2}$ $\frac{1}{2}+3x = 2$ $x=\frac{1}{2}$ $8^{5x} = \frac{\log(160000)}{\log(400)}$ $8^{5x} = 2$ $8^{5x} = 8^{\frac{1}{3}}$ $5x = \frac{1}{3}$ $x = \frac{1}{15}$ Lucy came up with the model $f(t) = 0.701(1.382)^t$ for the first bean activity. When does her model predict that

> $1000 = 0.701(1.382)^t$ $\log(1000) = \log(0.701) + t \log(1.382)$ $t = \frac{\log(1000) - \log(0.701)}{\log(1.382)}$ $t \approx 22.45$

Lucy's model predicts that it will take 23 trials to have over 1,000 beans.



Lesson 24: Solving Exponential Equations Date: 11/17/14

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she would have 1,000 beans?





M3

Lesson 24

3. Jack came up with the model $g(t) = 1.033(1.707)^t$ for the first bean activity. When does his model predict that he would have 50,000 beans? $50,000 = 1.033(1.707)^t$ $\log(50000) = \log(1.033) + t\log(1.707)$ $t = \frac{\log(50000) - \log(1.033)}{1000}$ log(1.707) $t \approx 20.17$ Jack's model predicts that it will take 21 trials to have over 50,000 beans. 4. If instead of beans in the first bean activity you were using fair coin, when would you expect to have \$1,000,000? One million dollars is 10^8 pennies. Using fair pennies, we can model the situation by $f(t) = 1.5^t$. $10^8 = 1.5^t$ $8 = t \log(1.5)$ $t = \frac{8}{\log(1.5)}$ $t \approx 45.43$ We should expect it to take 46 trials to reach more than \$1 million using fair pennies. Let $f(x) = 2 \cdot 3^x$ and $g(x) = 3 \cdot 2^x$. 5. Which function is growing faster as *x* increases? Why? a. The function f is growing faster due to its larger base, even though g(0) > f(0). When will f(x) = g(x)? b. $\boldsymbol{f}(\boldsymbol{x}) = \boldsymbol{g}(\boldsymbol{x})$ $2 \cdot 3^x = 3 \cdot 2^x$ $\ln(2\cdot 3^x) = \ln(3\cdot 2^x)$ $\ln(2) + x \ln(3) = \ln(3) + x \ln(2)$ $x\ln(3) - x\ln(2) = \ln(3) - \ln(2)$ $x\ln\left(\frac{3}{2}\right) = \ln\left(\frac{3}{2}\right)$ x = 1Note: Students can also use common logs to solve for the solution.



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Solving Exponential Equations 11/17/14









Lesson 24: Solving Exponential Equations Date: 11/17/14

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b. The population of earth is approximately 7.1 billion people. On what day will 7.1 billion emails be sent out? $7.1(10^9) = 10(3^n)$ $7.1(10^8) = 3^n$ $\log(7.1(10^8)) = n \cdot \log(3)$ $n = \frac{8 + \log(7.1)}{\log(3)}$ $n \approx 18.5514$ By the 19th day, more than 7.1 billion emails will be sent. 8. Solve the following exponential equations. $10^{(3x-5)} = 7^x$ a. $10^{3x-5} = 7^x$ $3x - 5 = x \log(7)$ $x(3-\log(7))=5$ $x = \frac{5}{3 - \log(7)}$ b. $3^{\frac{x}{5}} = 2^{4x-2}$ $3^{\frac{x}{5}} = 2^{4x-2}$ $\frac{x}{5}\log(3) = (4x - 2)\log(2)$ $4x\log(2) - x\frac{\log(3)}{5} = 2\log(2)$ $x\left(4\log(2)-\frac{\log(3)}{5}\right)=2\log(2)$ $x = \frac{2\log(2)}{4\log(2) - \frac{\log(3)}{5}}$ $10^{x^2+5} = 100^{2x^2+x+2}$ с. $\mathbf{10}^{x^2+5} = \mathbf{100}^{2x^2+x+2}$ $x^{2} + 5 = (2x^{2} + x + 2)\log(100)$ $x^2 + 5 = 4x^2 + 2x + 4$ $3x^2 + 2x - 1 = 0$ (3x-1)(x+1) = 0 $x = \frac{1}{3}$ or x = -1



Solving Exponential Equations 11/17/14





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 $4^{x^2 - 3x + 4} = 2^{5x - 4}$ d. $4^{x^2 - 3x + 4} = 2^{5x - 4}$ $(x^2 - 3x + 4) \log_2(4) = (5x - 4) \log_2(2)$ $2(x^2 - 3x + 4) = 5x - 4$ $2x^2 - 6x + 8 = 5x - 4$ $2x^2 - 11x + 12 = 0$ (2x-3)(x-4) = 0 $x=\frac{3}{2} or x=4$ 9. Solve the following exponential equations. $(2^x)^x = 8^x$ a. $2^{x^2} = 8^x$ $x^2 \log_2(2) = x \log_2(8)$ $x^2 = 3x$ $x^2 - 3x = 0$ x(x-3) = 0x = 0 or x = 3 $(3^x)^x = 12$ b. $3^{x^2} = 12$ $x^2 log(3) = log(12)$ $x^2 = \frac{log(12)}{log(3)}$ $x = \sqrt{\frac{\log(12)}{\log(3)}}$ or $x = -\sqrt{\frac{\log(12)}{\log(3)}}$ 10. Solve the following exponential equations. $10^{x+1} - 10^{x-1} = 1,287$ a. $10^{x+1} - 10^{x-1} = 1,287$ $100(10^{x-1}) - 10^{x-1} = 1,287$ $10^{x-1}(100-1) = 1,287$ $99(10^{x-1}) = 1,287$ $10^{x-1} = 13$ $x - 1 = \log(13)$ $x = \log(13) + 1$ $2(4^x) + 4^{x+1} = 342$ b. $2(4^x) + 4^{x+1} = 342$ $2(4^x) + 4(4^x) = 342$ $6(4^x) = 342$ $4^{x} = 57$ $x = \log_4(57) = \frac{\log(57)}{\log(4)} = \frac{1}{2}\log_2(57)$



Date:





11. Solve the following exponential equations. $(10^x)^2 - 3(10^x) + 2 = 0$ Hint: Let $u = 10^x$, and solve for u before solving for x. a. Let $u = 10^x$. Then $u^2-3u+2=0$ (u-2)(u-1)=0u=2 or u=1*If* u = 2, we have $2 = 10^x$, and then $x = \log(2)$. *If* u = 1*, we have* $1 = 10^{x}$ *, and then* x = 0*.* Thus, the two solutions to this equation are 0 and log(2). b. $(2^x)^2 - 3(2^x) - 4 = 0$ *Let* $u = 2^{x}$. $u^2-3u-4=0$ (u-4)(u+1)=0u = 4 or u = -1If u = 4, we have $2^x = 4$, and then x = 2. If u = -1, we have $2^x = -1$, which has no solution. Thus, the only solution to this equation is 2. $3(e^{x})^{2} - 8(e^{x}) - 3 = 0$ c. Let $u = e^x$. $3u^2 - 8u - 3 = 0$ (u-3)(3u+1)=0 $u = 3 \text{ or } u = -\frac{1}{3}$ If u = 3, we have $e^x = 3$, and then $x = \ln(3)$. If $u = -\frac{1}{3}$, we have $e^x = -\frac{1}{3}$, which has no solution because $e^x > 0$ for every value of x. Thus, the only solution to this equation is ln(3). $4^x + 7(2^x) + 12 = 0$ d. Let $u = 2^{x}$. $(2^x)^2 + 7(2^x) + 12 = 0$ $u^2 + 7u + 12 = 0$ (u+3)(u+4) = 0u = -3 or u = -4But $2^x > 0$ for every value of x, thus there are no solutions to this equation.



Solving Exponential Equations 11/17/14





398

 $(10^x)^2 - 2(10^x) - 1 = 0$ e. *Let* $u = 10^{x}$. $u^2-2u-1=0$ $u = 1 + \sqrt{2}$ or $u = 1 - \sqrt{2}$ If $u = 1 + \sqrt{2}$, we have $10^x = 1 + \sqrt{2}$, and then $x = \log(1 + \sqrt{2})$. If $u = 1 - \sqrt{2}$, we have $10^x = 1 - \sqrt{2}$, which has no solution because $1 - \sqrt{2} < 0$. Thus, the only solution to this equation is $\log(1+\sqrt{2})$. 12. Solve the following systems of equations. $2^{x+2y} = 8$ $2^{x+2y} = 2^3$ a. $4^{2x+y} = 1$ $4^{2x+y} = 4^0$ x + 2y = 32x + y = 0x + 2y = 34x + 2y = 0*y* = 2 x = -1 $2^{2x+y-1} = 2^5$ $2^{2x+y-1} = 32$ b. $4^{x-2y} = 2$ $(2^2)^{x-2y} = 2^1$ 2x + y - 1 = 52(x-2y)=12x + y = 62x - 4y = 1*y* = 1 $x = \frac{5}{2}$ $2^{3x} = 8^{2y+1}$ $2^{3x} = (2^3)^{2y+1}$ c. $9^{2y} = 3^{3x-9}$ $(3^2)^{2y} = 3^{3x-9}$ 3x = 3(2y + 1)2(2y) = (3x - 9)3x - 6y = 33x - 4y = 9y = 3*x* = 7

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e. $\begin{pmatrix} \frac{3}{4} \end{pmatrix}^{x} > \left(\frac{4}{3}\right)^{x+1}$ $\begin{pmatrix} \frac{3}{4} \end{pmatrix}^{x} > \left(\frac{4}{3}\right)^{x+1}$ $x \log\left(\frac{3}{4}\right) > (x+1)\log\left(\frac{4}{3}\right)$ $x \left(\log\left(\frac{3}{4}\right) - \log\left(\frac{4}{3}\right)\right) > \log\left(\frac{4}{3}\right)$ $But, \log\left(\frac{3}{4}\right) = -\log\left(\frac{4}{3}\right), \text{ so we have}$ $x \left(-\log\left(\frac{4}{3}\right) - \log\left(\frac{4}{3}\right)\right) > \log\left(\frac{4}{3}\right)$ $x \left(-2\log\left(\frac{4}{3}\right)\right) > \log\left(\frac{4}{3}\right)$ $But, -2\log\left(\frac{4}{3}\right) < 0, \text{ so we need to divide by a negative number, so we have }$ $x < \frac{\log\left(\frac{4}{3}\right)}{-2\log\left(\frac{4}{3}\right)}$ $x < -\frac{1}{2}$





