# **Lesson 13: Mastering Factoring**

## Classwork

## **Opening Exercises**

Factor each of the following expressions. What similarities do you notice between the examples in the left column and those on the right?

a. 
$$x^2 - 1$$

b. 
$$9x^2 - 1$$

c. 
$$x^2 + 8x + 15$$

d. 
$$4x^2 + 16x + 15$$

e. 
$$x^2 - y^2$$

f. 
$$x^4 - y^4$$

## Example 1

Write  $9 - 16x^4$  as the product of two factors.

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# Example 2

Factor  $4x^2y^4 - 25x^4z^6$ .

#### **Exercise 1**

1. Factor the following expressions:

a. 
$$4x^2 + 4x - 63$$

b.  $12y^2 - 24y - 15$ 



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### Exercises 2-4

Factor each of the following, and show that the factored form is equivalent to the original expression.

2. 
$$a^3 + 27$$

3. 
$$x^3 - 64$$

4. 
$$2x^3 + 128$$

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## **Lesson Summary**

In this lesson we learned additional strategies for factoring polynomials.

- The difference of squares identity  $a^2 b^2 = (a b)(a + b)$  can be used to to factor more advanced
- Trinomials can often be factored by looking for structure and then applying our previous factoring
- Sums and differences of cubes can be factored by the formulas

$$x^3 + a^3 = (x + a)(x^2 - ax - a^2)$$

$$x^3 - a^3 = (x - a)(x^2 + ax + a^2).$$

#### **Problem Set**

1. If possible, factor the following expressions using the techniques discussed in this lesson.

a. 
$$25x^2 - 25x - 14$$

b. 
$$9x^2y^2 - 18xy + 8$$

c. 
$$45y^2 + 15y - 10$$

d. 
$$y^6 - y^3 - 6$$

e. 
$$x^3 - 125$$

f. 
$$2x^4 - 16x$$

g. 
$$9x^2 - 25y^4z^6$$

h. 
$$36x^6y^4z^2 - 25x^2z^{10}$$

i. 
$$4x^2 + 9$$

j. 
$$x^4 - 36$$

k. 
$$1 + 27x^9$$

I. 
$$x^3y^6 + 8z^3$$

- Consider the polynomial expression  $y^4 + 4y^2 + 16$ .
  - a. Is  $y^4 + 4y^2 + 16$  factorable using the methods we have seen so far?
  - b. Factor  $y^6 64$  first as a difference of cubes, then factor completely:  $(y^2)^3 4^3$ .
  - c. Factor  $y^6 64$  first as a difference of squares, then factor completely:  $(y^3)^2 8^2$ .
  - Explain how your answers to parts (b) and (c) provide a factorization of  $y^4 + 4y^2 + 16$ .
  - If a polynomial can be factored as either a difference of squares or a difference of cubes, which formula should you apply first, and why?
- 3. Create expressions that have a structure that allows them to be factored using the specified identity. Be creative and produce challenging problems!
  - Difference of squares
  - b. Difference of cubes
  - Sum of cubes



