Lesson 18: Graphs of Exponential Functions and Logarithmic Functions

Classwork

Opening Exercise

Complete the following table of values of the function . We want to sketch the graph of and then reflect that graph across the diagonal line with equation .

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|  |  | Point on the graphof  |
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On the set of axes below, plot the points from the table and sketch the graph of . Next, sketch the diagonal line with equation , and then reflect the graph of across the line.



Exercises

1. Complete the following table of values of the function . We want to sketch the graph of and then reflect that graph across the diagonal line with equation .

|  |  |  |
| --- | --- | --- |
|  |  | Point on the graphof  |
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On the set of axes below, plot the points from the table and sketch the graph of . Next, sketch the diagonal line with equation , and then reflect the graph of across the line.

1. Working independently, predict the relation between the graphs of the functions and . Test your predictions by sketching the graphs of these two functions. Write your prediction in your notebook, provide justification for your prediction, and compare your prediction with that of your neighbor.



1. Now let’s compare the graphs of the functions and ; sketch the graphs of the two exponential functions on the same set of axes; then, answer the questions below.



* 1. Where do the two graphs intersect?
	2. For which values of is ?
	3. For which values of is ?
	4. What happens to the values of the functions and as ?
	5. What happens to the values of the functions and as ?
	6. Does either graph ever intersect the -axis? Explain how you know.
1. Add sketches of the two logarithmic functions and to the axes with the graphs of the exponential functions; then, answer the questions below.
	1. Where do the two logarithmic graphs intersect?
	2. For which values of is ?
	3. For which values of is ?
	4. What happens to the values of the functions and as ?
	5. What happens to the values of the functions and as ?
	6. Does either graph ever intersect the -axis? Explain how you know.
	7. Describe the similarities and differences in the behavior of and as .

Problem Set

1. Sketch the graphs of the functions and .
2. Sketch the graphs of the functions and .
3. Sketch the graphs of the functions and on the same sheet of graph paper and answer the following questions.
	1. Where do the two exponential graphs intersect?
	2. For which values of is ?
	3. For which values of is ?
	4. What happens to the values of the functions and as?
	5. What are the domains of the two functions and ?
4. Use the information from Problem 3 together with the relationship between graphs of exponential and logarithmic functions to sketch the graphs of the functions and on the same sheet of graph paper. Then, answer the following questions.
	1. Where do the two logarithmic graphs intersect?
	2. For which values of is ?
	3. For which values of is ?
	4. What happens to the values of the functions and as ?
	5. What are the domains of the two functions and ?
5. For each function , find a formula for the function in terms of .
	1. If , find .
	2. If , find .
	3. If , find .
	4. If , find .
6. In Problem 5, parts (c) and (d), list at least two aspects about the formulas you found as they relate to the function
.
7. For each of the functions and below, write an expression for (i) , (ii) , and (iii) in terms of .
	1. ,
	2. , for two numbers and , when is not equal to or
	3. , , when is not equal to or
	4. ,
	5. ,
	6. ,